



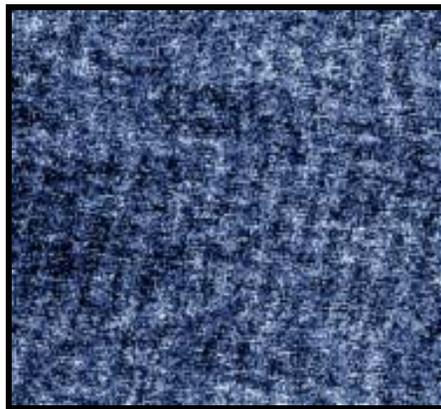
Practical STEM: More than Z Contrast



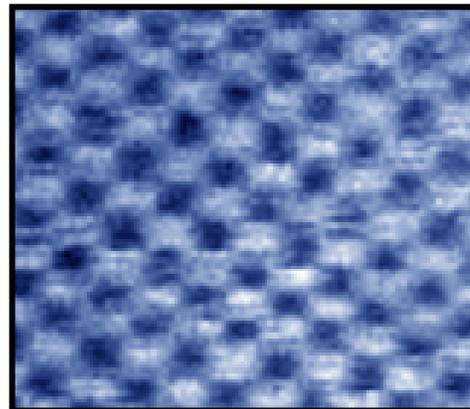
David Muller

Applied Physics, Cornell University

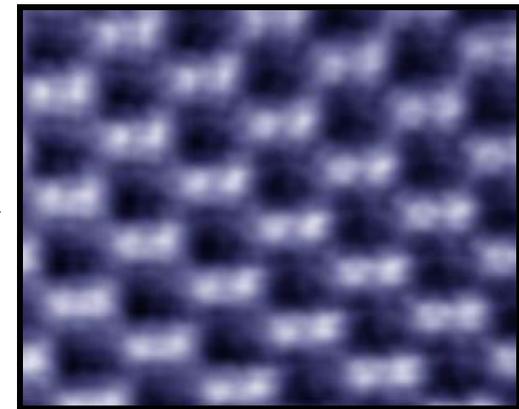
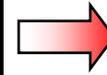
- Thickness dependence of images
- Common mistakes
- Alignment Tricks



