

FRANC3D / OSM

Overview Slides

October, 2003

Cornell Fracture Group

INTRODUCTION



<http://ppe.navail.navy.mil>

Realistic 3D crack growth simulations require:

- actual geometric models, including crack(s)
- ability to discretize and analyze the model
- ability to post-process analysis results
- and the ability to incorporate the results into design and/or assessment

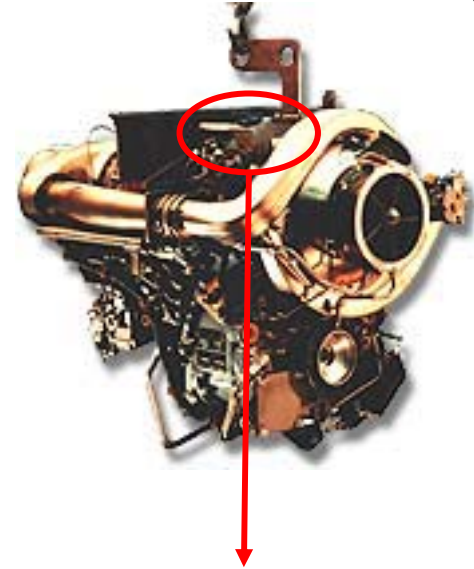
A framework for simulation requires:

- an intuitive, relatively simple, user interface
- sophisticated capabilities, while hiding complex details
- automation, speed, efficiency
- testing, benchmarking, and support

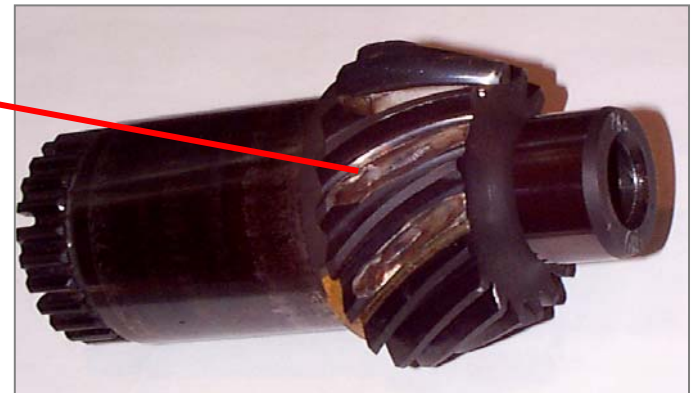
Example: Life Prediction in Transmission Gears



Allison 250-C30R Engine



Fatigue Cracks in Spiral Bevel
Power Transmission Gear



*U.S. Army Vehicle Technology Center
NASA/Lewis Research Center*

Constrained Shape: Known Solution Method

Characteristic—Library:

look-up stress intensity factor solutions for finite number of simple shapes and boundary conditions

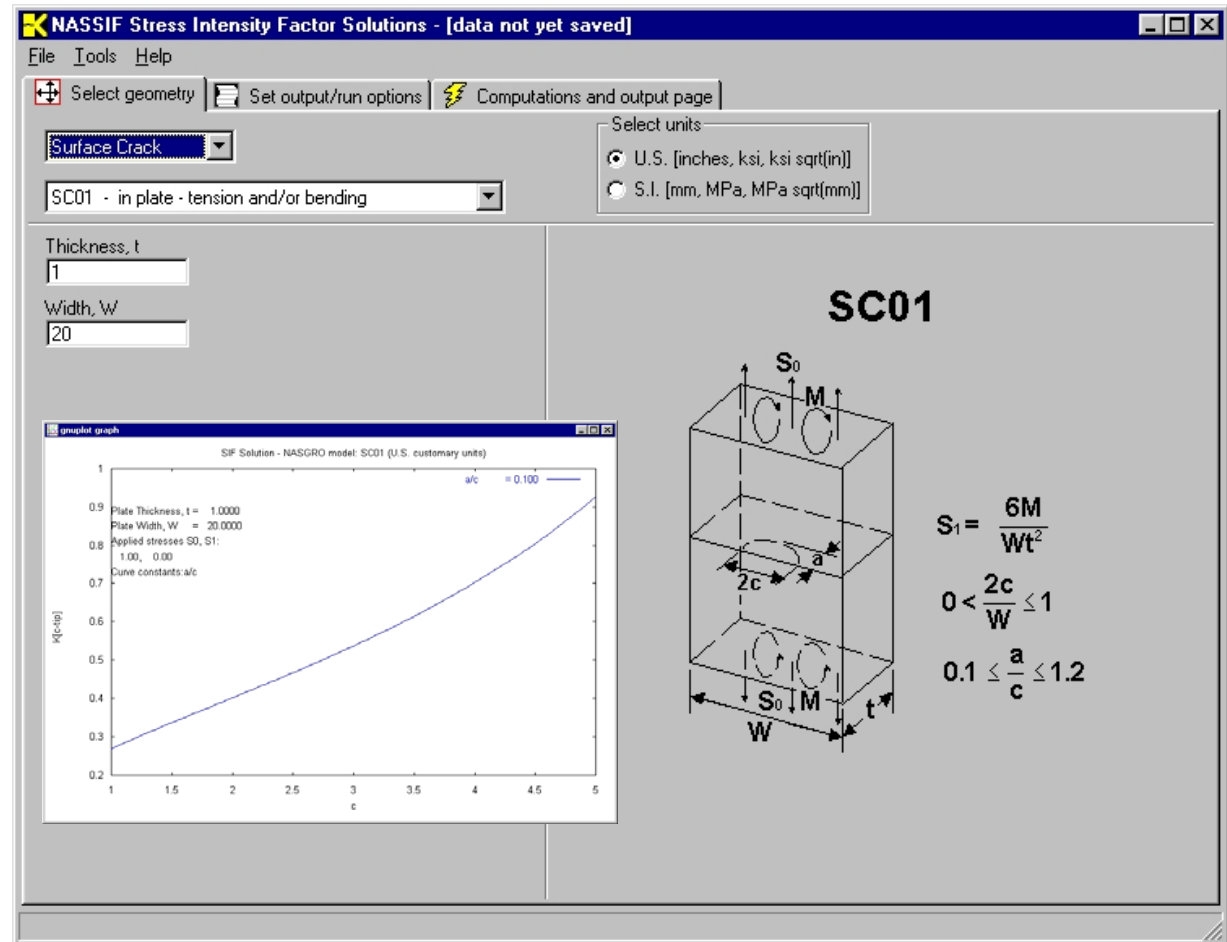
Benefits:

no model to build,
no meshing,
fast analysis,
simple interface.

Drawbacks:

models do not match real geometry and boundary conditions,
no multi-scale,
no multi-physics.
A fast, accurate solution to the wrong problem.

Examples: NASGRO, AFGROW



Unconstrained Shape: Computed Solution

FRANC3D:

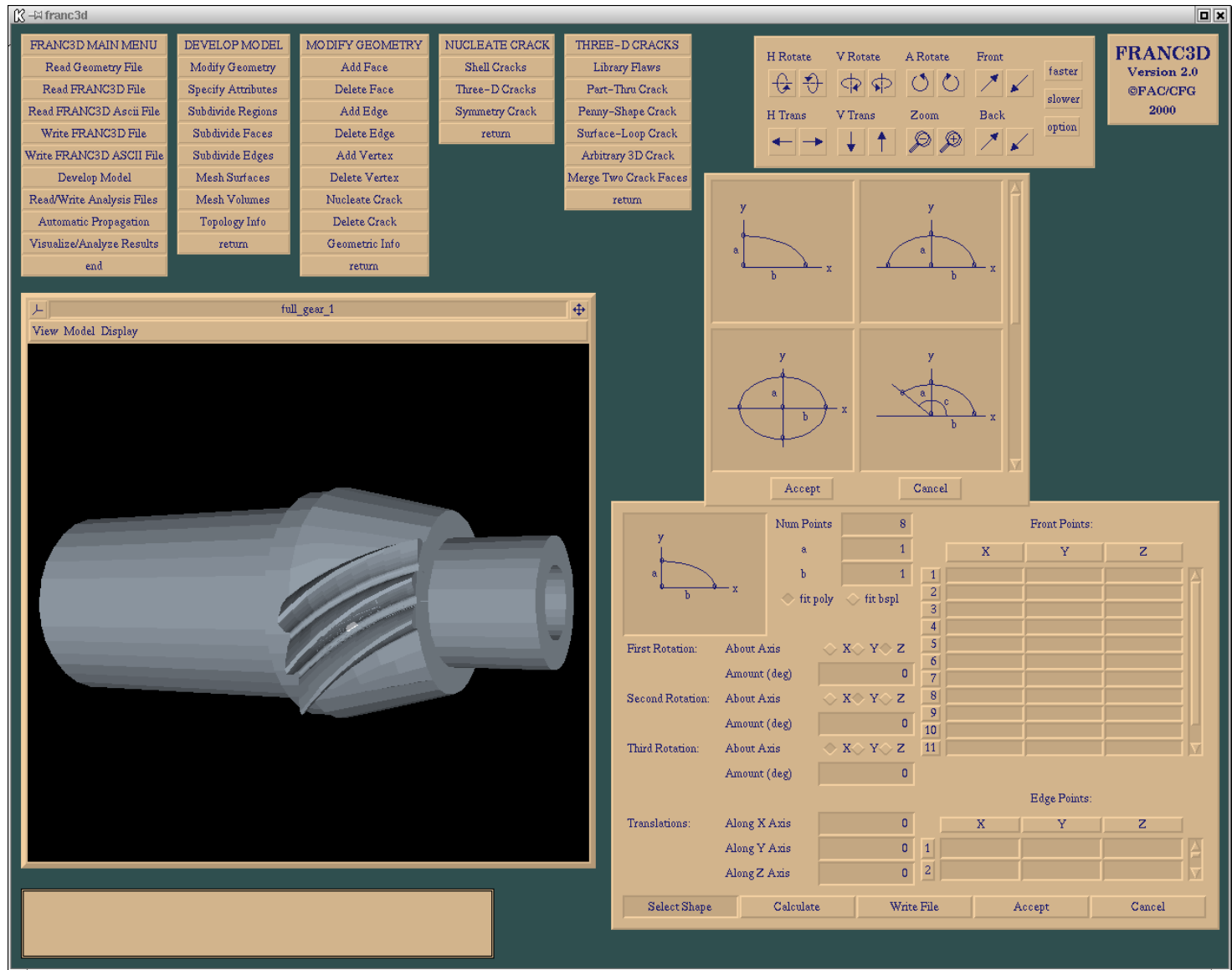
actual part
with actual
boundary
conditions

Benefits:

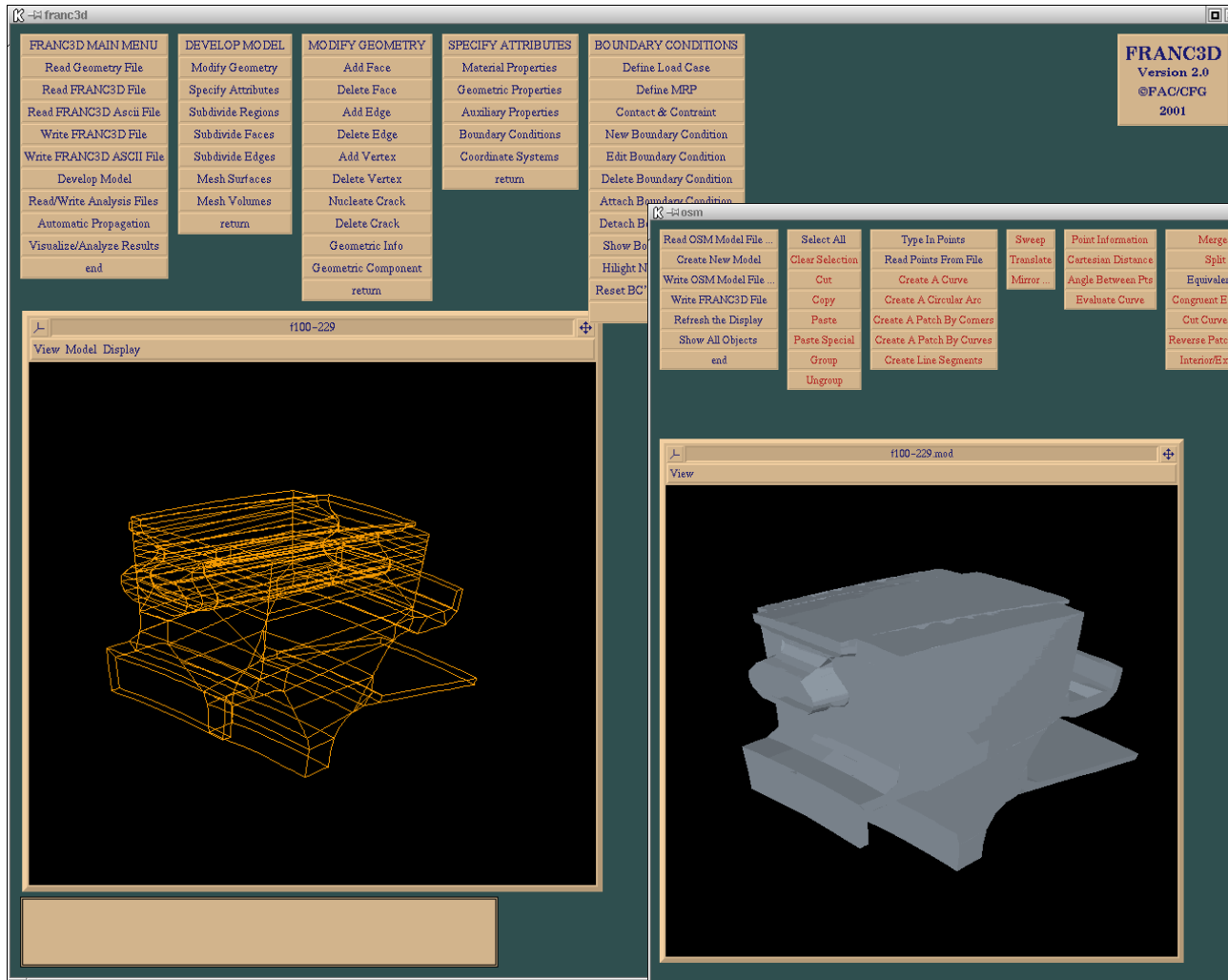
realistic
solution,
multi-scale,
multi-physics
capable.

Drawbacks:

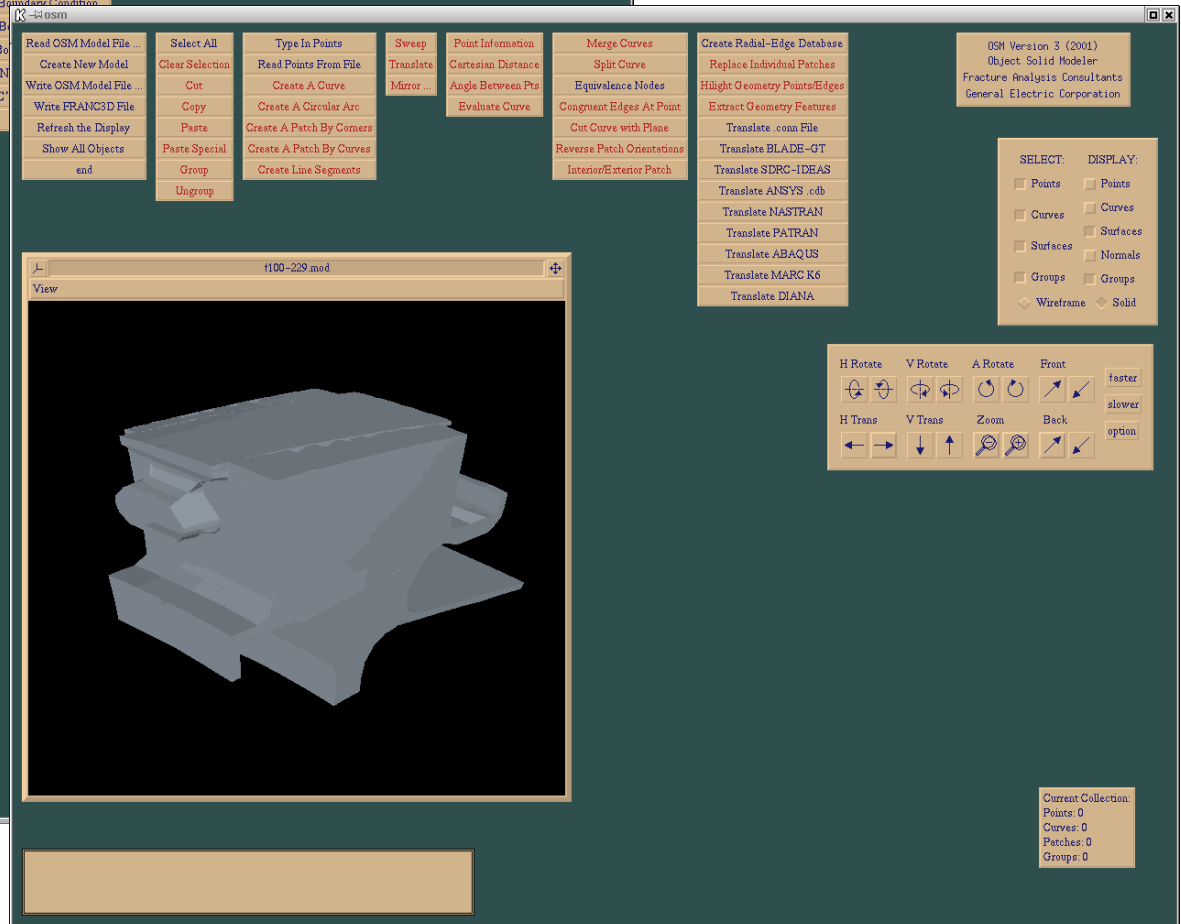
time
consuming.



FRANC3D / OSM



X Windows-based,
menu driven,
C code



FRANC3D / OSM

what they are and are not!

FRacture ANalysis Code - 3D

❖ hybrid software that combines solid modeling, mesh generation, and fracture mechanics for nucleating and propagating cracks in the model geometry.

FRANC3D is not a boundary nor a finite element analysis code, although it is capable of writing input files for a variety of in-house and commercial BEM and FEM codes.

Object Solid Modeler

❖ generates boundary representation (B-rep) solid model for FRANC3D from user-defined geometry points, curves and surfaces, or by converting FEM data.

OSM is not a general purpose solid modeler or CAD program.

Supported FEM / BEM Analysis Codes

BES - Cornell University Boundary Element System

CPTC - Cornell University parallel finite element code
(ongoing research and development)

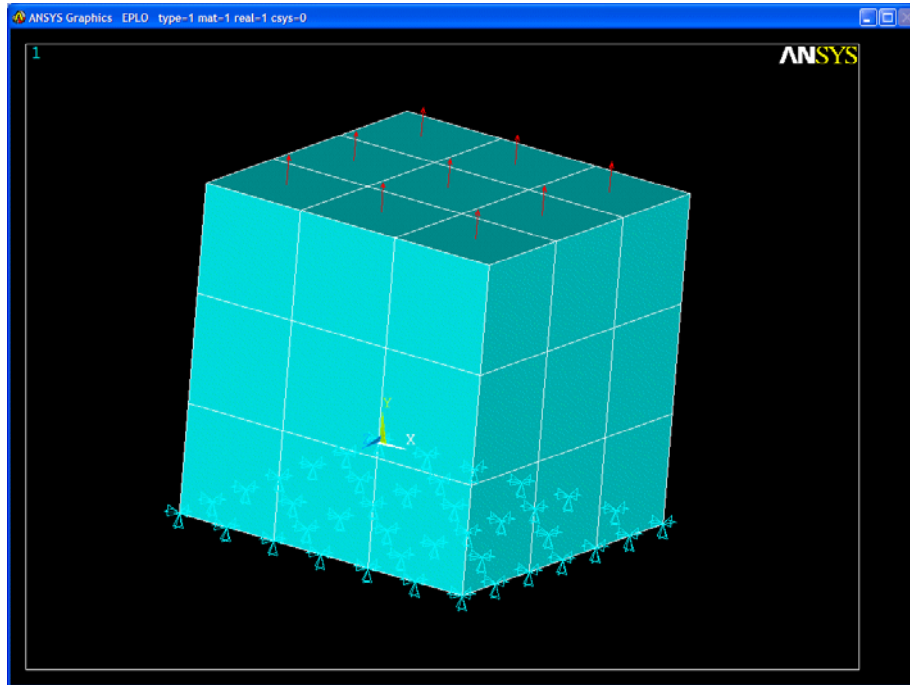
Overview of Simulation Process

- a B-rep solid model is the primary input to FRANC3D;
this normally is generated by OSM.
- boundary conditions can be specified within FRANC3D;
these include imposed loads, imposed displacements, temperatures,
and crack face pressure interpolated from finite element stresses
- material properties can be specified within FRANC3D;
available materials include elastic, orthotropic, and elasto-plastic.
- the model is discretized or meshed within FRANC3D;
this could include surface (for BEM) and volume meshing (ANSYS).
- analysis input files are generated by FRANC3D.
- an external program provides displacements and stresses;
these should be imported into FRANC3D.