3 weeks



6 months



1 year



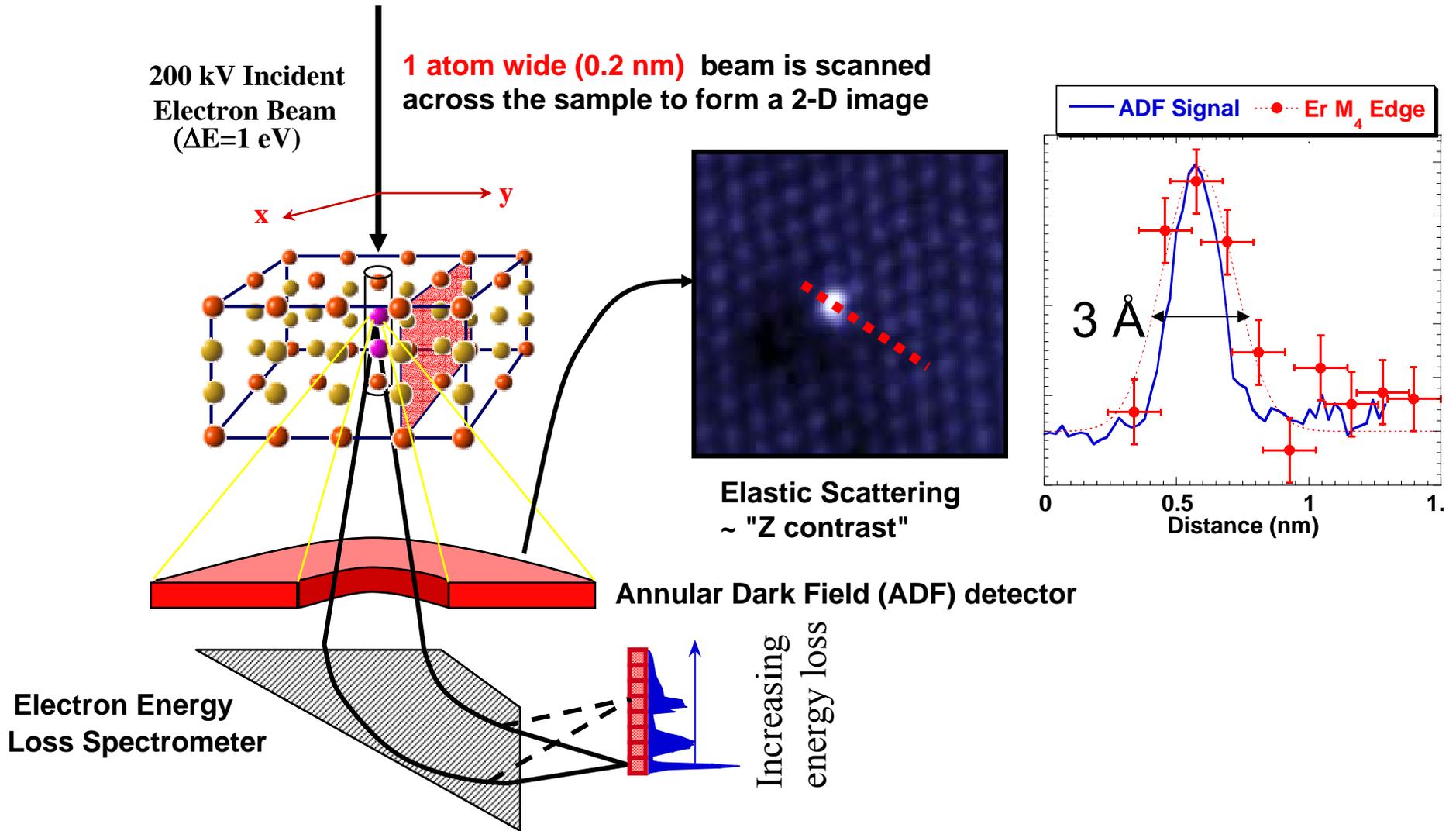
Acknowledgements

*Matt Weyland, Zhiheng Yu,
Peter Ercius, Lena Fitting, Earl Kirkland*
Applied Physics, Cornell University

Paul Voyles
University of Wisconsin, Madison

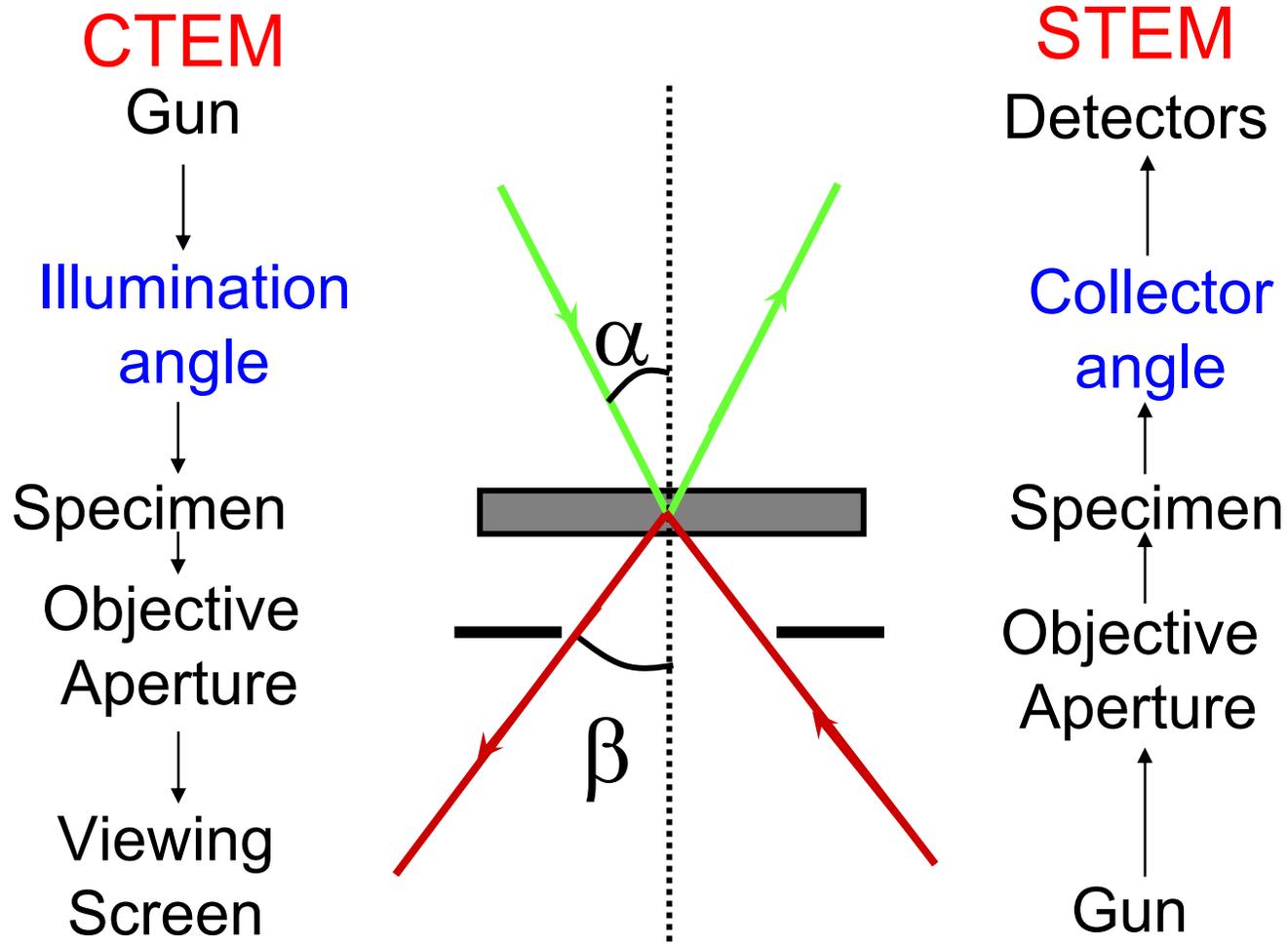
John Grazul, Mick Thomas
Cornell Center for Materials Research

Scanning Transmission Electron Microscopy



Single atom Sensitivity: P. Voyles, D. Muller, J. Grazul, P. Citrin, H. Gossmann, *Nature* **416** 826 (2002)
 U. Kaiser, D. Muller, J. Grazul, M. Kawasaki, *Nature Materials*, **1** 102 (2002)

Reciprocity (or STEM vs. CTEM)



Reciprocity (for zero-loss images):

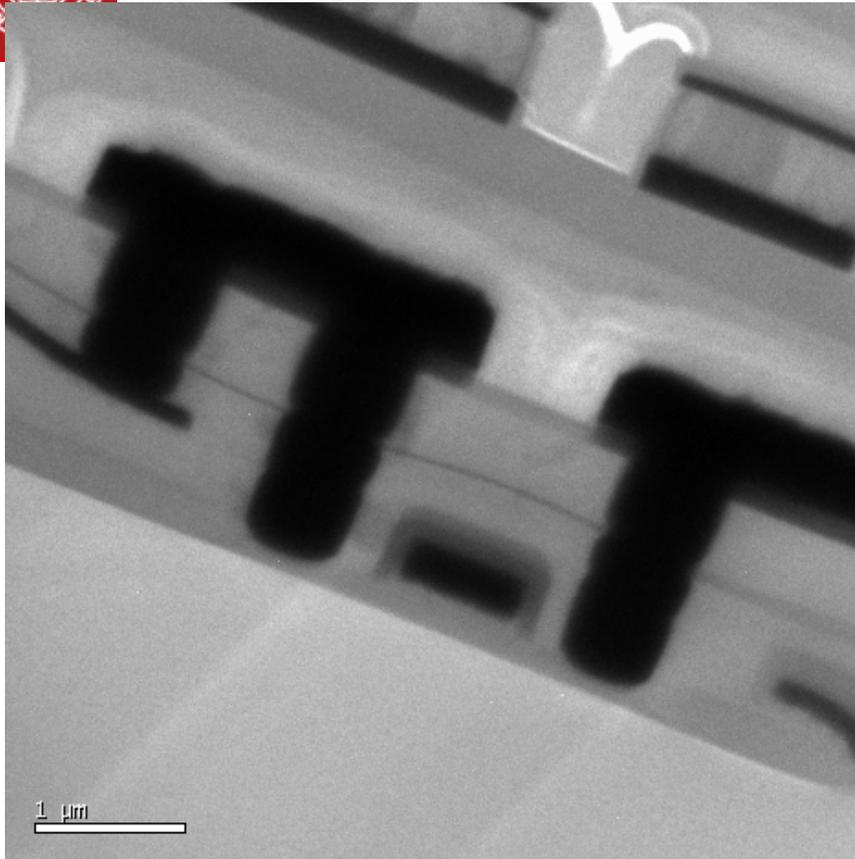
A hollow-cone image in CTEM \longleftrightarrow an annular-dark field image in STEM.

However: In STEM, energy losses in the sample do not contribute to chromatic aberrations (Strong advantage for STEM in thick specimens)