Overview of Simulation Process (continued)

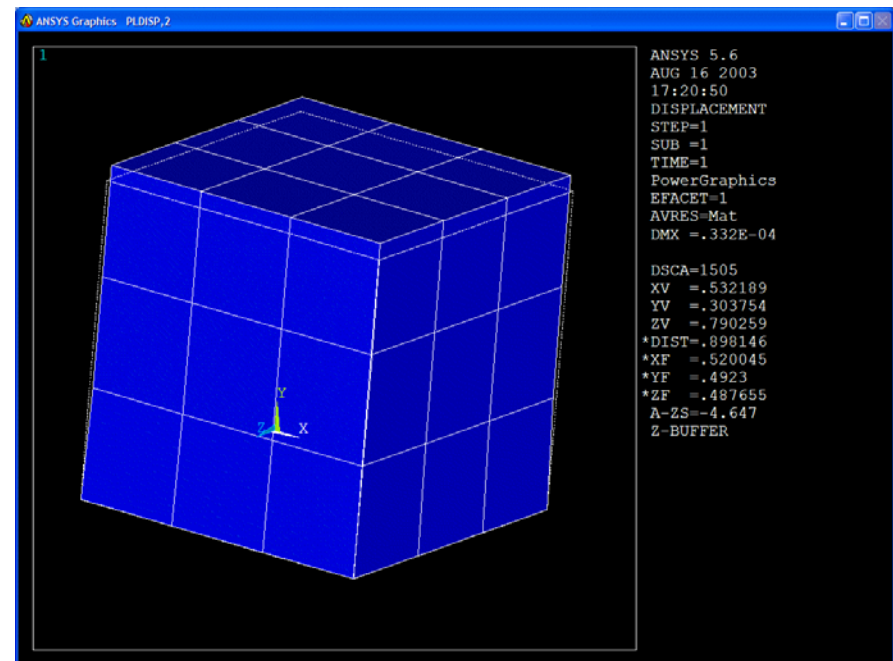
- one or more **flaws can be initiated in the model**; the location, orientation, size and shape could be based on the stress analysis, or based on field evidence, or completely arbitrary
- fracture parameters, such as **stress-intensity factors, are computed** based on the displacements from the external stress analysis (e.g. ANSYS).
- **crack propagation** is based on the computed fracture parameters and a “rule” to predict the new crack front – orientation and advance. The model geometry is modified automatically to grow the crack.
- a history of the stress intensity factors as a function of the flaw size can be used in conjunction with the crack growth properties of the material and load history to make a **prediction of the fatigue life**.

Simple Cube Example – Hands-on-training



- simple cube with 3x3x3 grid of SOLID95 elements
- kinematic constraint on base nodes
- surface traction on upper surface
- linear elastic ANSYS analysis

- demonstrate ANSYS FEM to OSM conversion
- demonstrate MRP boundary conditions – transfer ANSYS stresses to crack face tractions for BEM analysis

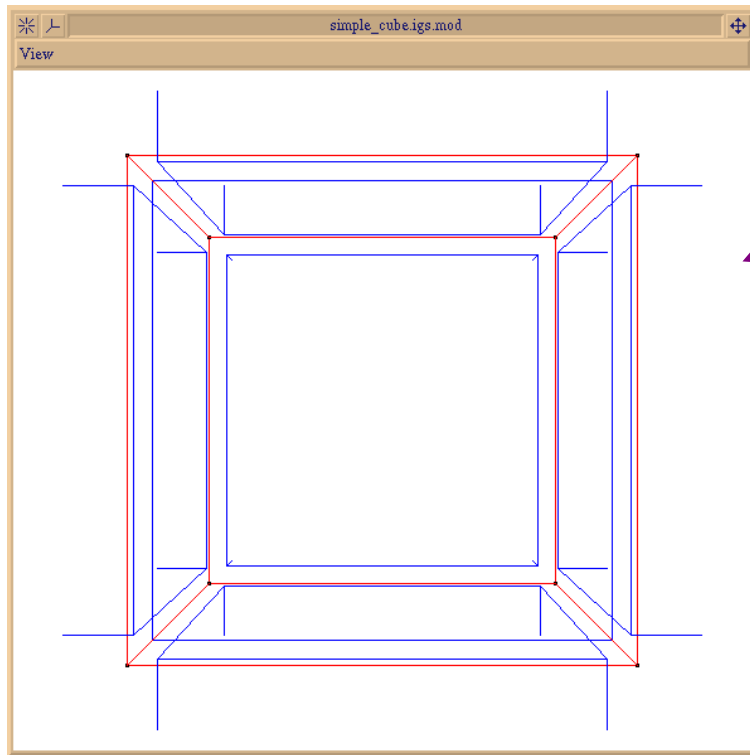


Simple Cube Example

Steps:

- read the ANSYS .cdb and .igs files into OSM and extract the geometry features
- discuss MRP's generated by OSM from ANSYS .cdb file and from ANSYS nodal results saved as .dsp and .str files
- read model into FRANC3D and apply MRP boundary conditions
- add a crack and analyze using BES
- compare stress intensity factors based on both BES and ANSYS results

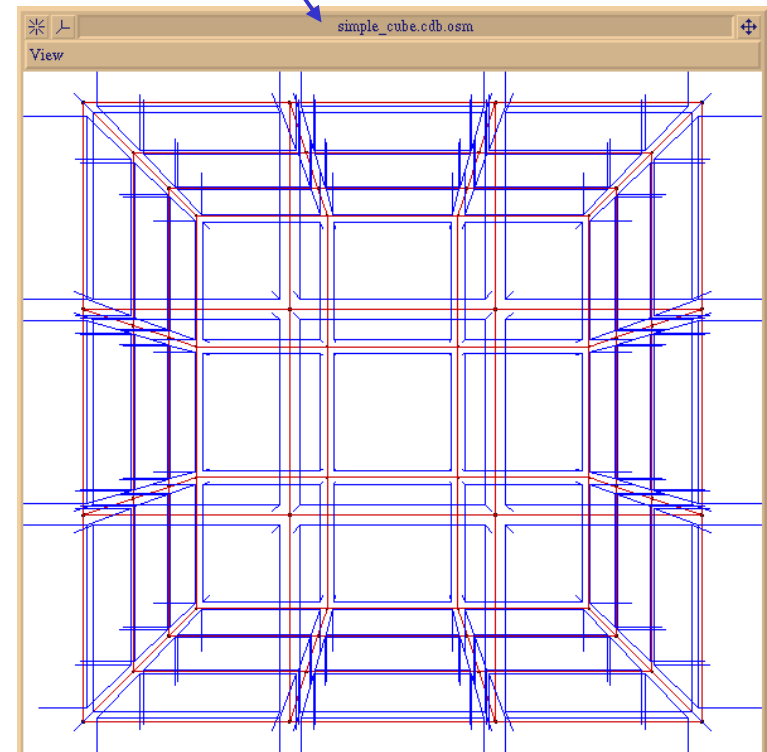
Simple Cube Example



iges file contains only geometry
and if a solid model does not exist
there is no iges information

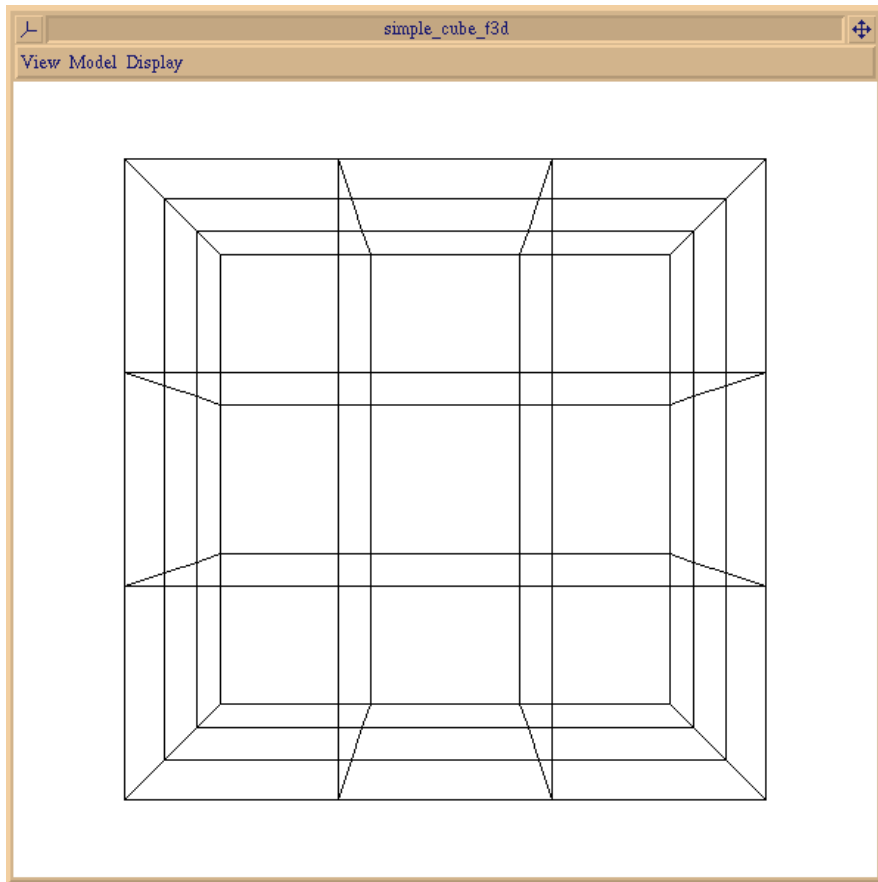
- Create Radial-Edge Database
- Highlight Geometry Points/Edges
- Extract Geometry Features
- Translate ANSYS .cdb
- Translate ANSYS .igs

OSM can convert ANSYS
iges and cdb files

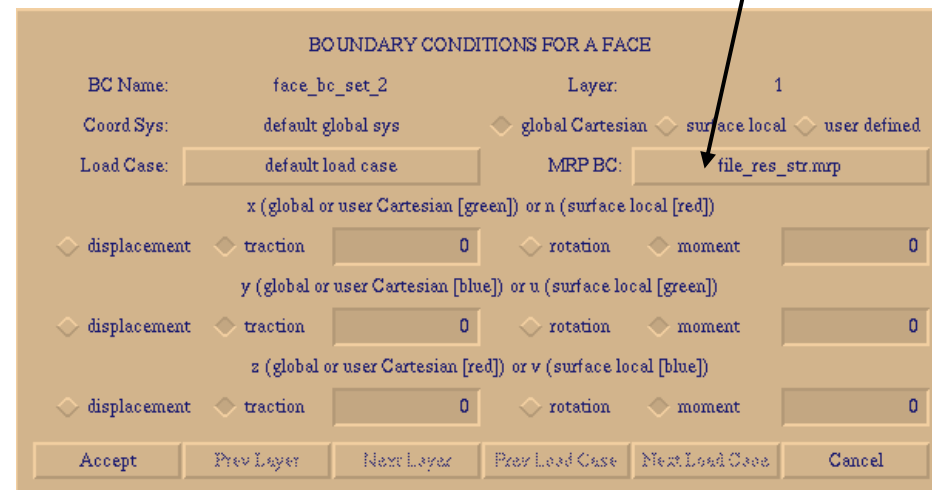
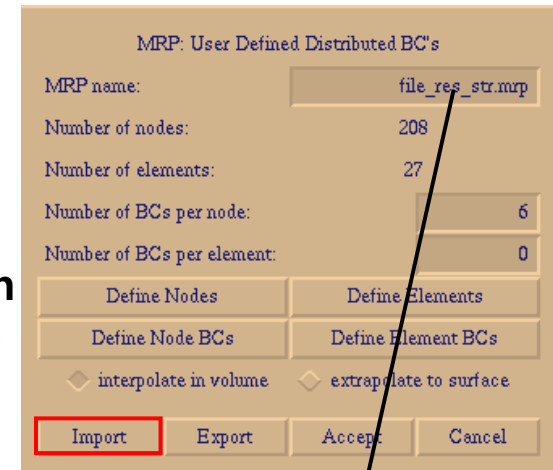


cdb file contains finite element
mesh information along with
boundary conditions and materials

Simple Cube Example



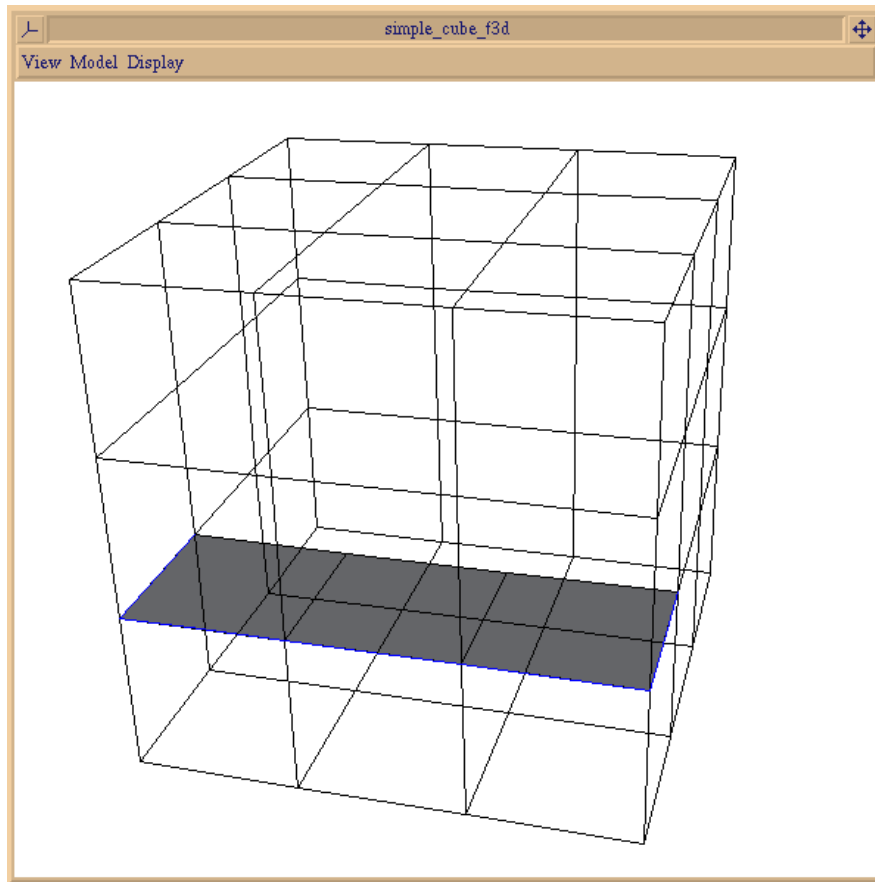
OSM reads the .str file and saves a _res_str.mrp file that contains the mesh information from the .cdb file as well as the stress results



We can use the ANSYS mesh facets to define FRANC3D geometry, but it is not recommended for big models.

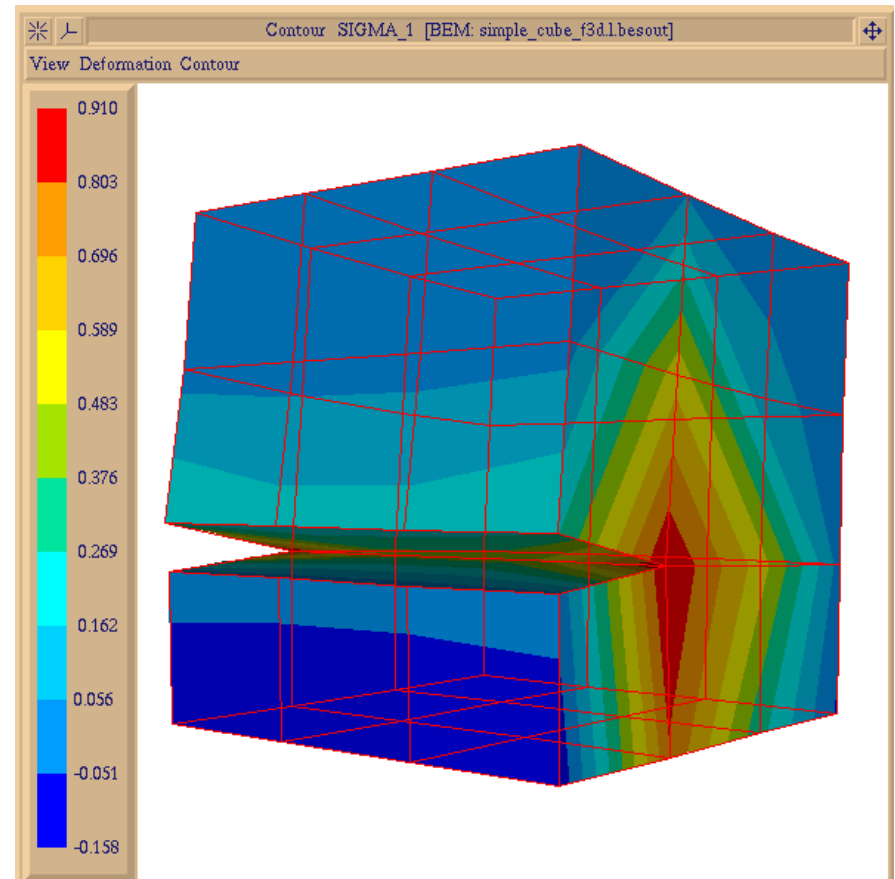
The MRP is Imported into FRANC3D and used in the Face Boundary Condition dialog box – this is then attached to the crack surface.

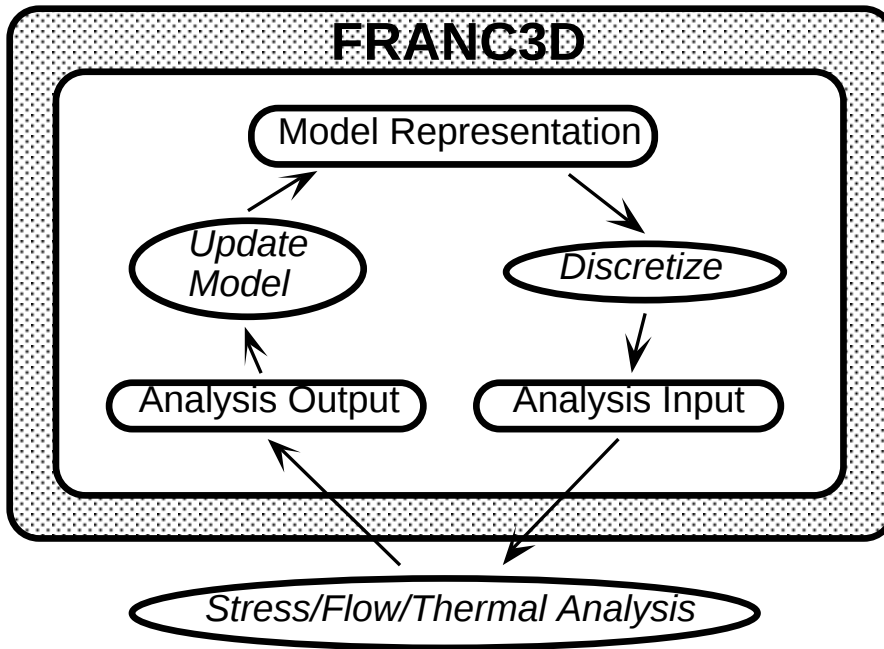
Simple Cube Example



A part through crack is inserted into the FRANC3D model and the face boundary condition defined previously is attached to this surface.