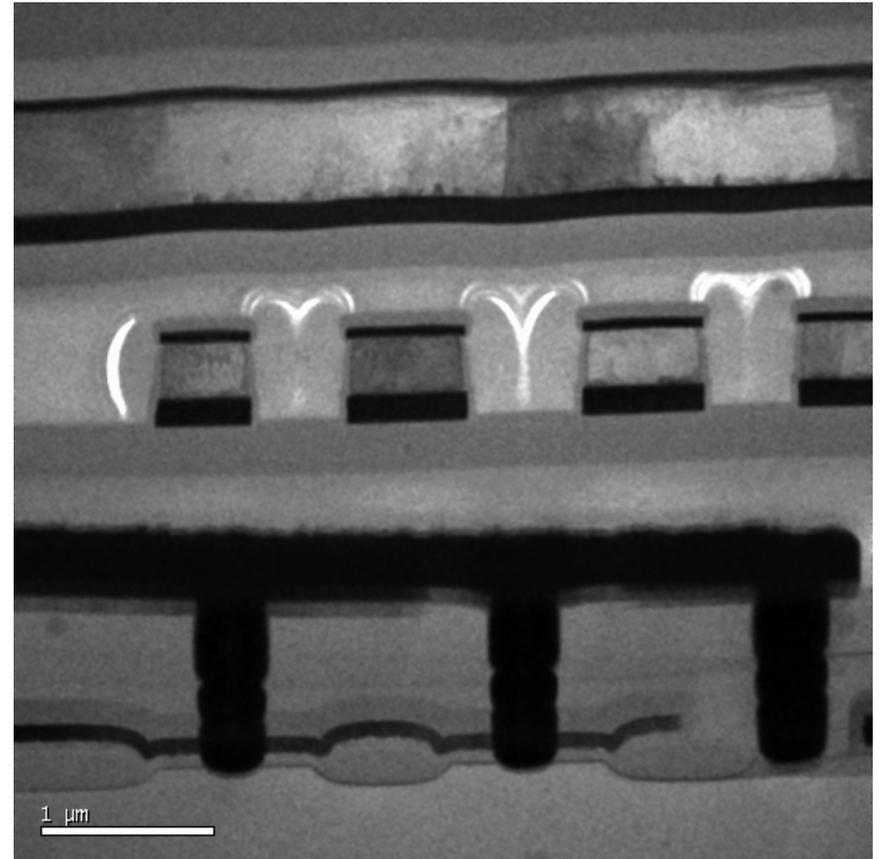
Imaging Thick Samples at 200 kV



BF-TEM



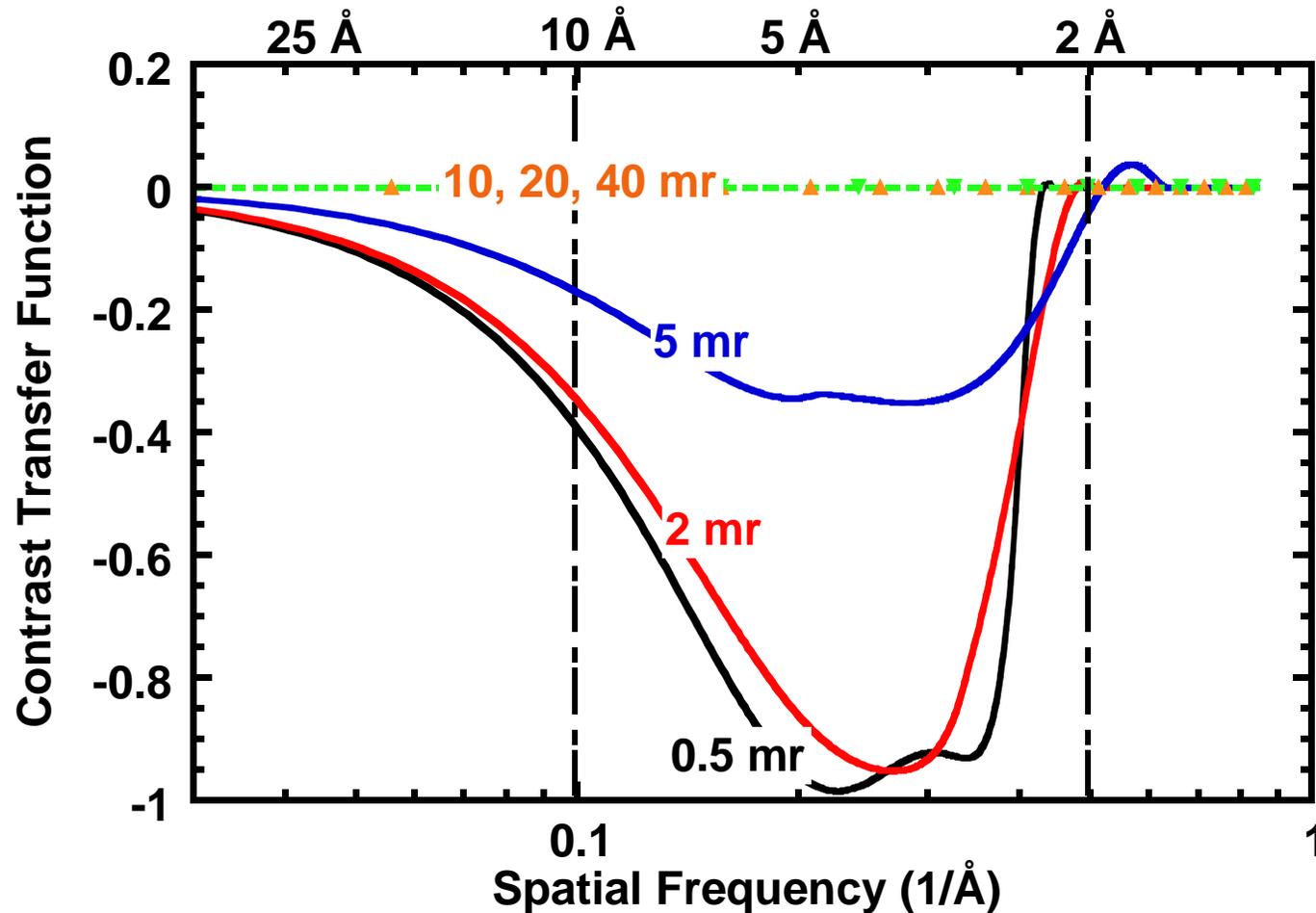
BF-STEM ($\sim 2\text{mr } \theta_c$)



- Less blurring, more contrast in thick samples with STEM
- No Signal in W plugs, diffraction in poly
 → unsuitable for tomography

Phase Contrast for Different Illumination Angles

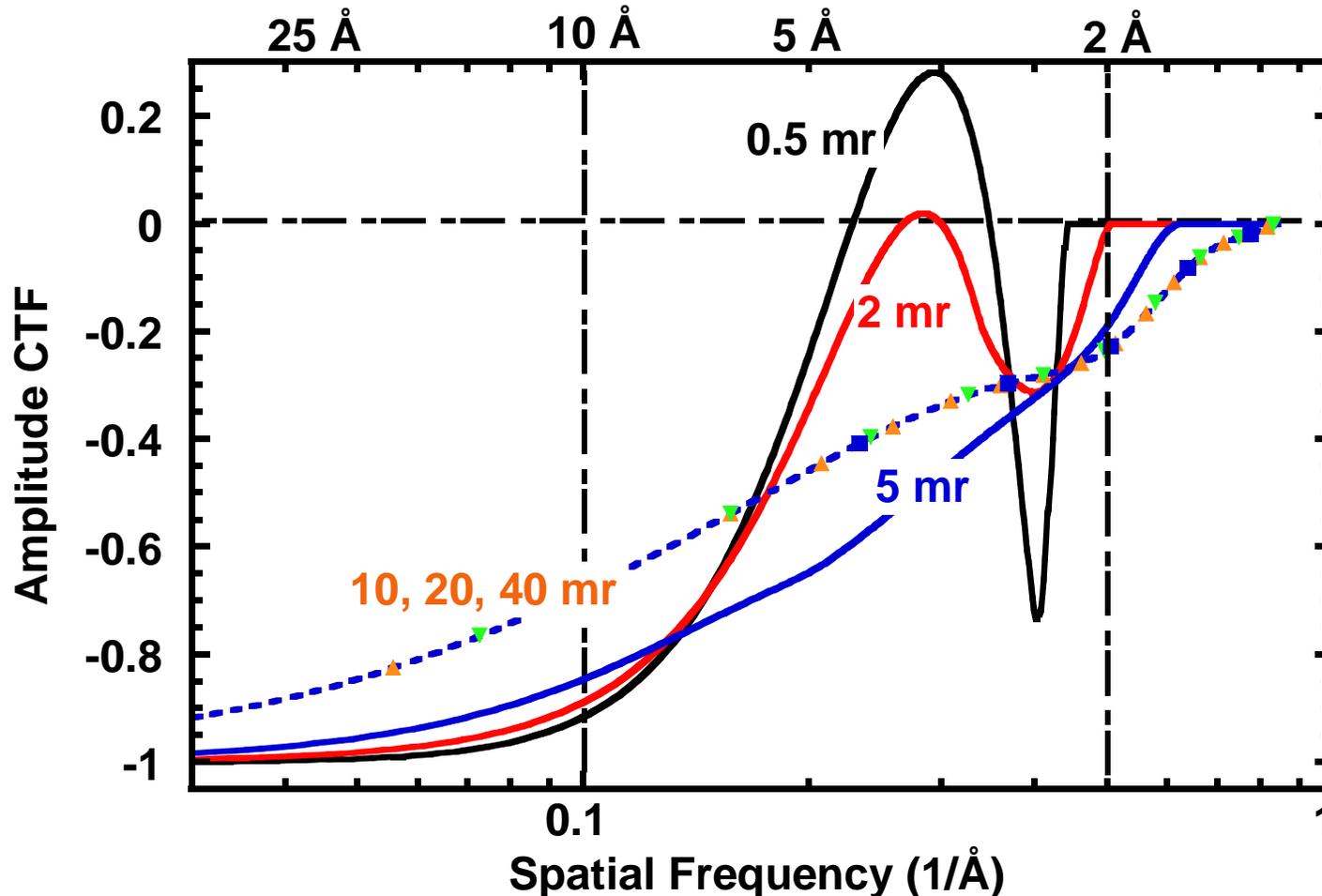
(10.5 mr Objective, $E_0=200\text{kV}$, $C_s=1\text{ mm}$, Scherzer Defocus)



- For distances larger than 1 nm, there is little phase contrast to start with.
- When the illumination angles exceeds the objective aperture, all phase contrast is suppressed!

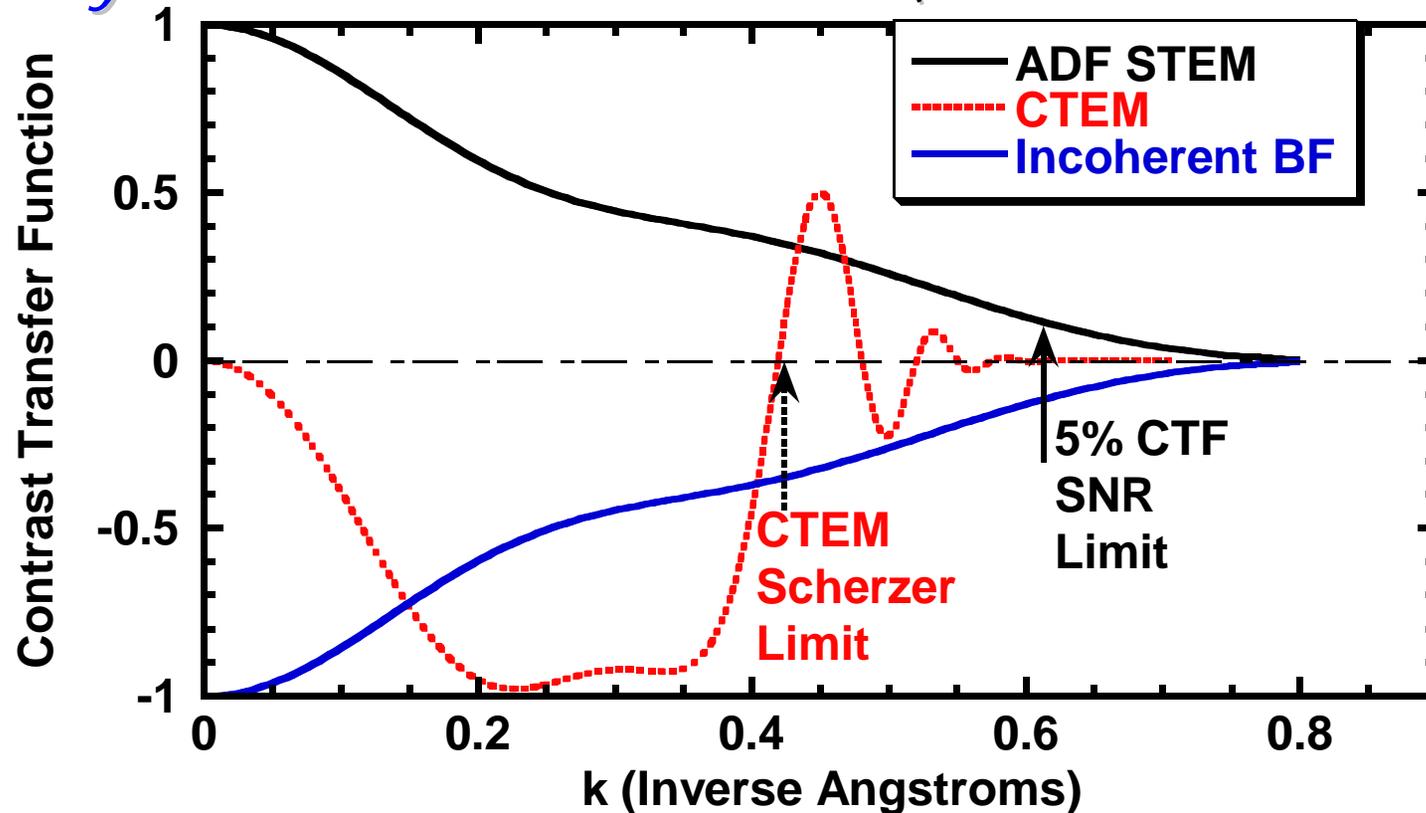
Amplitude Contrast for Different Illumination Angles