The BEM analysis provides the stresses and displacements for the cracked model. Stress intensity factors can be computed.

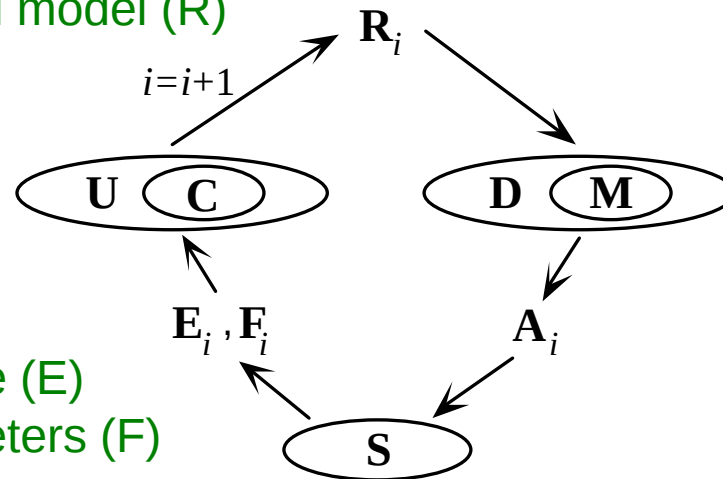




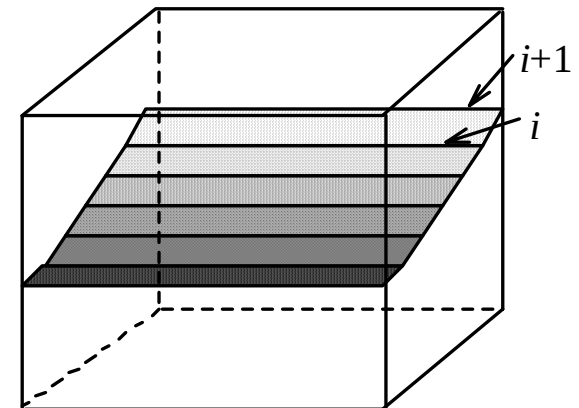
FRANC3D Concepts

- incremental process involving 'n' steps of crack growth in a "true" geometric model of the structure.

Representational model (R)

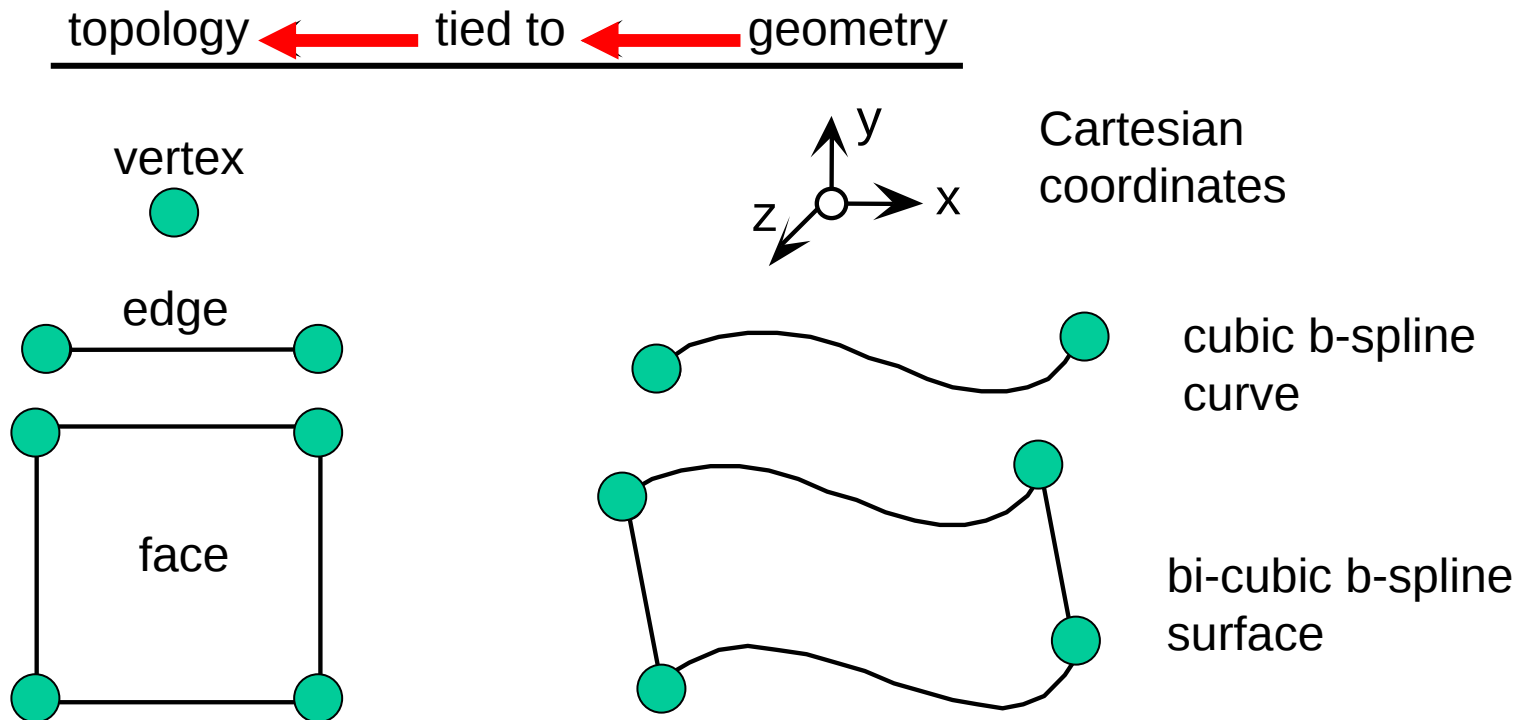


Equilibrium state (E)
Fracture parameters (F)



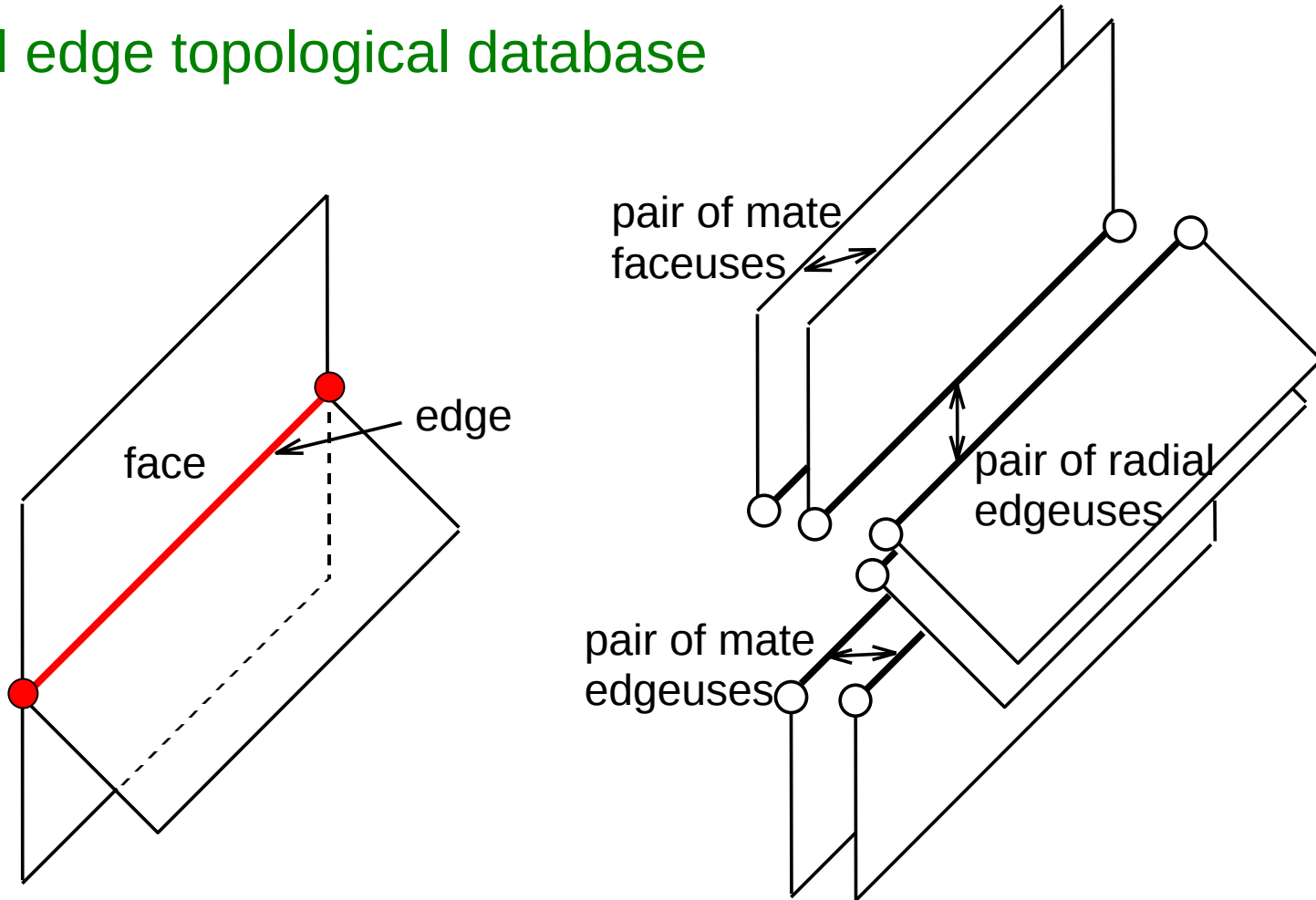
Geometric Model and Topology

The essence of the problem is predicting and tracking the changing geometry as the crack grows. A topology-based data structure underlies the solid model geometry, which allows for efficient interaction and accurate representation of evolving cracks.



Geometric Model and Topology

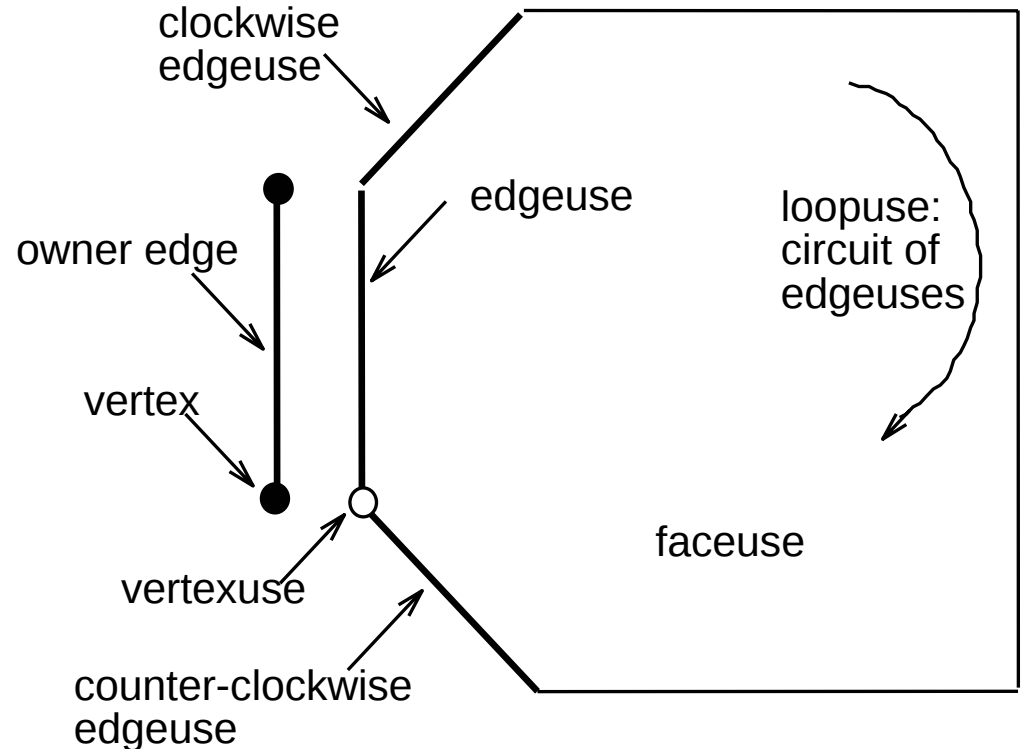
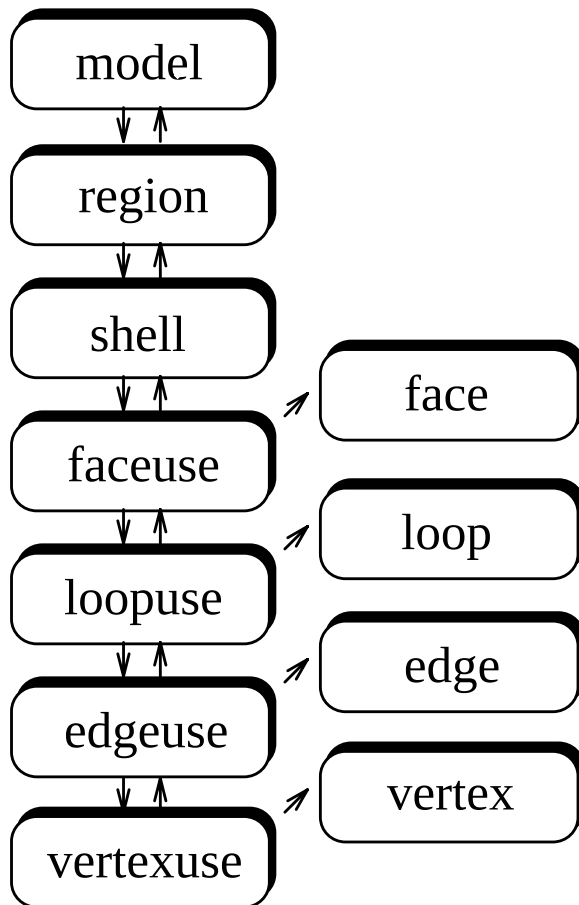
radial edge topological database



Topological edges provide ordering based on the edge uses.

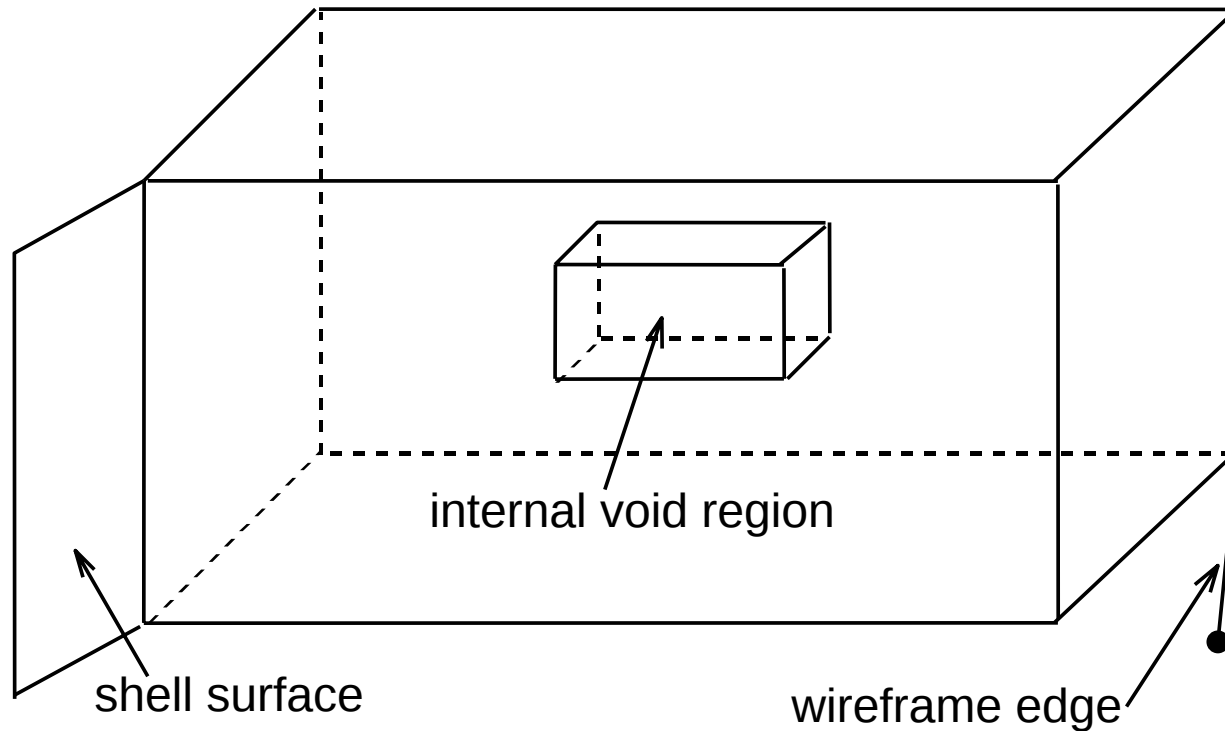
Geometric Model and Topology

Topological entities have orientations and uses and the data is stored accordingly, such that traversals and queries are efficient.



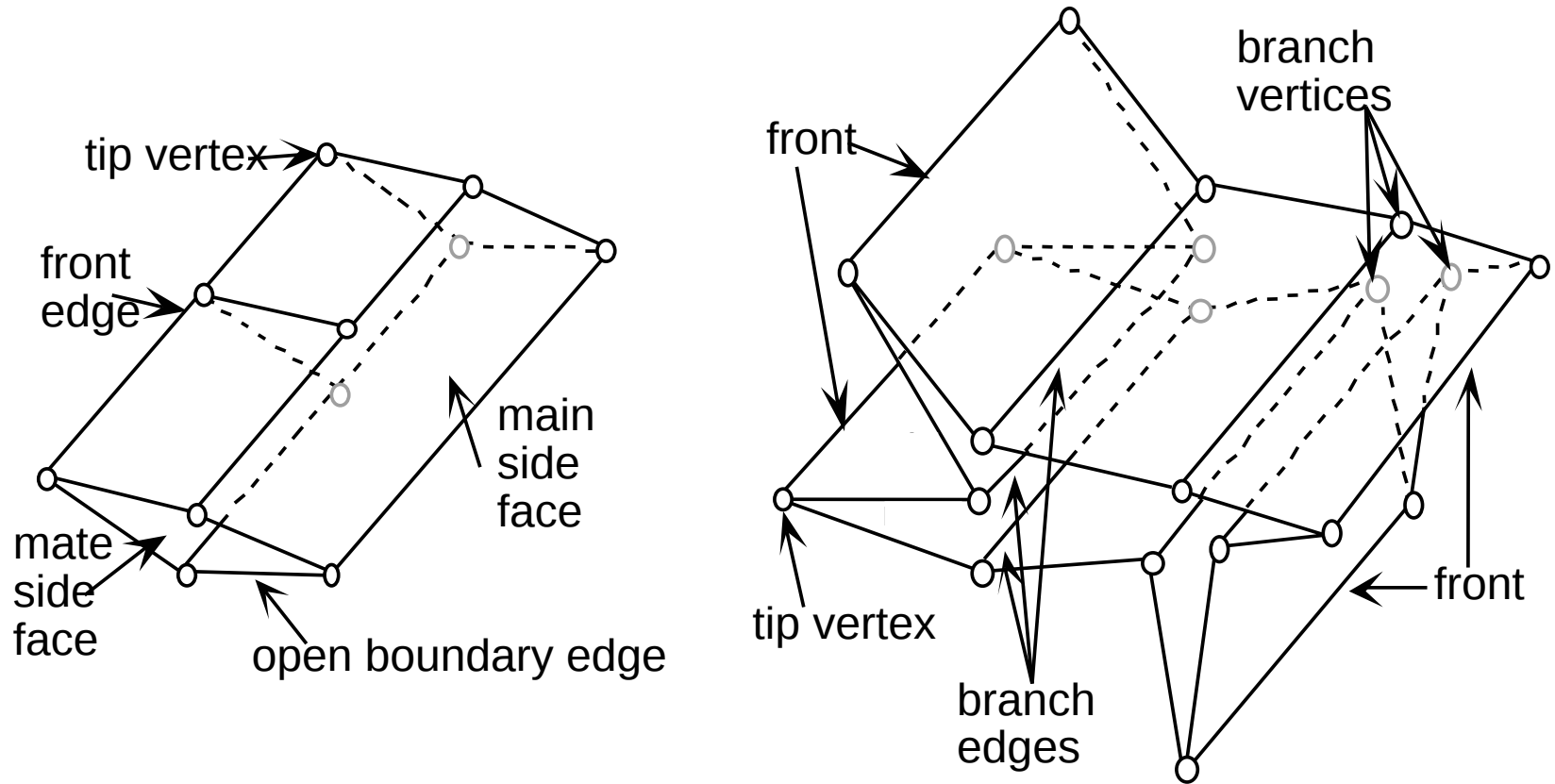
Geometric Model and Topology

Allows for the definition of complex topological models,



including the definition of complex cracks.