(10.5 mr Objective, $E_0=200\text{kV}$, $C_s=1\text{ mm}$, Scherzer Defocus)



- For distances larger than 1 nm, there is little phase contrast to start with.
- When the illumination angles exceeds the objective aperture, **all contrast reversals are removed and the resolution is increased!**

Why Increased Resolution? (coherent vs. incoherent imaging)



- $E_0 = 200 \text{ kV}$
- $C_s = 1.0 \text{ mm}$
- Scherzer aperture and defocus

- Coherent imaging PSF is the probe wavefunction,
- Incoherent imaging PSF is the **square** of wavefunction

Eg: $\varphi(r) \approx \exp(-r^2 / \sigma^2)$

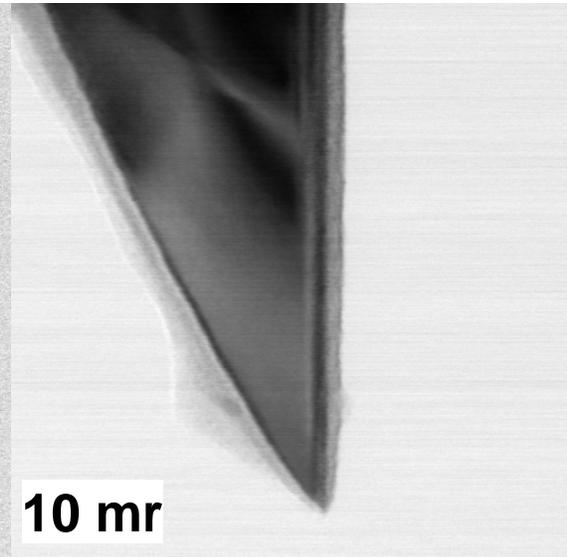
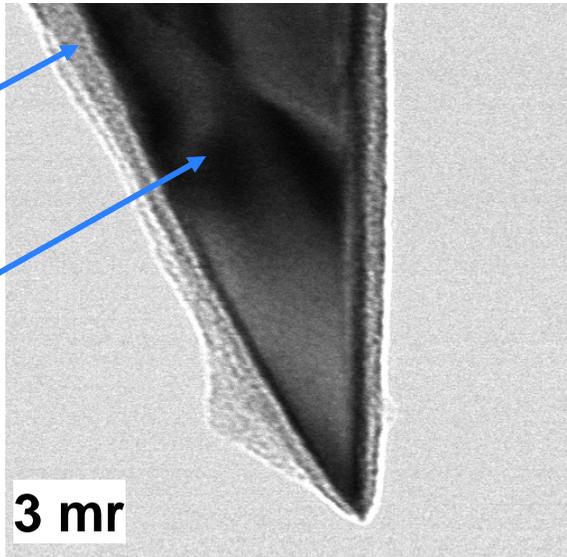
$$|\varphi(r)|^2 \approx \exp(-2r^2 / \sigma^2) \Rightarrow \sigma' = \sigma / \sqrt{2}$$

Increasing the Collector Angle (θ_c)



$$\theta_c \ll \theta_{obj}$$

- Phase contrast
- Diffraction contrast

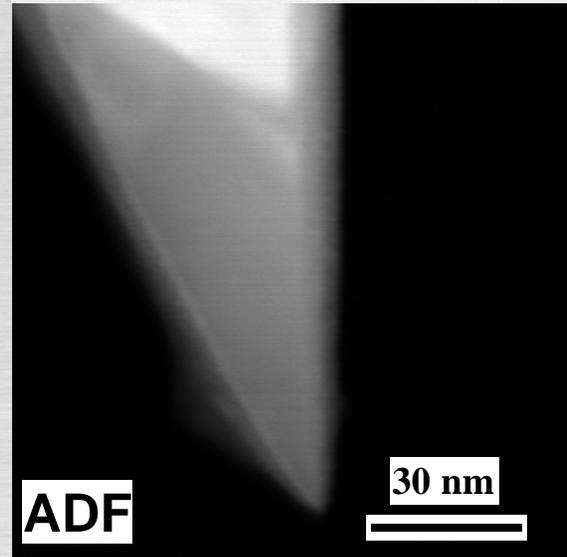
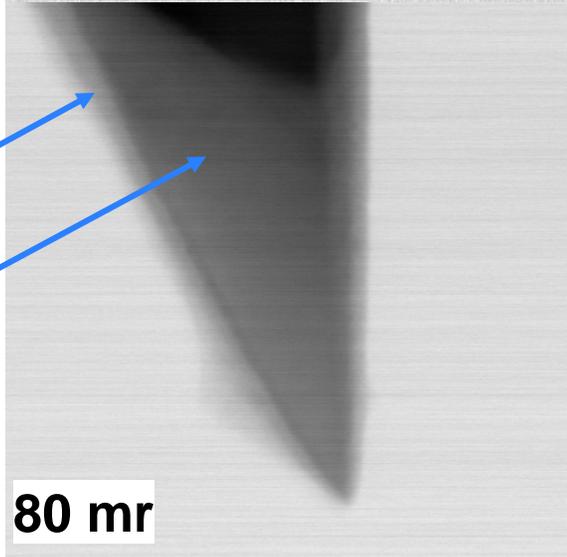


$$\theta_c \approx \theta_{obj}$$

- **No** Phase contrast
- Diffraction contrast

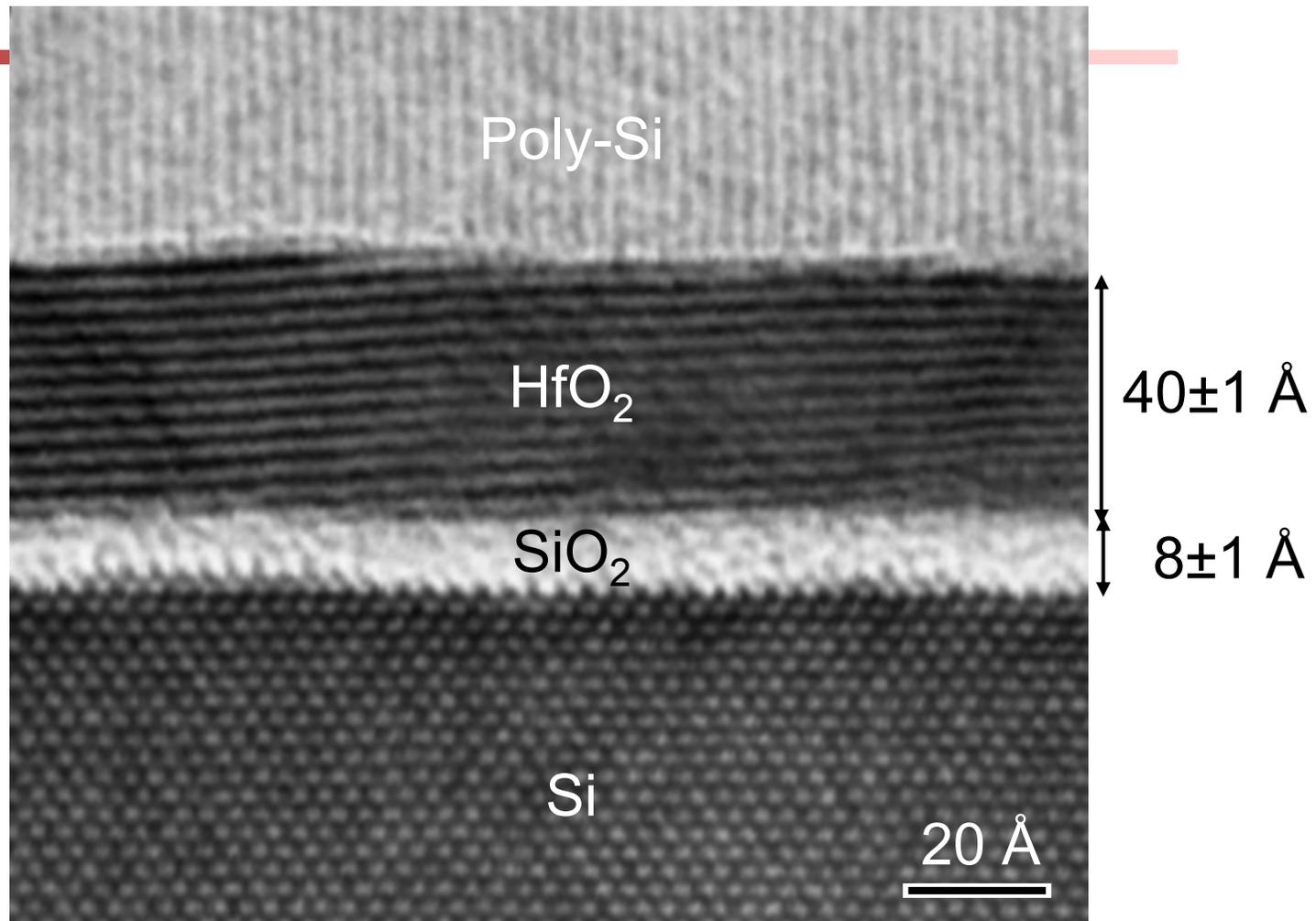
$$\theta_c \gg \theta_{obj}$$

- **No** Phase contrast
- **No** Diffraction contrast



The incoherent BF image is the complement of the ADF image

WiSi40 - 40Å HfO₂ on O₃ Underlayer + 850C/Spike/NO (6/12/2)