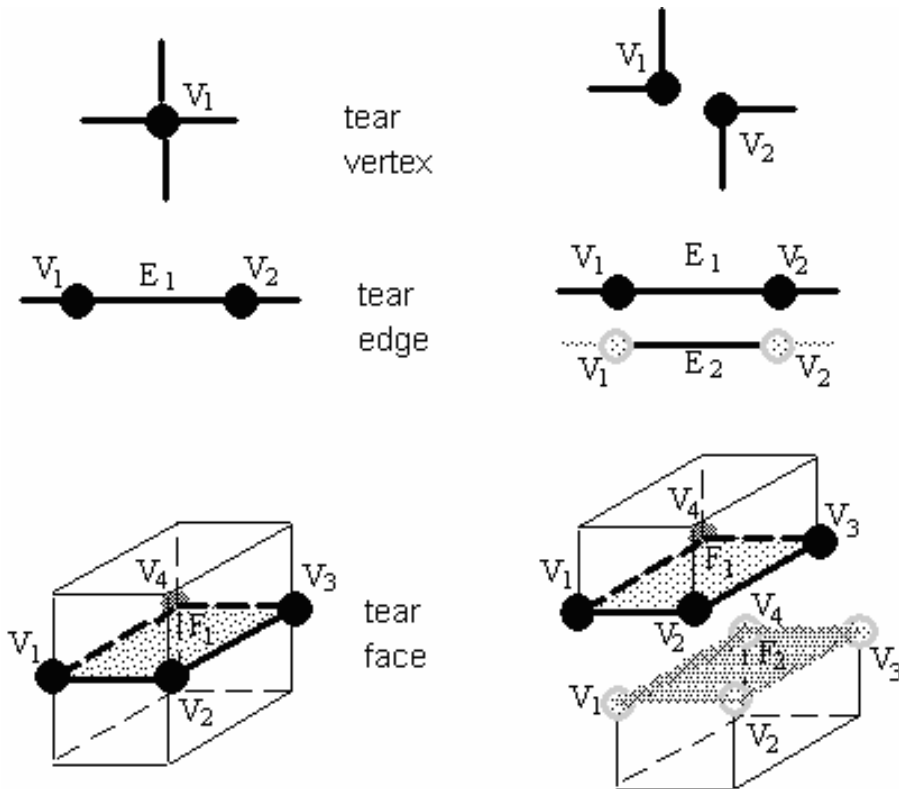
Geometric Model and Topology



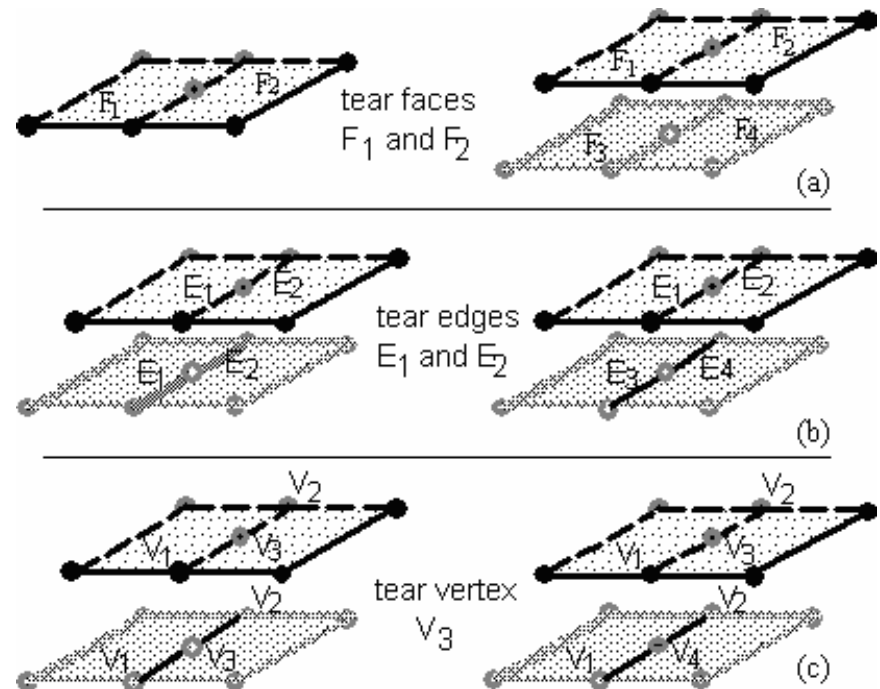
- main and mate crack topological surfaces share the same geometry
- the normal to the main side surface points into the crack towards the mate
- the crack tip and branch vertices mark the ends of crack fronts
- crack fronts can grow independently

Topological Operators for Cracks

tear operators



tear operators are used in sequence to create a crack



glue operators can be used to delete a crack

Crack Nucleation

NUCLEATE CRACK

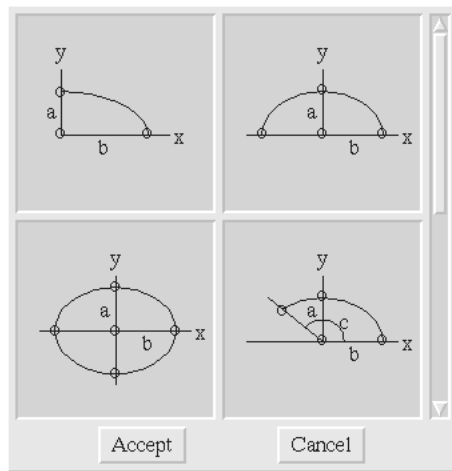
- Shell Cracks
- Three-D Cracks
- Symmetry Crack
- return

THREE-D CRACKS

- Library Flaws
- Part-Thru Crack
- Penny-Shape Crack
- Surface-Loop Crack
- Arbitrary 3D Crack
- Merge Two Crack Faces
- return

show library of flaws
read flaw from file
show flaw in model
create flaw in model
cancel

a library of common flaw shapes



Num Points: 8

a: .01

b: .005

☐ fit poly ☐ fit bspl

First Rotation: About Axis ☐ X ☒ Y ☐ Z
Amount (deg): 90

Second Rotation: About Axis ☐ X ☒ Y ☐ Z
Amount (deg): 37

Third Rotation: About Axis ☒ X ☐ Y ☐ Z
Amount (deg): 0

Translations: Along X Axis: 14.5
Along Y Axis: 3.2
Along Z Axis: 7.4567

Front Points:

	X	Y	Z
1	14.492	3.2	7.46272
2	14.4924	3.20162	7.46239
3	14.4934	3.20283	7.46166
4	14.4946	3.20369	7.46076
5	14.4959	3.20429	7.45978
6	14.4973	3.20469	7.45877
7	14.4986	3.20492	7.45774
8	14.5	3.205	7.4567
9			
10			

Edge Points:

	X	Y	Z
1	14.5	3.205	7.4567
2	14.5	3.2	7.4567

Select Shape Calculate Write File Accept Cancel

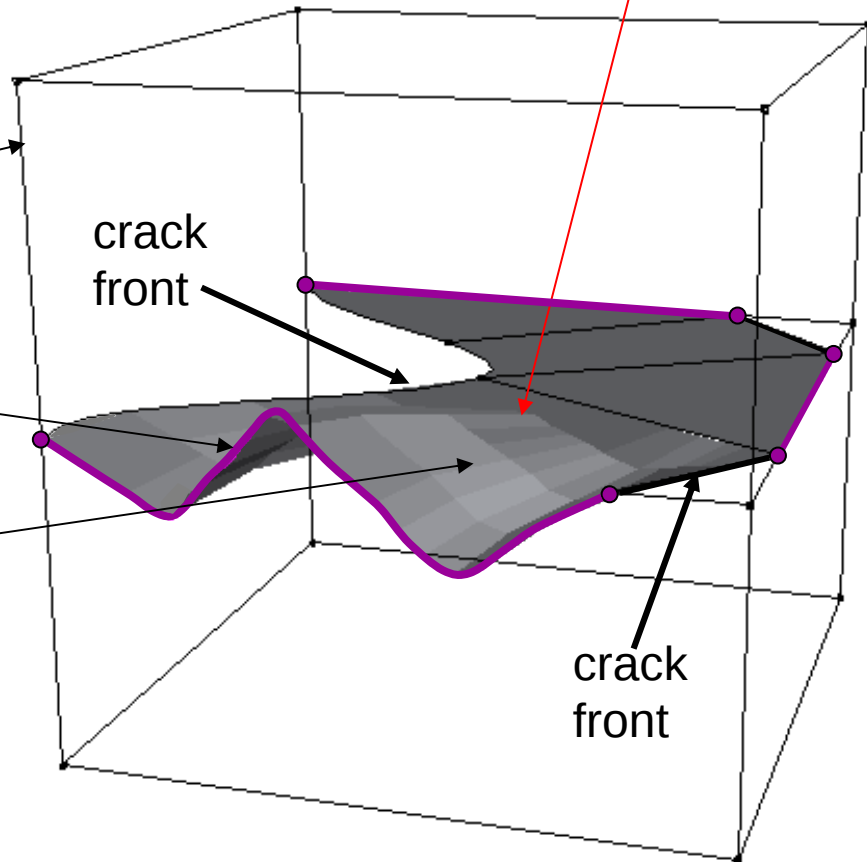
A crack can be nucleated manually by adding the edges and faces and 'tearing' the entities using the **Arbitrary 3D Crack** menu option.

Crack Nucleation

Completely arbitrary initial flaws (arbitrary size, orientation, location, and shape, including non-planar flaws) can be specified in the geometrical model.

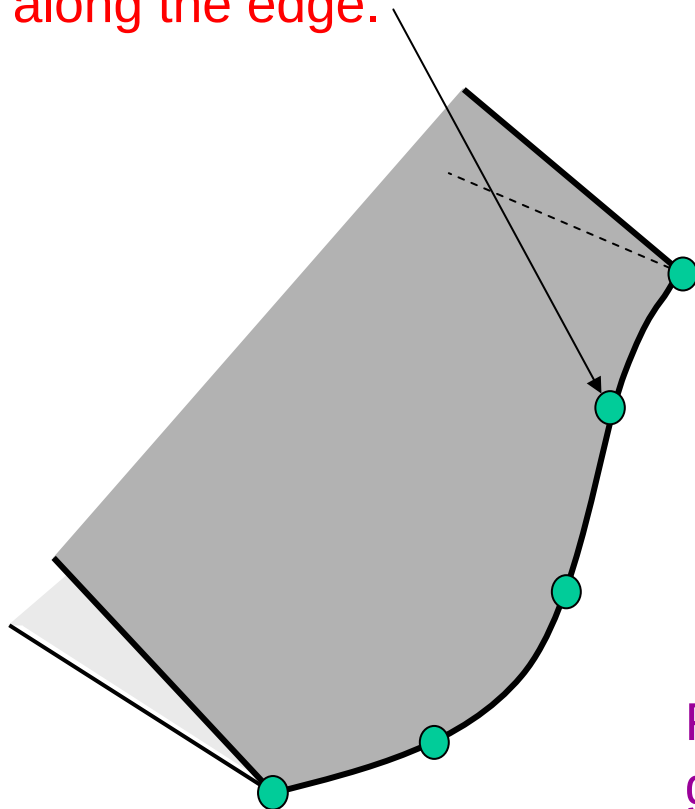
- start with a cube
- define edges on the surfaces and in the interior
- define faces from the edges
- pick the faces and create a crack

THREE-D CRACKS
Library Flaws
Part-Thru Crack
Penny-Shape Crack
Surface-Loop Crack
Arbitrary 3D Crack
Merge Two Crack Faces
return

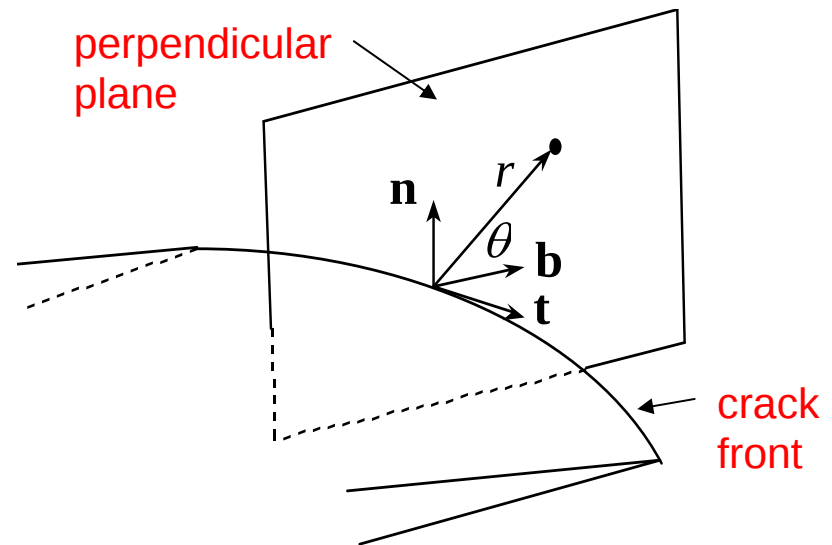


Crack Propagation

The 3D crack front is divided into a number of segments by defining geometric points along the edge.

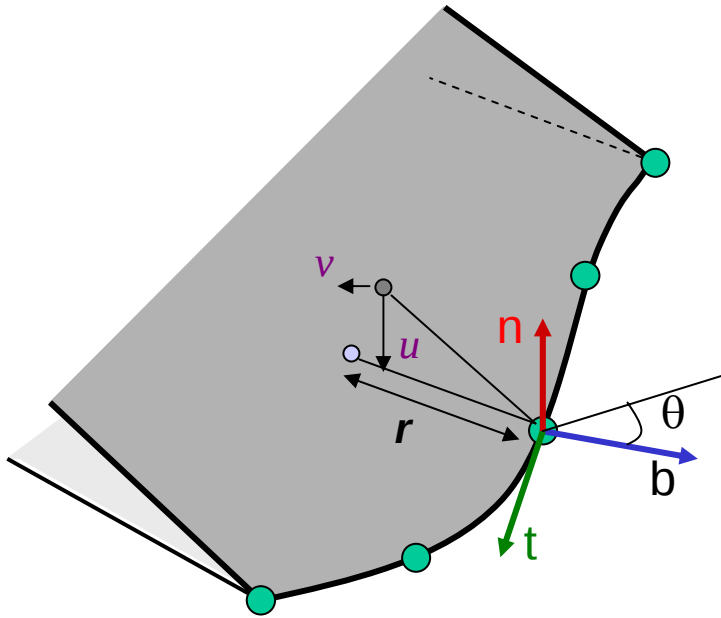


At each point, the plane orthogonal to the local tangent on the crack front is defined and 2D theories for crack growth are invoked.



Fracture mechanics theories and crack growth models are encapsulated in easily modified modules.

Crack Propagation: Displacement Correlation

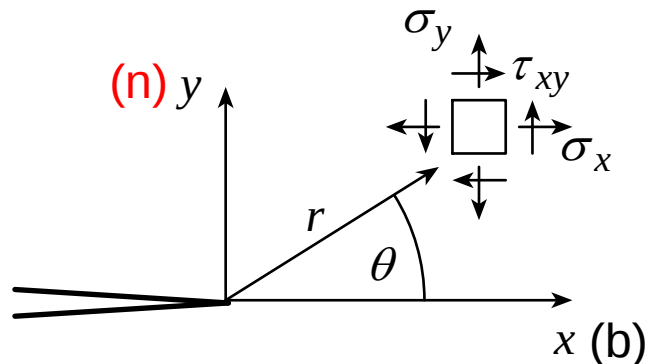


Stress and displacement near the crack tip as a function of r and θ :

$$\sigma_x = \frac{K_I}{\sqrt{2\pi r}} \cos \frac{\theta}{2} \left(1 - \sin \frac{\theta}{2} \sin \frac{3\theta}{2} \right)$$

$$\sigma_y = \frac{K_I}{\sqrt{2\pi r}} \cos \frac{\theta}{2} \left(1 + \sin \frac{\theta}{2} \sin \frac{3\theta}{2} \right)$$

$$\tau_{xy} = \frac{K_I}{\sqrt{2\pi r}} \sin \frac{\theta}{2} \cos \frac{\theta}{2} \cos \frac{3\theta}{2}$$



$$u = 2(1 + \nu) \frac{K_I}{E} \sqrt{\frac{r}{2\pi}} \cos \frac{\theta}{2} \left[1 - 2\nu + \sin^2 \frac{\theta}{2} \right]$$

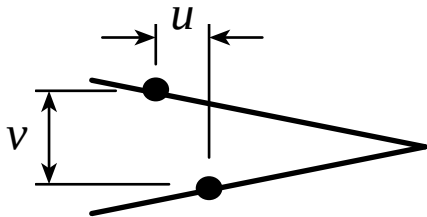
$$v = 2(1 + \nu) \frac{K_I}{E} \sqrt{\frac{r}{2\pi}} \sin \frac{\theta}{2} \left[2 - 2\nu - \cos^2 \frac{\theta}{2} \right]$$

Crack Propagation: Displacement Correlation

Stress intensity factors can be extracted from boundary or finite element analyses using displacement correlation:

The crack-tip displacement fields are given by:

$$\begin{Bmatrix} u \\ v \end{Bmatrix} = 2(1+\nu) \frac{K_I}{E} \sqrt{\frac{r}{2\pi}} \begin{Bmatrix} \cos \frac{\theta}{2} \left[1 - 2\nu + \sin^2 \frac{\theta}{2} \right] \\ \sin \frac{\theta}{2} \left[2 - 2\nu + \cos^2 \frac{\theta}{2} \right] \end{Bmatrix} + 2(1+\nu) \frac{K_{II}}{E} \sqrt{\frac{r}{2\pi}} \begin{Bmatrix} \sin \frac{\theta}{2} \left[2 - 2\nu + \cos^2 \frac{\theta}{2} \right] \\ \cos \frac{\theta}{2} \left[-1 + 2\nu + \sin^2 \frac{\theta}{2} \right] \end{Bmatrix}$$



At 180 degrees, along the crack flank:

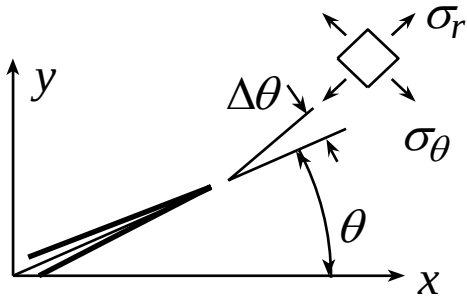
$$\begin{Bmatrix} u \\ v \end{Bmatrix} = \frac{(1+\nu)(1-\nu)}{E} \sqrt{\frac{r}{2\pi}} \begin{Bmatrix} K_{II} \\ K_I \end{Bmatrix}$$

Using displacements from a finite or boundary element analysis, we can solve for the K's:

$$\begin{Bmatrix} K_{II} \\ K_I \end{Bmatrix} = \frac{E}{(1+\nu)(1-\nu)} \sqrt{\frac{2\pi}{r}} \begin{Bmatrix} u_{FEM} \\ v_{FEM} \end{Bmatrix}$$

Crack Propagation: Direction and Extension

Maximum Hoop Stress Criterion: $\sigma_{\theta\theta}$ is maximum when $\sigma_{r\theta} = 0$

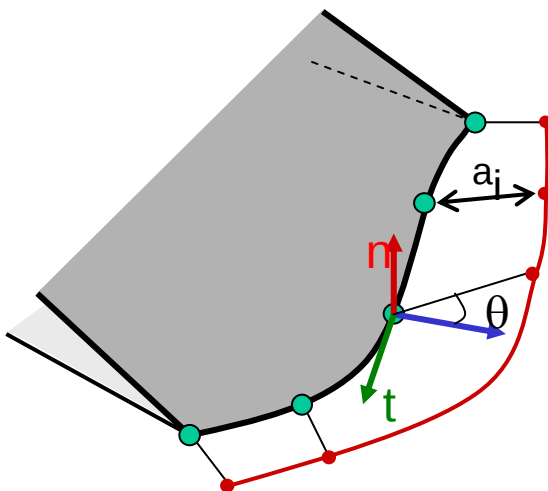


crack-tip “kinks” in the direction where $\sigma_{r\theta} = 0$

$$\sigma_{r\theta} = \frac{K_I}{\sqrt{2\pi r}} \sin \frac{\theta}{2} \cos^2 \frac{\theta}{2} + \frac{K_{II}}{\sqrt{2\pi r}} \left(\frac{1}{4} \cos \frac{\theta}{2} + \frac{3}{4} \cos \frac{3\theta}{2} \right)$$

Solve for θ :

$$\tan \frac{\theta_0}{2} = \frac{1}{4} \frac{K_I}{K_{II}} \pm \frac{1}{4} \sqrt{\left(\frac{K_I}{K_{II}} \right)^2 + 8}$$



Crack Extension Rule:

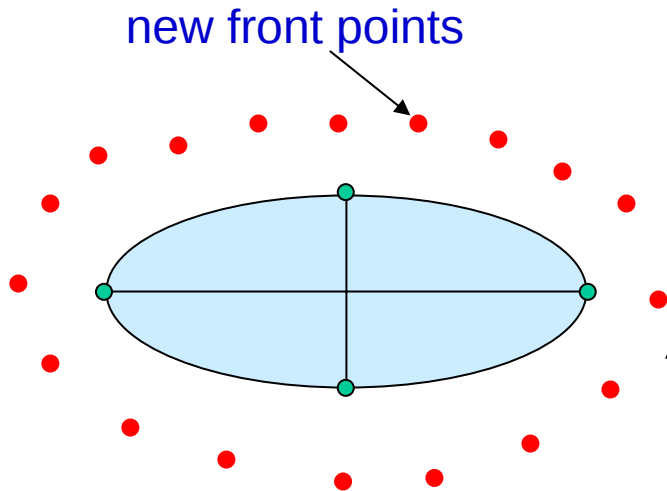
$$a_i = a_{\max} \left[\frac{K_I}{K_{I \max}} \right]^b$$

$a_{\max}$ is user defined

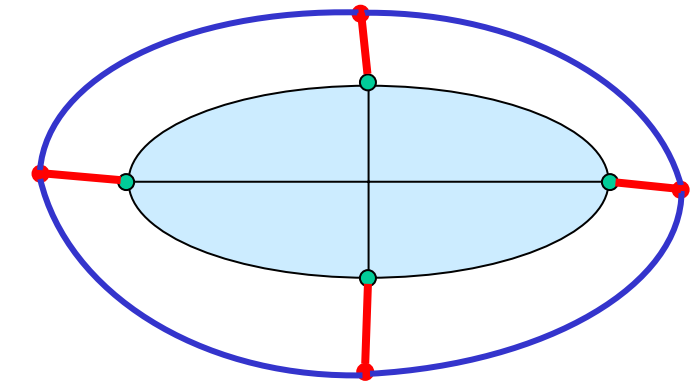
$K_{I \max}$ is the maximum computed K_I

Crack Propagation

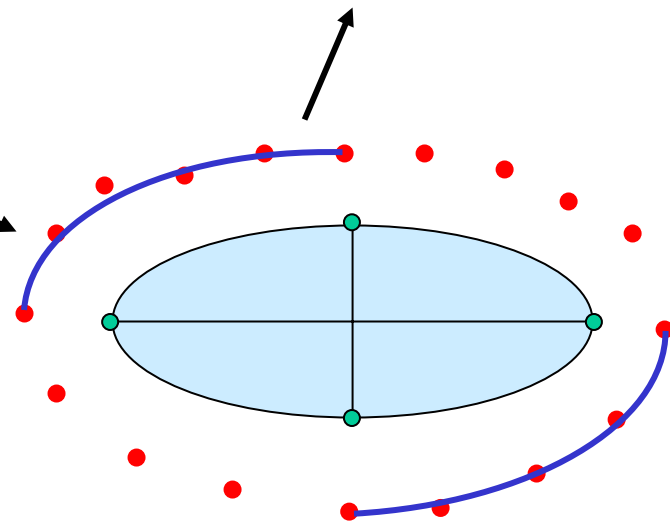
At each point on the crack front, a new front point is computed.



The new front points are smoothed by doing least-squares fitting of polynomials.

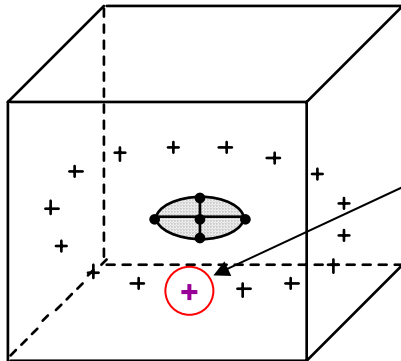


connect old and new front edges and create faces

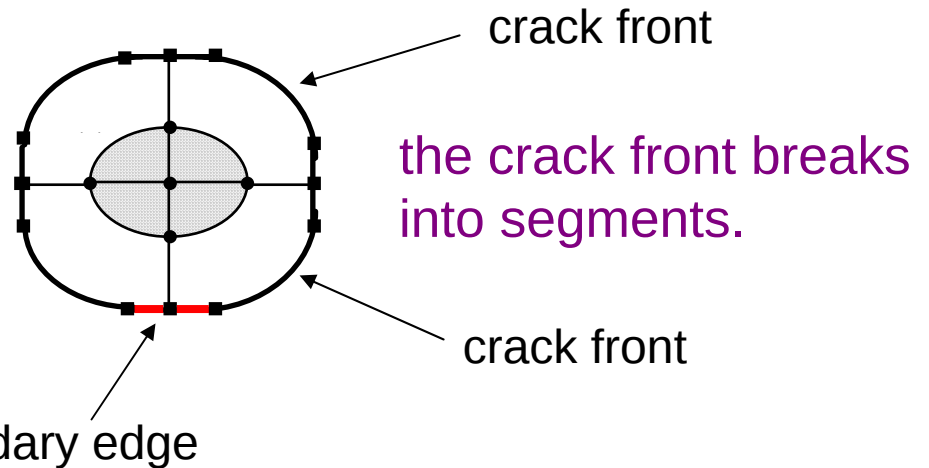


curve fitting & smoothing

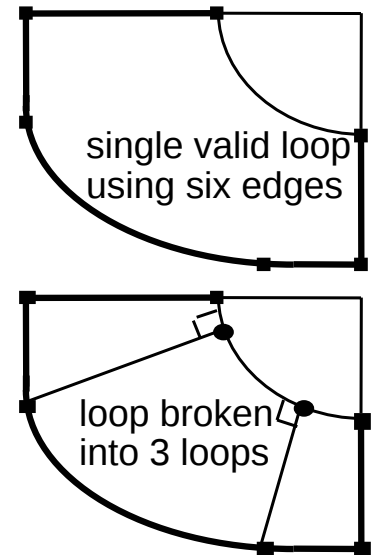
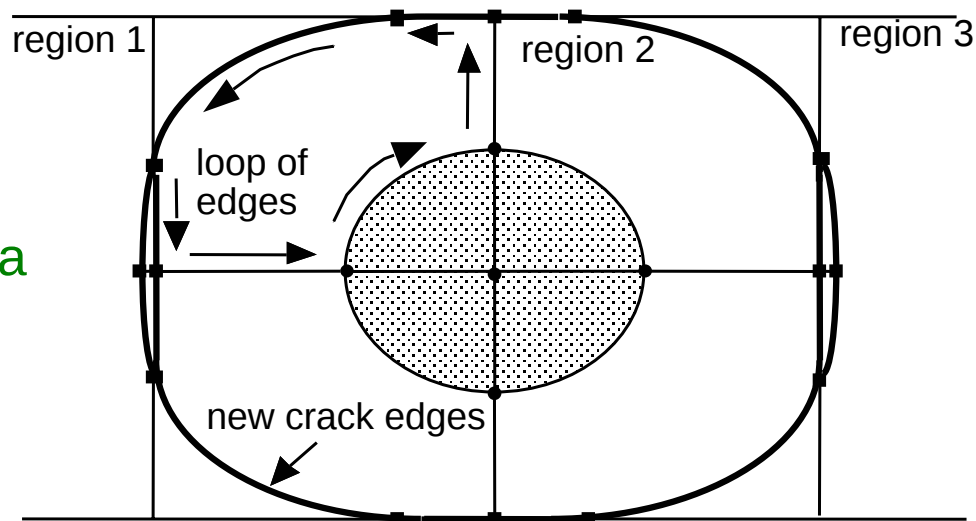
Crack Propagation



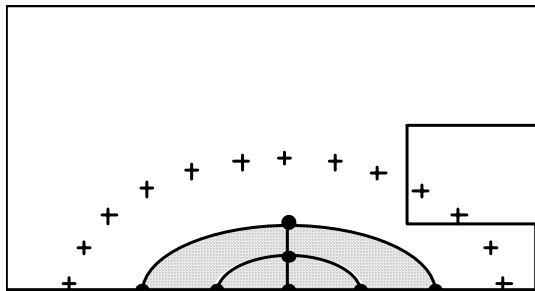
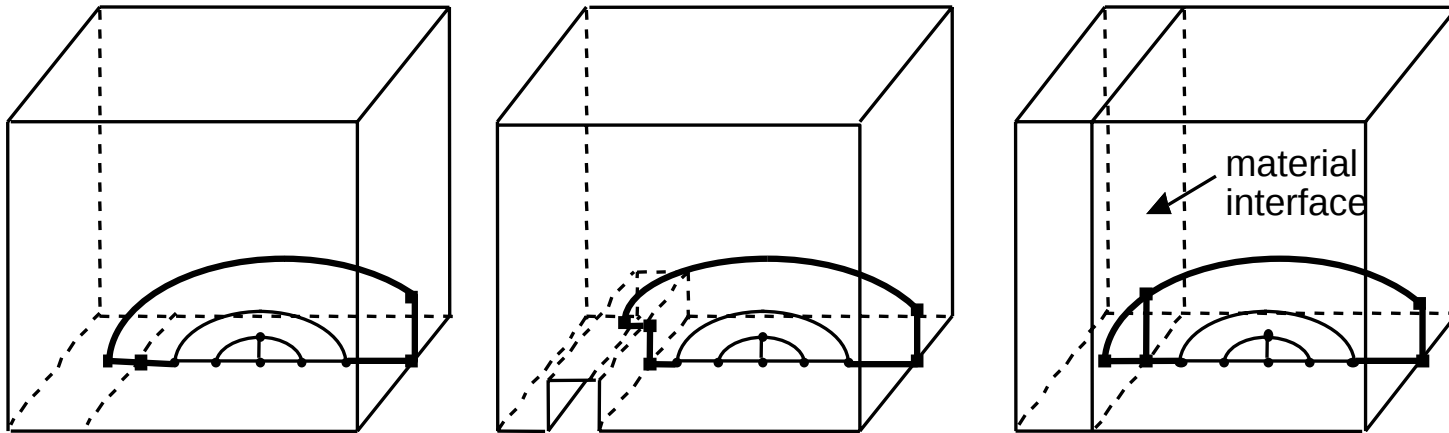
If the points
fall outside of
the region,



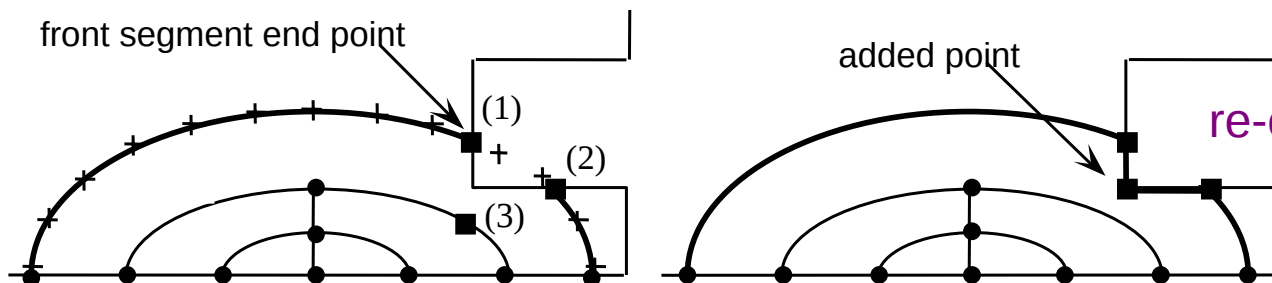
The collection
of edges must
be turned into a
collection of
faces that are
then 'torn'.



Crack Propagation



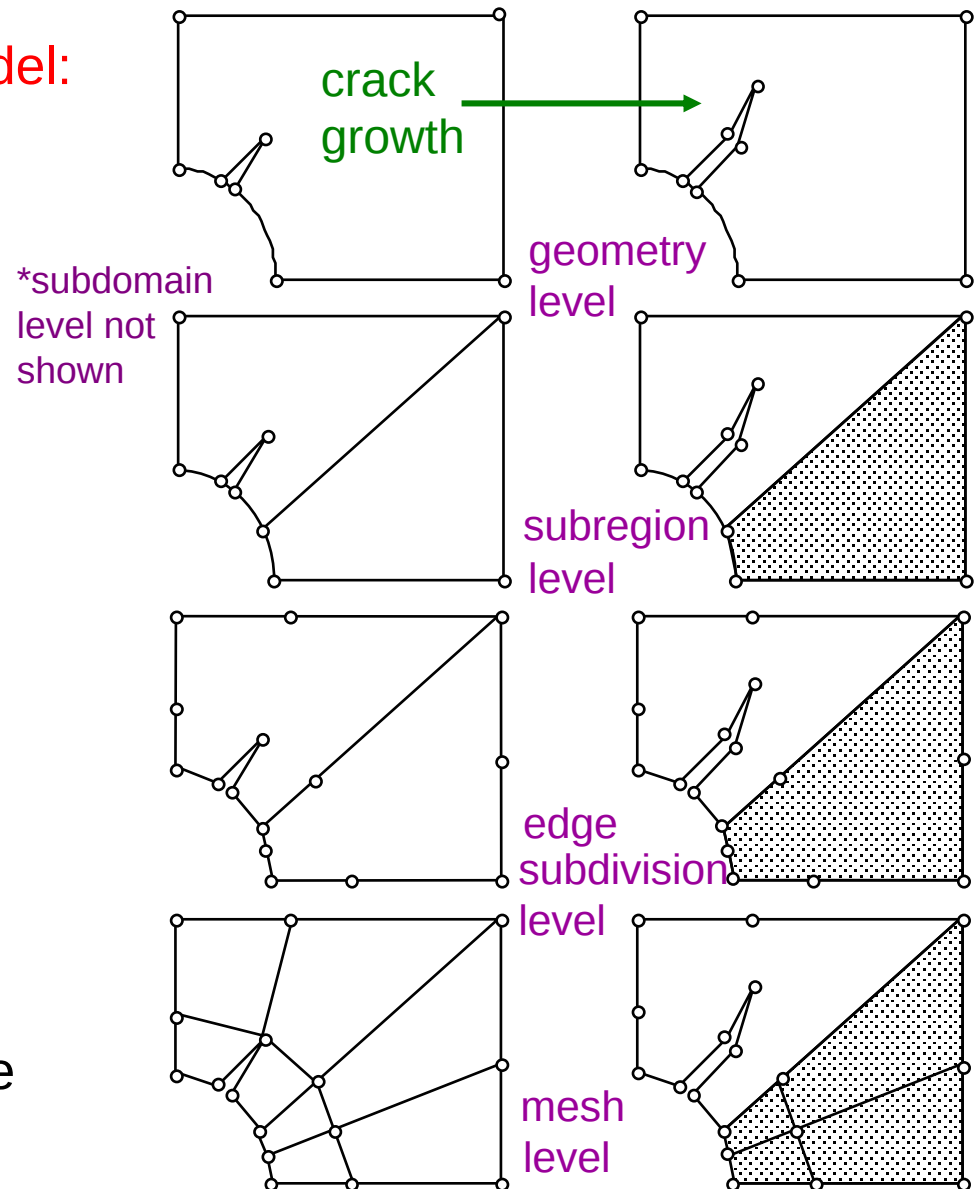
Propagation in a more complex geometry, such as through a material interface or around a re-entrant corner requires careful tracking and manipulation of both geometry and topology.



Crack Propagation

FRANC3D has 5 levels of the model:

- all five levels are automatically updated in response to predicted crack growth
- crack growth occurs at the geometry level first, but all lower levels are constrained by the levels above.
- remeshing is localized to the crack region
- local remeshing near the crack simplifies mapping of information from the previous equilibrium state



Boundary Conditions

Model boundary conditions: rotational and linear acceleration, nodal temperatures

Surface boundary conditions: displacement and pressure
uniform or arbitrary distributions

Edge boundary conditions: displacement and force
uniform or arbitrary distributions

Point boundary conditions: displacement and force

Arbitrary distributions
applied using MRPs
(Mesh RePresentation)

Coupled Sets: cyclic symmetry

Contact Surfaces: master/slave

BOUNDARY CONDITIONS FOR A FACE

BC Name: face_bc_set_1 Layer: 1

Coord Sys: default global sys ☐ global Cartesian ☐ surface local ☐ user defined

Load Case: default load case MRP BC: no MRP

x (global or user Cartesian [green]) or n (surface local [red])

☐ displacement ☐ traction 0 ☐ rotation ☐ moment 0

y (global or user Cartesian [blue]) or u (surface local [green])

☐ displacement ☐ traction 0 ☐ rotation ☐ moment 0

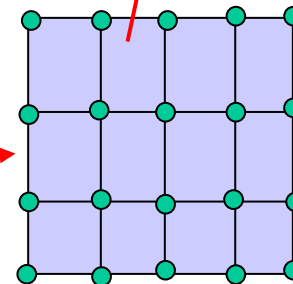
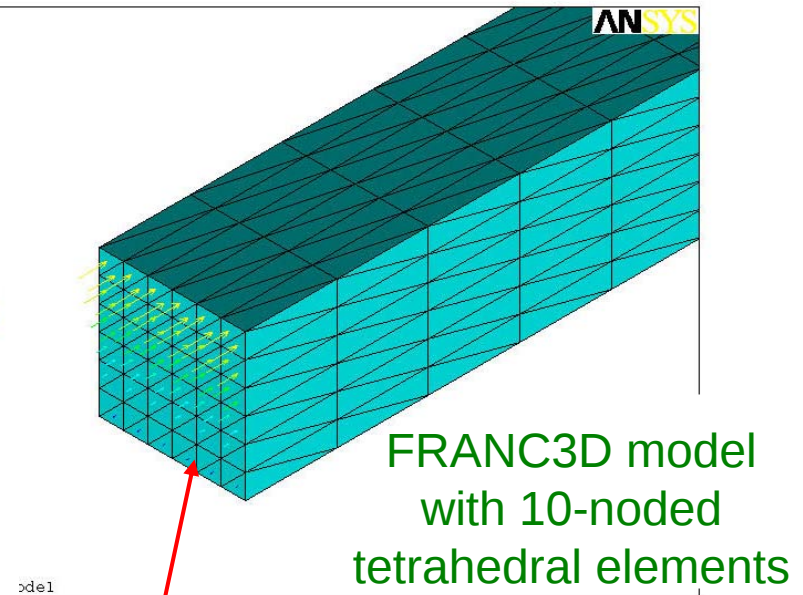
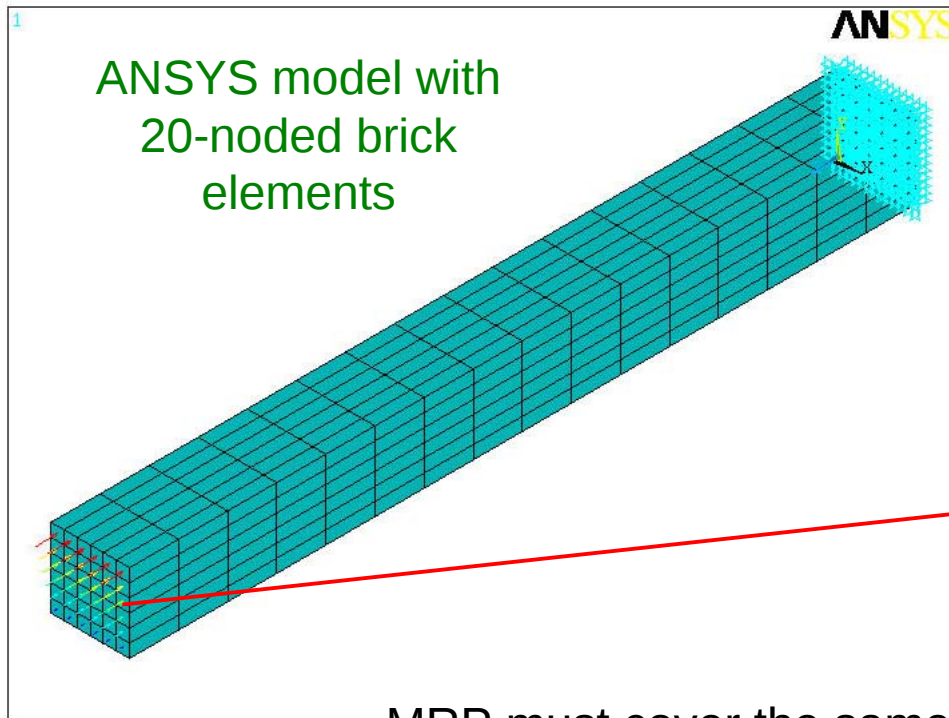
z (global or user Cartesian [red]) or v (surface local [blue])

☐ displacement ☐ traction 0 ☐ rotation ☐ moment 0

Accept Prev Layer Next Layer Prev Load Case Next Load Case Cancel

MRP boundary conditions

linear pressure distribution
on a cantilever beam

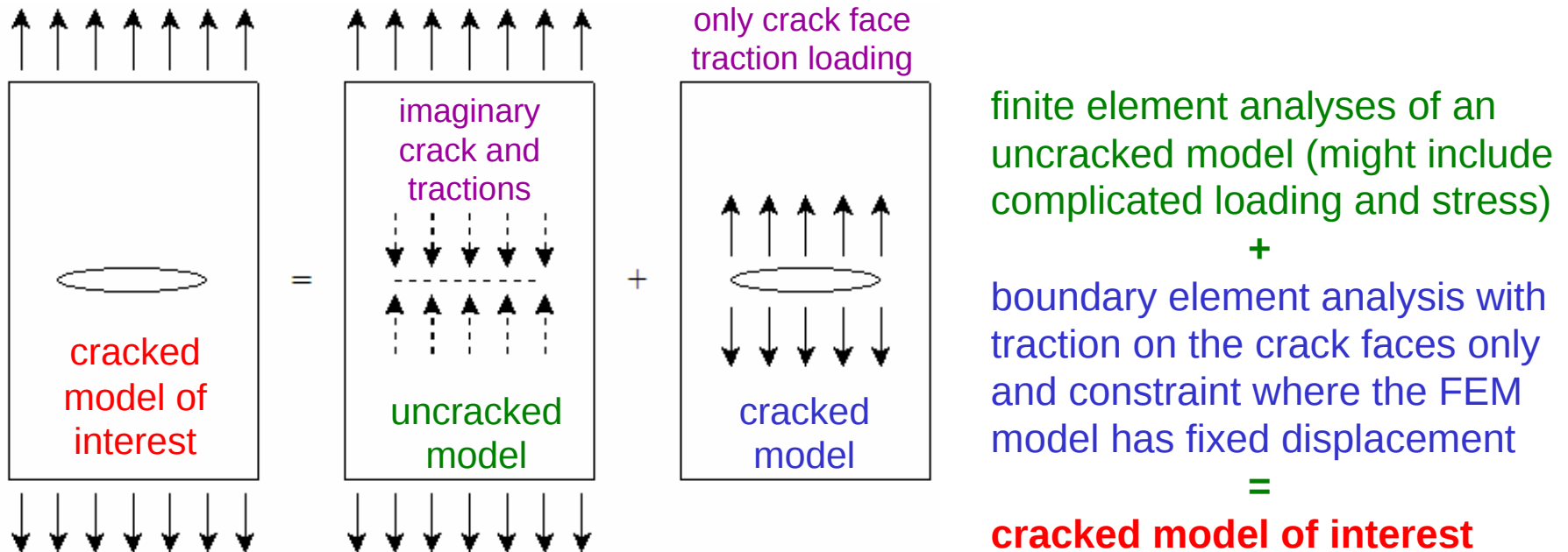


MRP:
12 elements
20 nodes
20 nodal pressures

MRP must cover the same geometric location
as the model surface where the MRP is to be
applied but the mesh does not have to match.

Superposition Based BC's

linear superposition [see Broek 1986]



The magnitudes of the tractions applied to the crack faces are equal in magnitude and opposite in direction to those holding an imaginary crack closed in the finite element analysis and are determined from the stresses from the finite element analysis.

All results -- stresses, strains, displacements, and stress-intensity factors -- for the model of interest, model (a), are the algebraic sum of the results of models (b) and (c). In the case of stress-intensity factors, $K_a = K_b + K_c$, but since K_b is equal to zero, $K_a = K_c$.

Meshing & Discretization

MESH SURFACES
Element Type
Diagonal Option
Bi-linear Mapping
Bi-linear Collapsed
Transition Mapping
Tri-linear Mapping
Arbitrary Region
Automatic
Copy Mesh
Construction
Clear Mesh
Highlight UnMeshed Faces
return

standard
mapped
meshing
algorithms

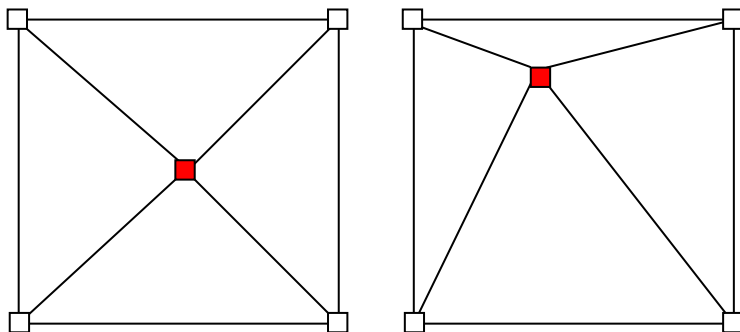
parameters control mesh density

set meshing parameters
automatically generate internal points
auto + user-specified internal points
only user-specified internal points
no internal points
Cancel

ARBITRARY REGION MESH GENERATION	
☐ all quadrilaterals	☐ all triangles
Quadtree Parameters For Internal Nodes	
refinement factor (mesh transitioning)	1.4
boundary factor (nodes near boundaries)	0.9
☐ points at quad corners	
Quadrilateral Element Merging Parameters	
mixed-mesh cutoff	1.5
polygon merge cutoff	2
☐ compute angles in cartesian space	
☐ generate templates at crack tips	
number of half template layers (1, 2, or 3)	1
☐ parametric space	☐ planar space
Accept	Cancel

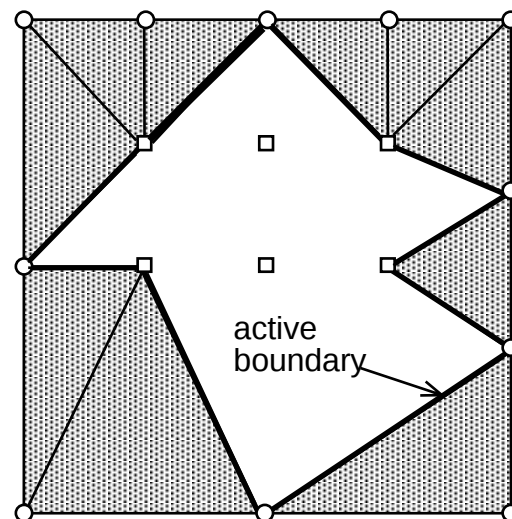
MESH CONSTRUCTION
Add Edge
Delete Edge
Delete Point
Move Point
Check Element
return

control mesh
manually by
moving points

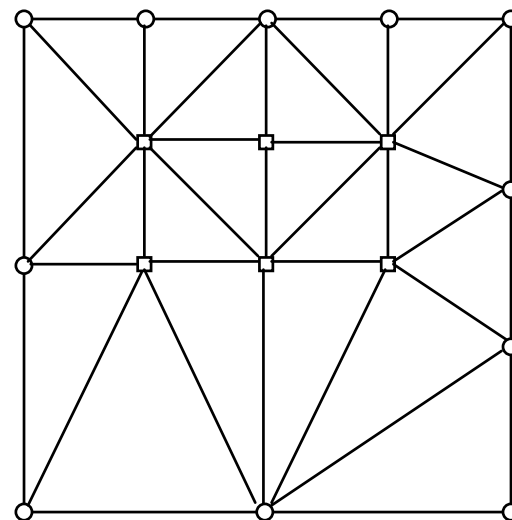


The arbitrary
region mesh can
still be modified
by moving nodes
and by adding or
deleting edges.

advancing front algorithm



final triangular mesh

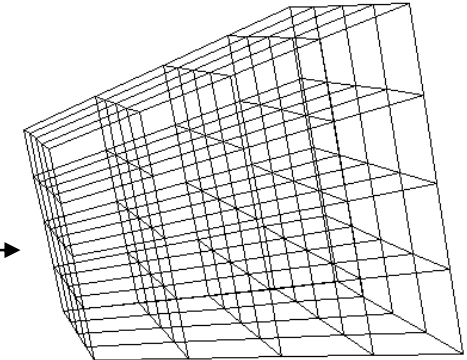
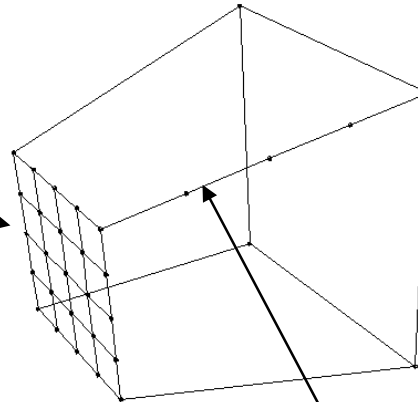


Meshing & Discretization

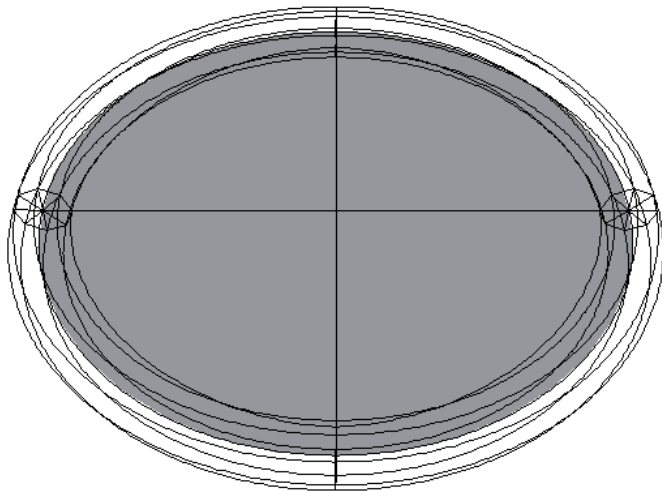
MESH VOLUMES
Tri-linear Mapping
Sweep Meshing
Tet/Pyr Mesh
Define Single Element
Split Brick into Wedges
Automatic
Clear Mesh
Hilight UnMeshed Regions
return

- sweep bricks or wedges depending on source face mesh

source
face
mesh



swept brick mesh



internal penny-shape crack
with crack front subvolume
(subvolume can be swept)

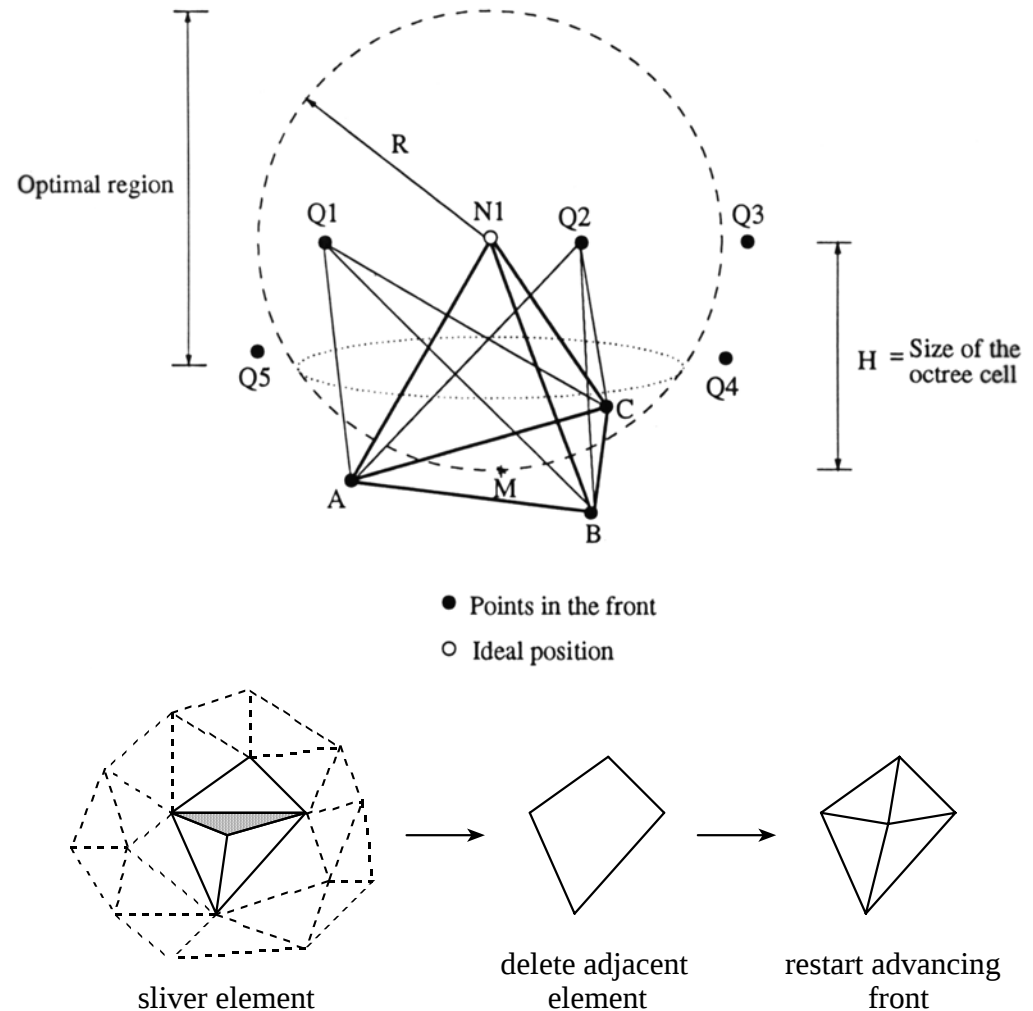
The mesh around the crack front can be:

- bricks
- wedges (singular)
- tetrahedra
- wedges surrounded by bricks, then pyramids and then tetrahedra

Tetrahedral Volume Meshing

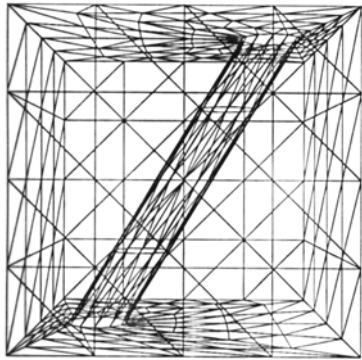
advancing front, unstructured tetrahedral mesh generation

- generate an octree “background mesh” to estimate element size.
- geometry-based advancing front - elements are generated based on ideal shapes.
- topology-based advancing front – all topologically valid elements are generated.
- backtracking to mesh any non-meshable polyhedra.
- edge and face swapping and laplace smoothing for local shape improvement.

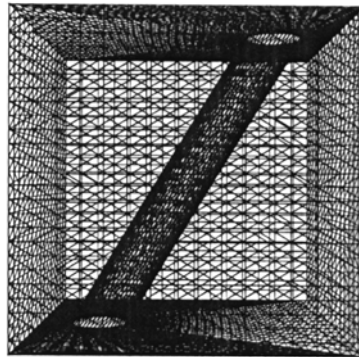


Tetrahedral Volume Meshing

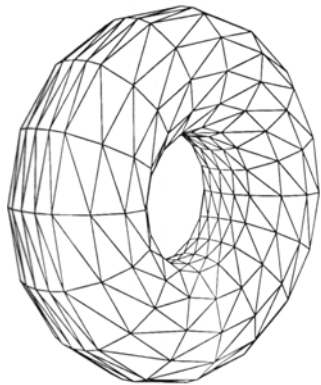
some examples



coarse
and
refined
meshes

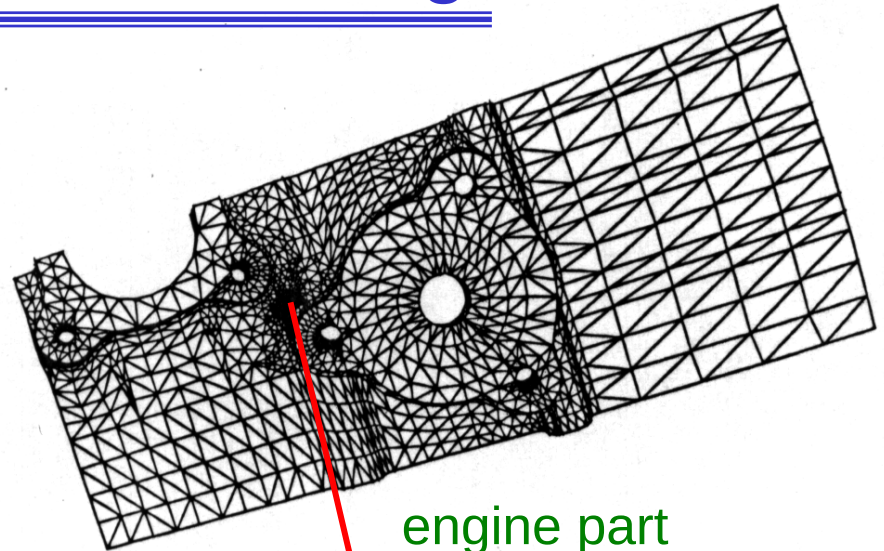
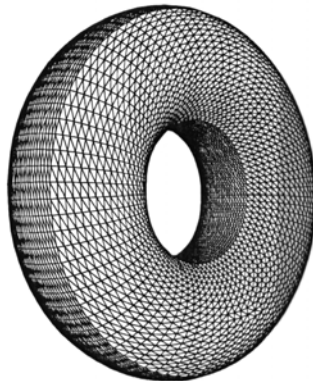


inclined borehole

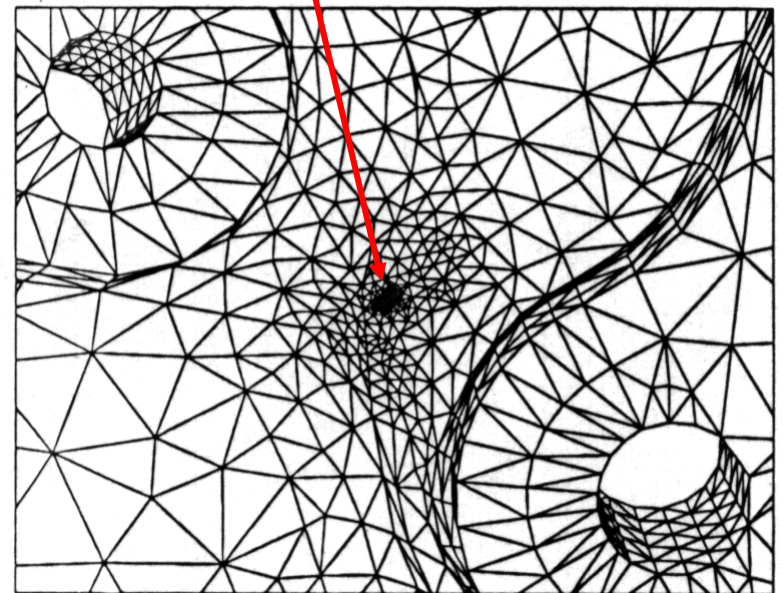


coarse
and
refined
meshes

torus



engine part



OSM Overview

Specifically designed to create B-rep models for FRANC3D:

- closed solid 3D models
- curved shells and 2D plate models

B-rep solid model for FRANC3D requires:

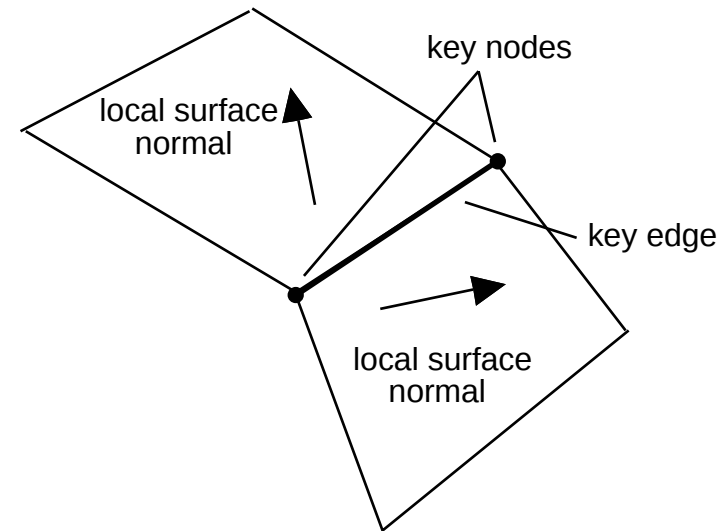
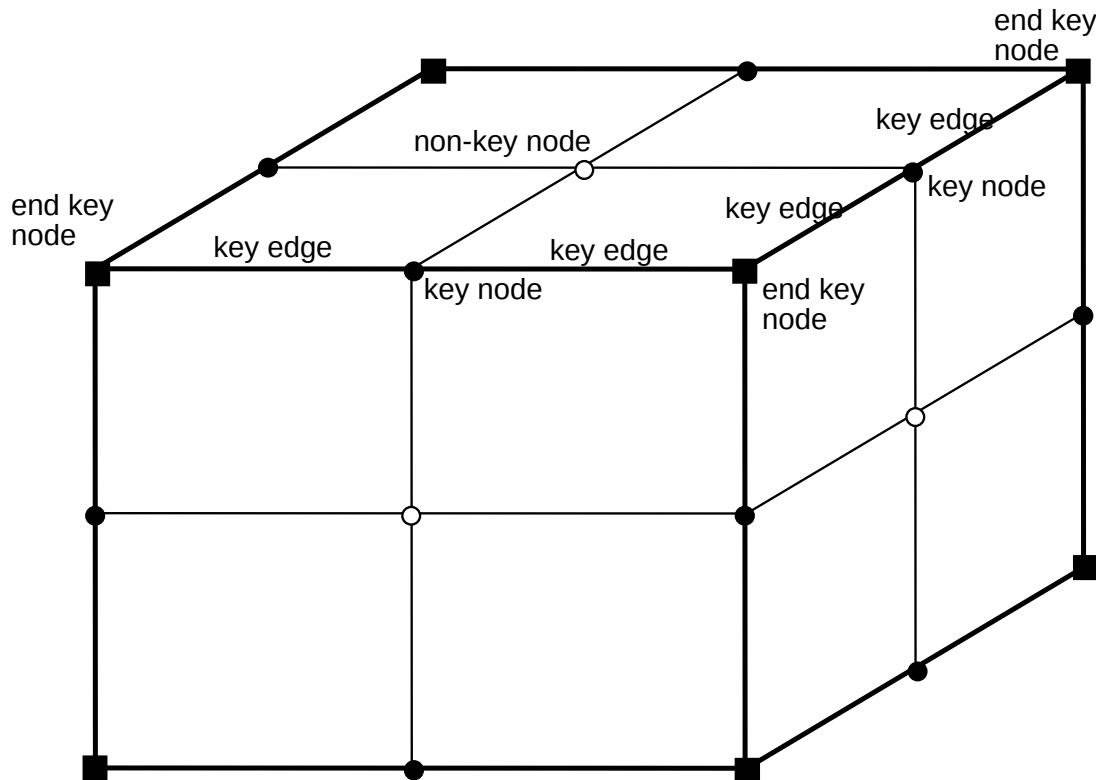
- watertight geometry
- exterior surface normals pointing outwards
- interior surfaces defined as 'interior'
- plates and curved shell models are not 'closed'

OSM capabilities:

- creates lines, arcs, spline curves
- creates triangular Bezier or bi-cubic b-spline surfaces
- planar surfaces are supported but cannot be created manually
- extrude, translate, rotate, mirror, cut & paste
- copy objects between multiple windows
- finite element model translation and conversion
- ANSYS generated IGES file conversion

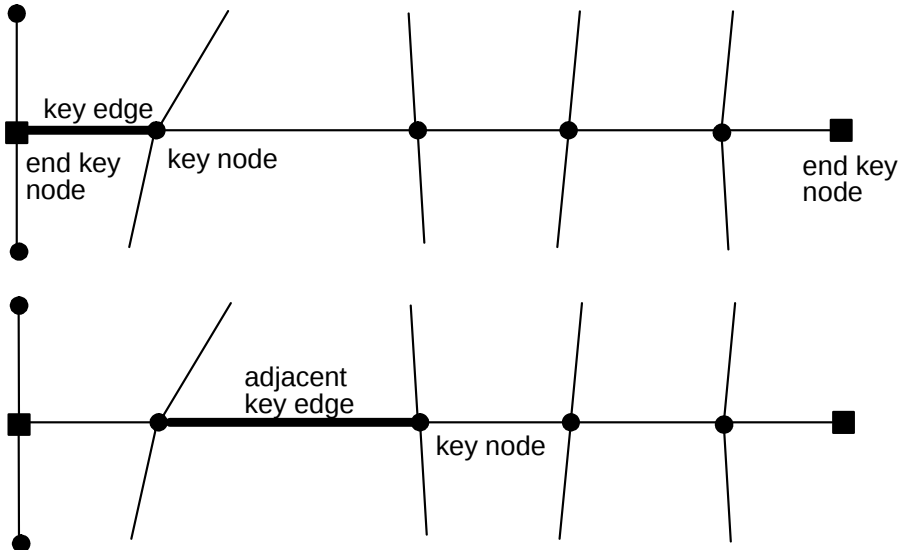
OSM: FEM Conversion

- start with FE data file that contains node and element information
- extract the surface facets with their edges and nodes (vertices)
- eliminate all interior features:
facets used by two elements are not surface facets and can be removed



identify key nodes and edges
based on angle changes

OSM: FEM Conversion

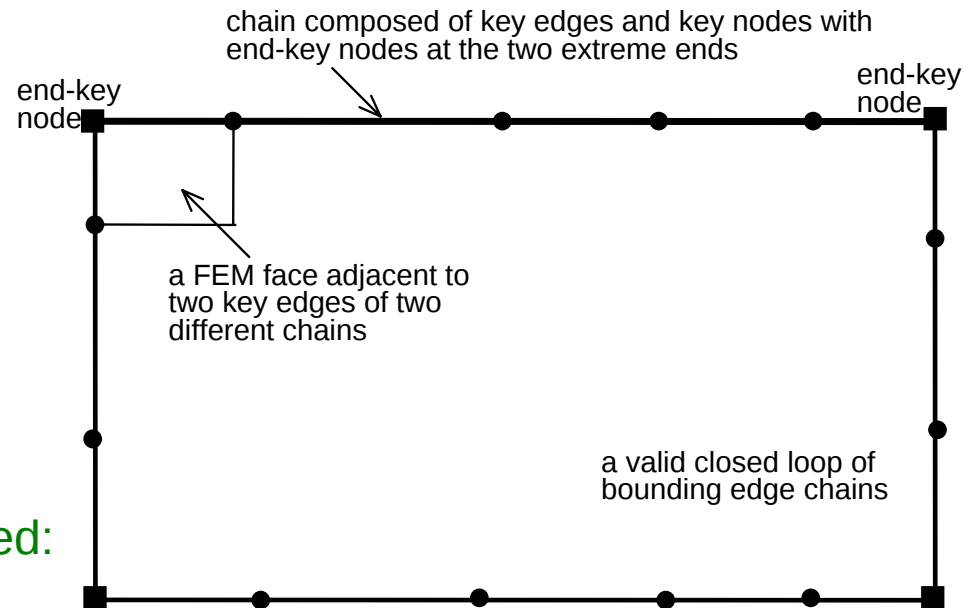


- compose chains of key edges between end key nodes

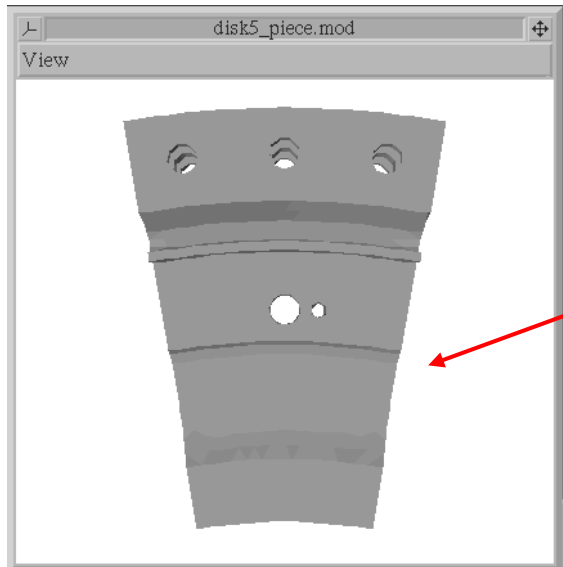
- form loops from the chains
- form faces from the loops

A limitation that has been partly resolved:

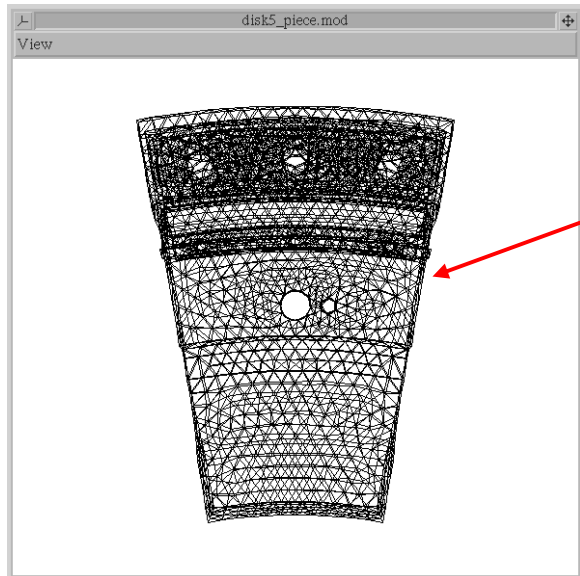
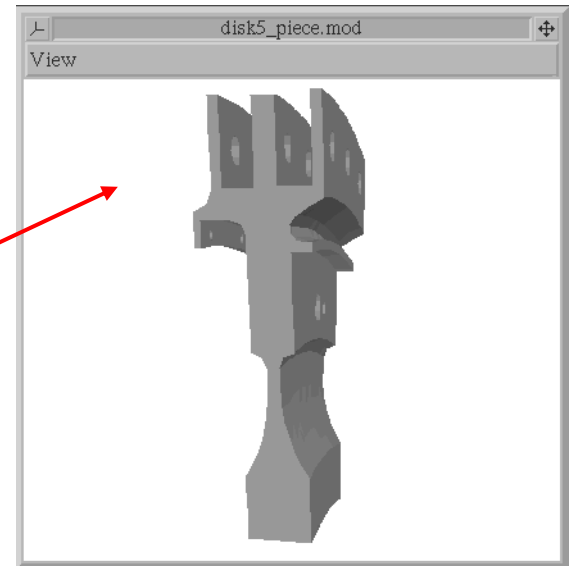
- faces must be 3 or 4-sided



OSM: FEM Conversion

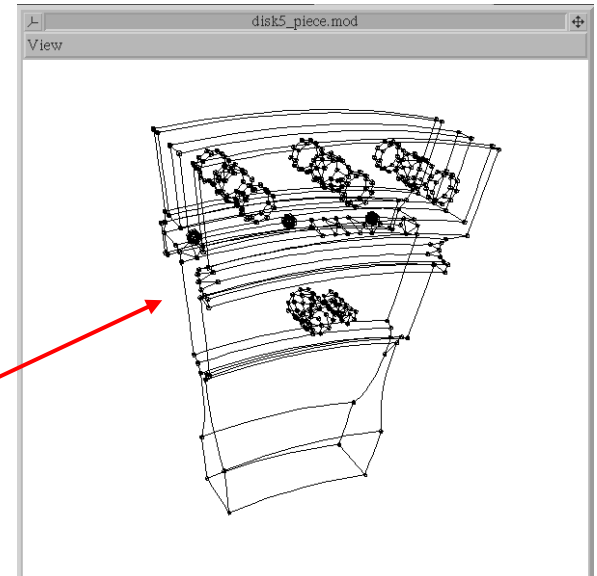


original
solid
model
geometry

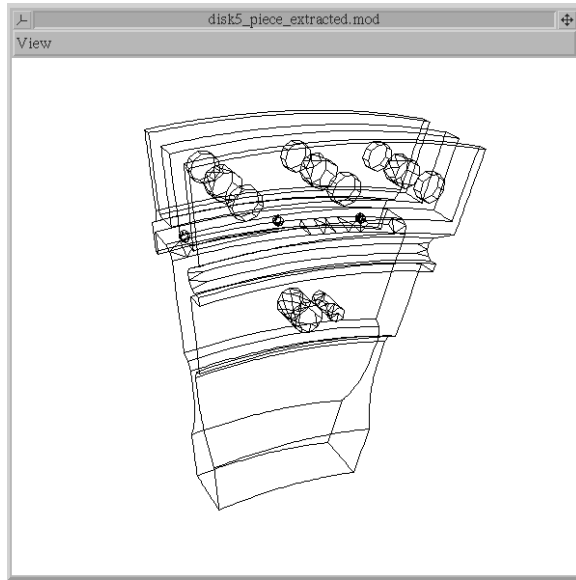


original
mesh

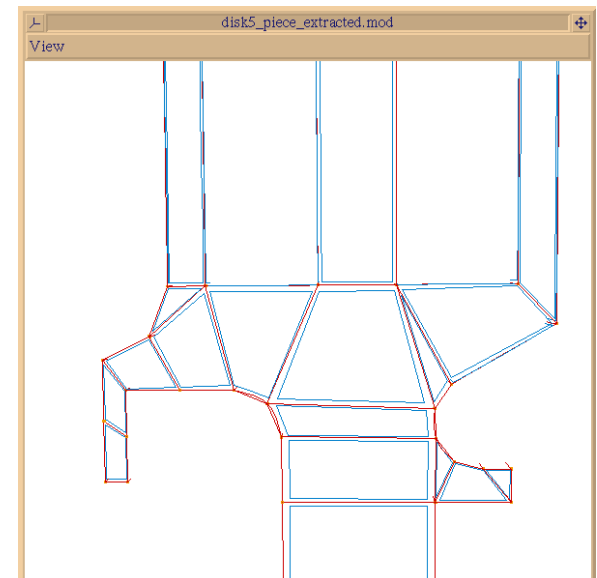
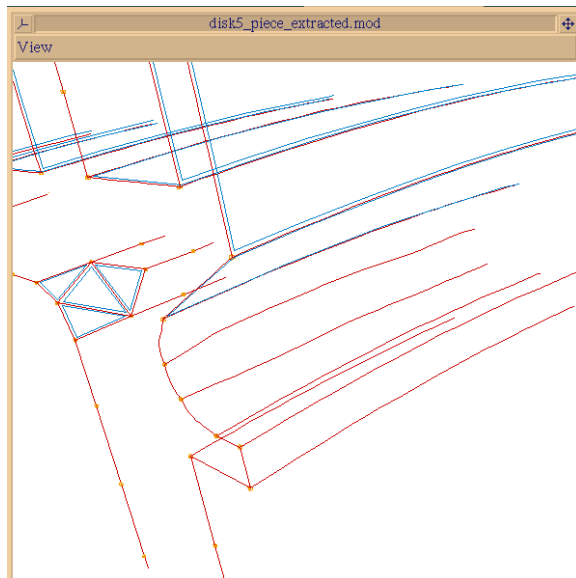
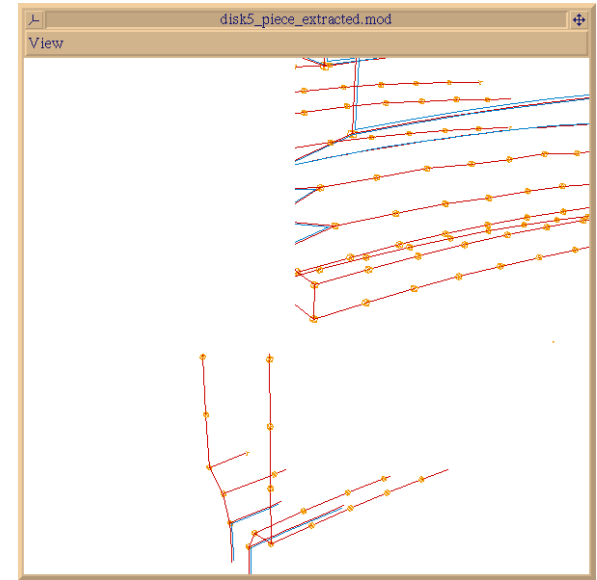
extracted
geometry



OSM: FEM Conversion



Models usually require that the user manually complete the process of forming a closed B-rep solid model. Problems arise if there are contact surfaces or other features where the original mesh facets do not match exactly. Problems also arise for surfaces that consist of more than four 'geometric' edges.



Description of Files

OSM files:

- *.mod a formatted text file - OSM restart file containing surface, edge, and vertex geometry information.
- *.osm a formatted binary file based on XDR routines for cross platform portability - OSM restart file containing surface, edge, and vertex geometry information.

FRANC3D files:

- *.dat a formatted text file - FRANC3D input file containing surface patch geometry information.
- *.fys an unformatted binary file - FRANC3D restart file containing all of the FRANC3D model information.
- *.afys a formatted text file - FRANC3D restart file containing all of the FRANC3D model information. Although this file is a formatted text file, the file should not be edited manually.

Description of Files (continued)

FRANC3D files (continued):

- *.frt a formatted text file containing crack front geometric point coordinates.
- *.mrp a formatted text file containing finite element mesh information and boundary condition data. This file is used to specify arbitrary loading conditions. NOTE: this file is generated by OSM and replaces the .conn and .fstr files. It can consist of 2D or 3D finite element information. It is currently generated from ANSYS .cdb files.
- *.conn (obsolete for Version 2.4) a text file containing finite element mesh information in FRANC3D generic format consisting of nodal coordinates and element connectivity. This file can be generated by OSM when translating FEM data from ANSYS .cdb files for example.
- *.fstr (obsolete for Version 2.4) a text file containing finite element nodal stress information. This file along with the .conn file is used by FRANC3D when applying crack face tractions based on FEM results.

Description of Files (continued)

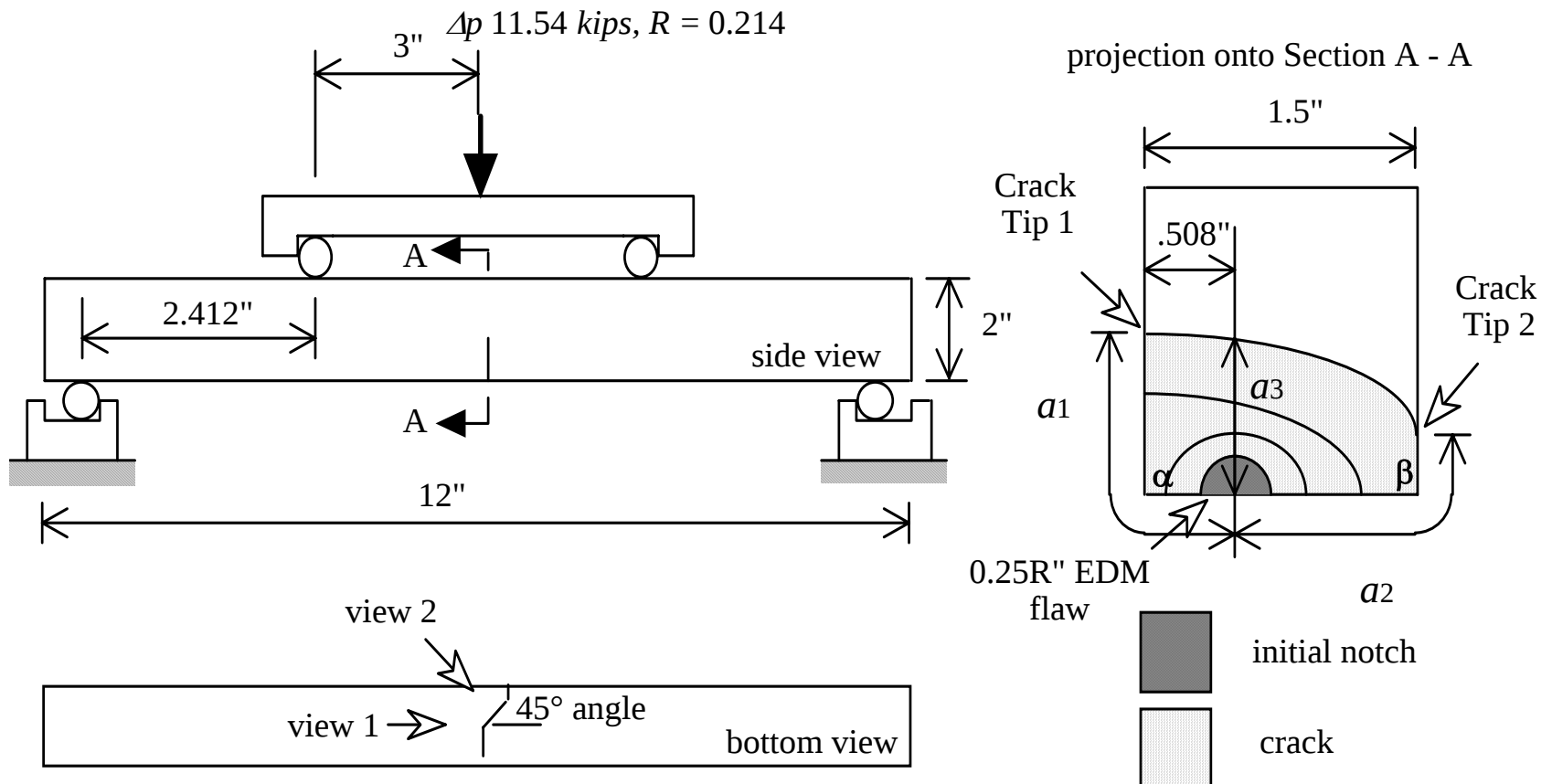
BES files:

- *.bes a formatted text file - BES input file containing nodal coordinates, element connectivity, boundary conditions, and material properties.
- coef.dat an unformatted binary file containing the BES coefficient matrix. This file is created when running the out-of-core version of the BES solver and the file should be deleted after BES is finished.
- *.besout a formatted text file - BES output file containing computed nodal displacements and tractions.
- *.con a formatted text file - BES output file containing computed element stresses.

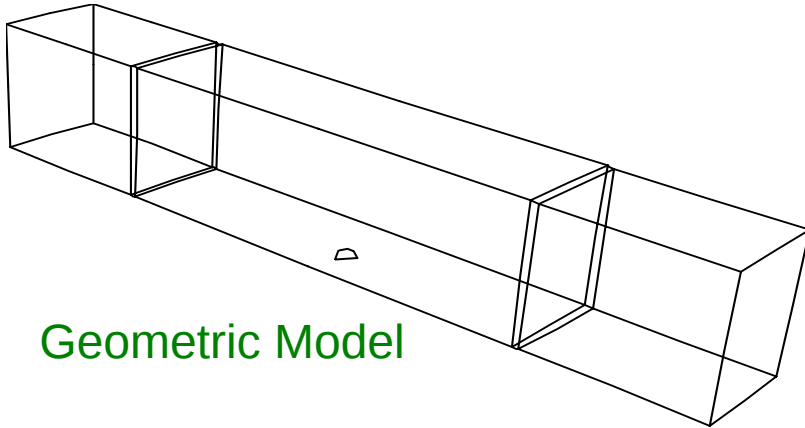
ANSYS files:

- *.cdb a formatted text file of the model data, including nodes, elements, etc
- *.igs an IGES formatted text file describing the model geometry
- *.dsp listing of nodal displacements
- *.str listing of nodal stress components
- *.tmp listing of nodal temperatures
- *.eps listing of nodal plastic strain

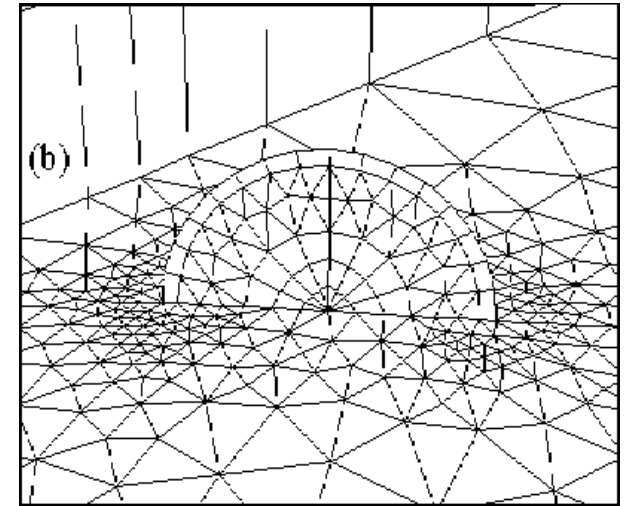
2219-T851 aluminum beam laboratory test specimen in four-point bending



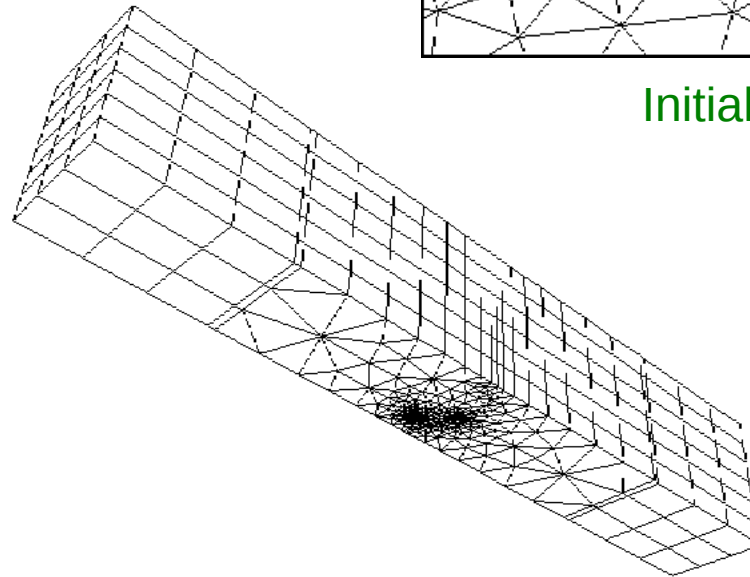
Initial Boundary Element Mesh



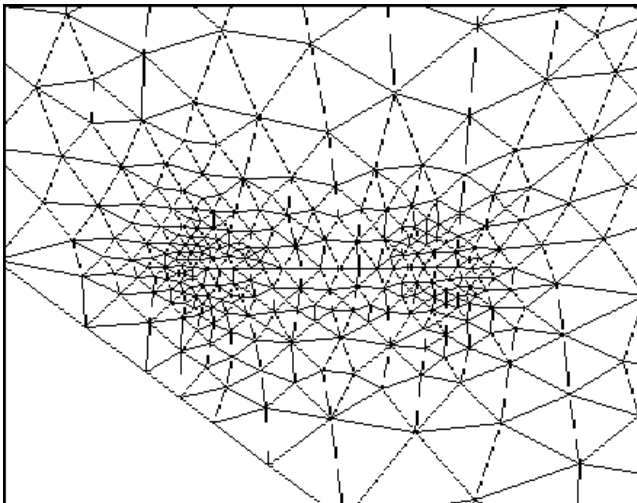
Geometric Model



Initial Flaw

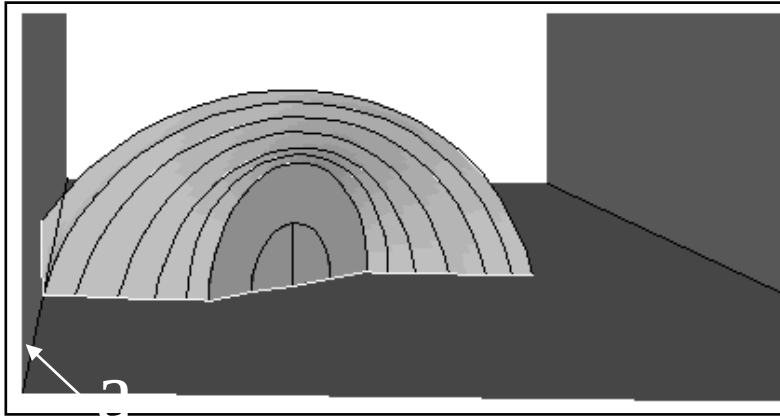


Full Beam



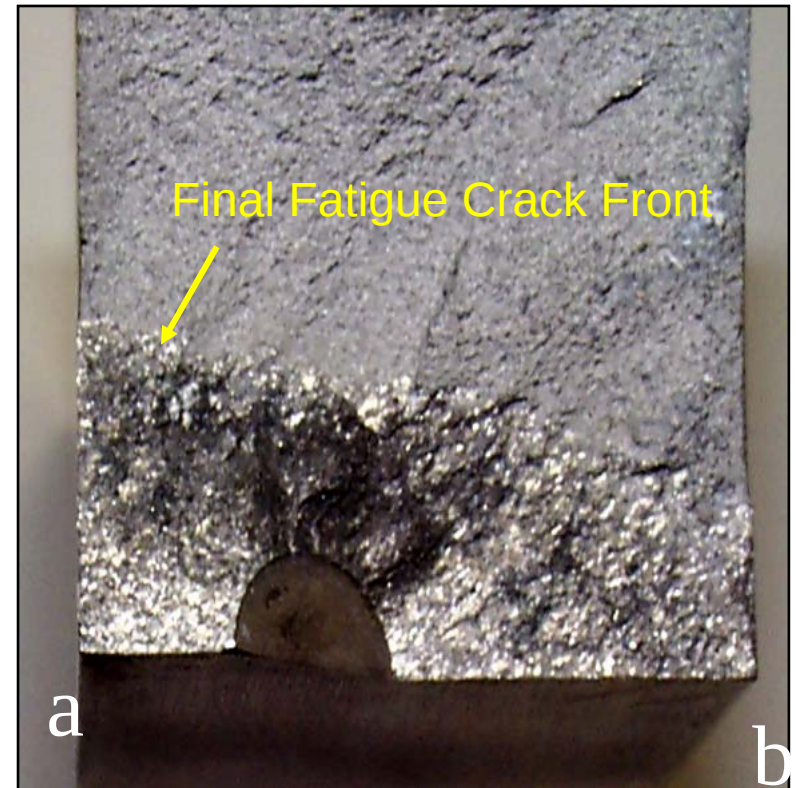
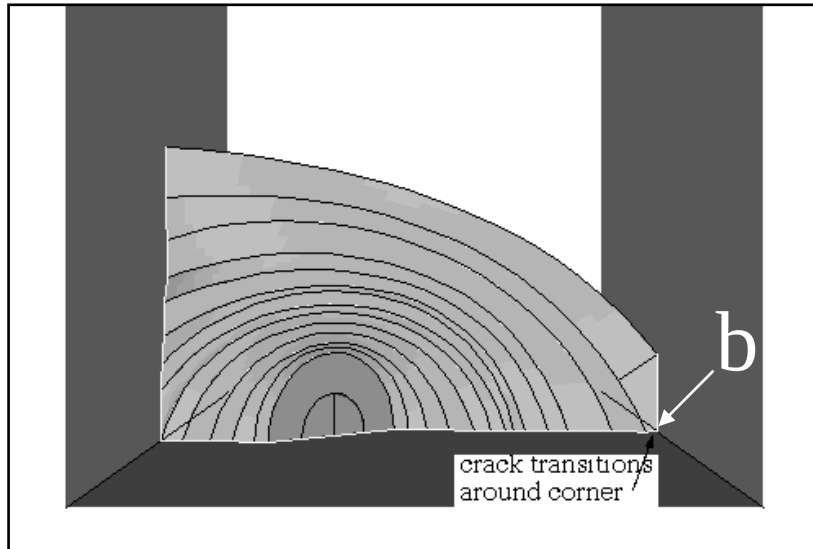
Flaw Mouth

Predicted and Observed Crack Fronts



Predicted Transition into Corner "a"

Predicted Transition into Corner "b"



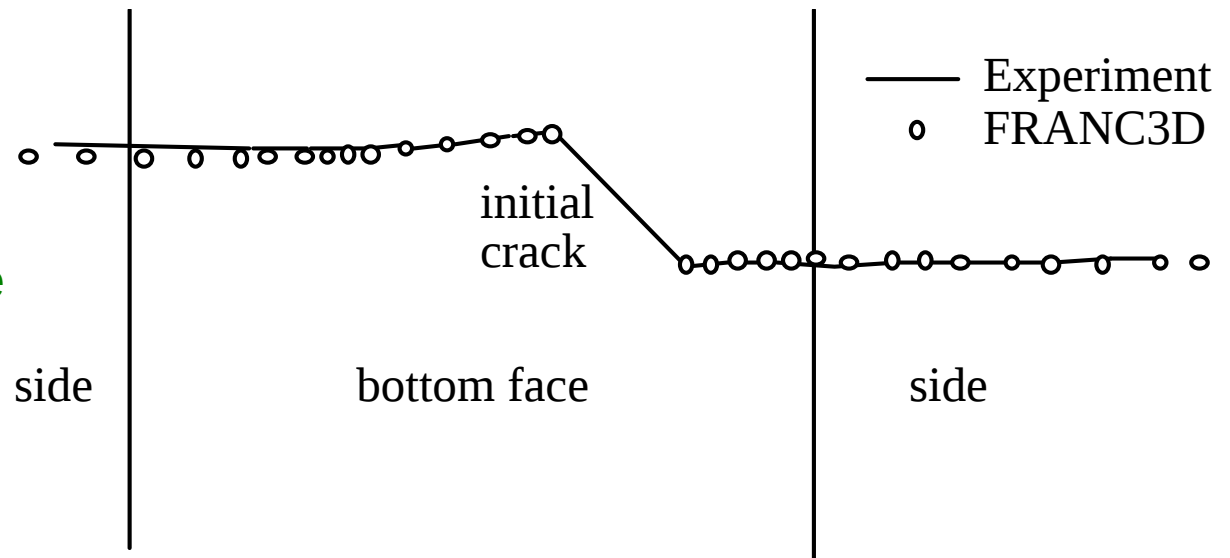
Observed Fatigue Crack Shape

Final Predicted Crack Shape

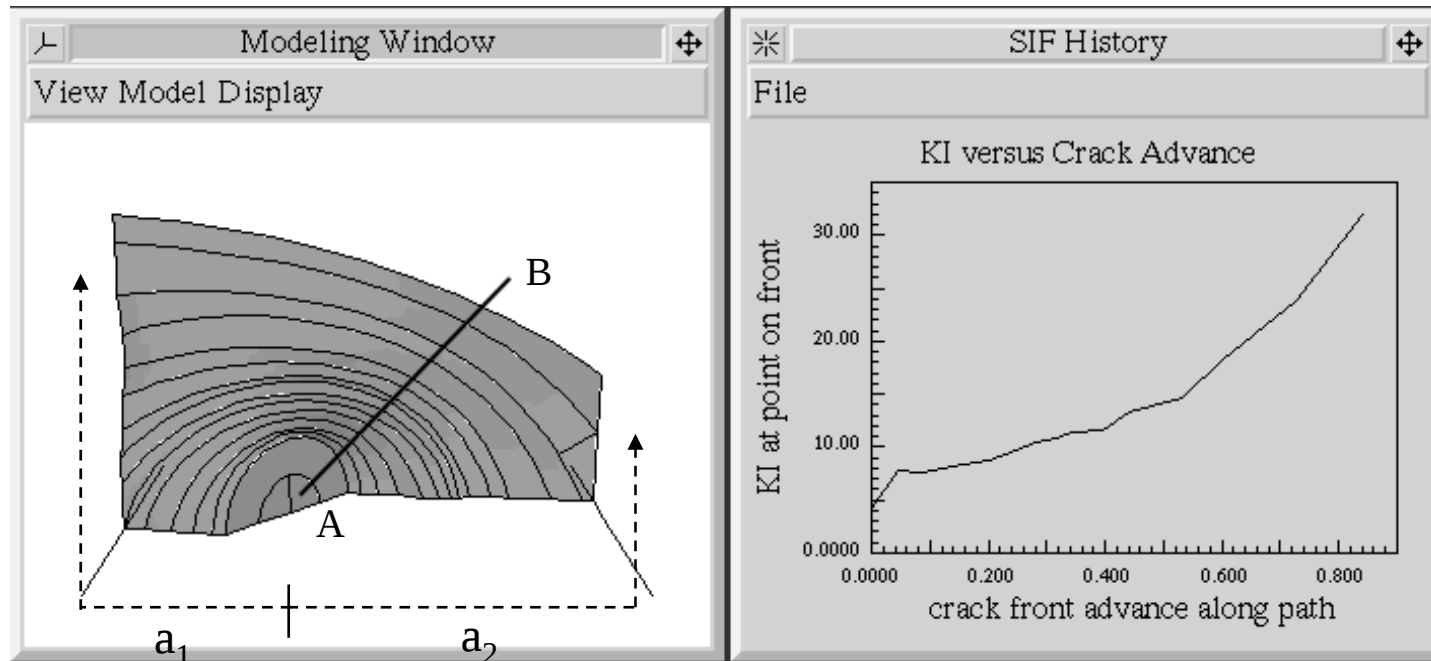


Deformed solid

Comparison of computed
and observed crack trace
on the surface



Computed SIF History and Comparison to Observations



Event	Observed	FRANC3D	% Difference
a-Corner (cycles)	106,800	140,000	32
b-Corner (cycles)	171,000	170,000	-0.5
Last Front (cycles)	175,000	190,000	8.5
a_1 (in.)	1.26	1.42	12.7
a_2 (in.)	1.38	1.34	-2.8

Summary

- We can translate the ANSYS model from either the mesh information (.cdb file) or from the solid model geometry (.iges file).
- Based on uncracked model stress results, we can predict the location of crack initiation.
- Model boundary conditions are mapped from the uncracked model to the cracked model.
- The orientation of the maximum principal stress provides the plane for the initial crack.
- The orientation can be input into the FRANC3D library flaw dialog box or can be “user defined”.
- Subsequent crack trajectory is predicted within FRANC3D based on the maximum hoop stress criterion.
- The resulting output can be a history of SIF versus crack size, which can then be input into a life analysis tool.