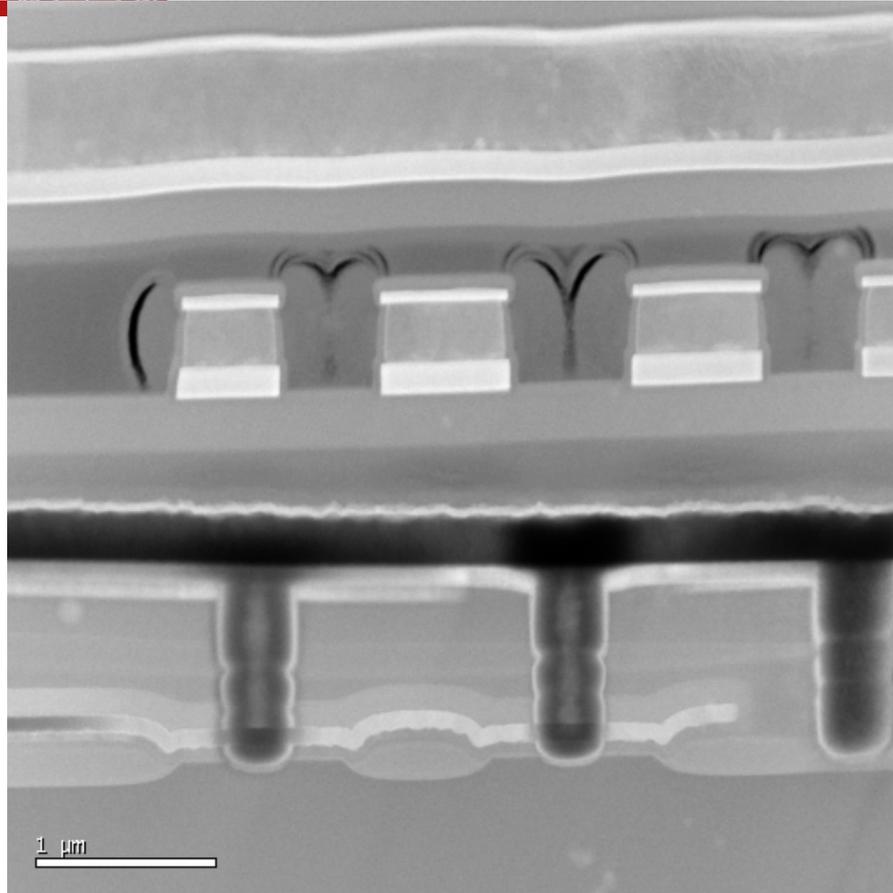


Bright-field STEM with small collector- like conventional TEM

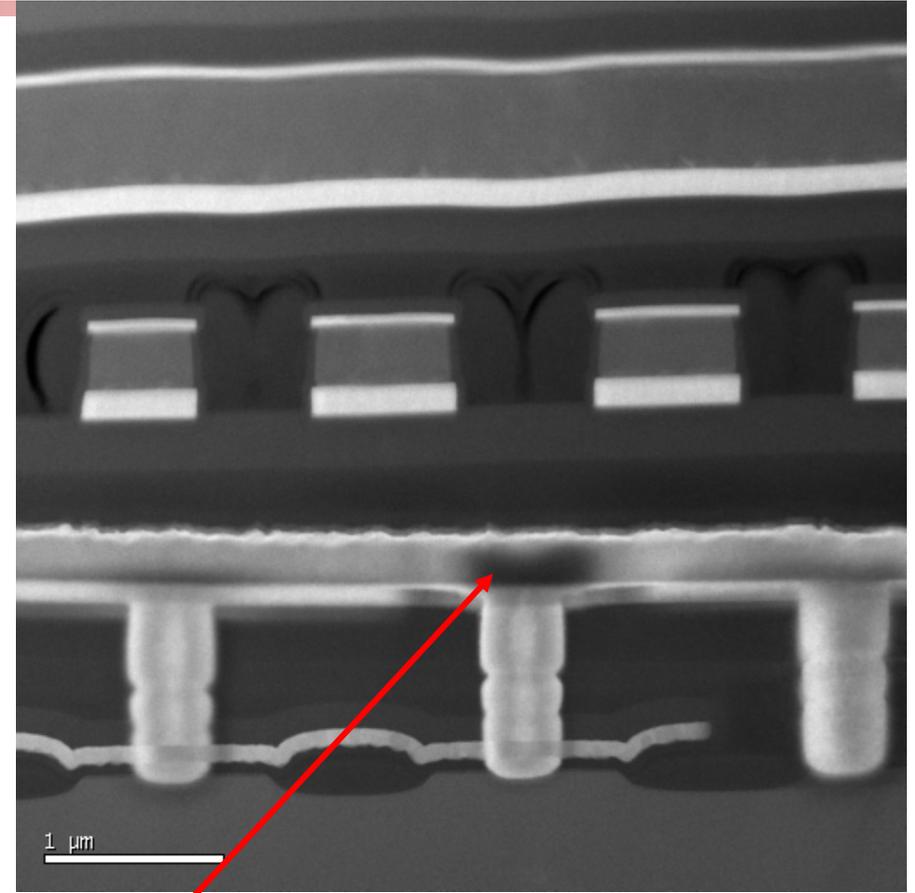
Imaging Thick Samples at 200kV



ADF-STEM ($\theta_c > 45$ mr)

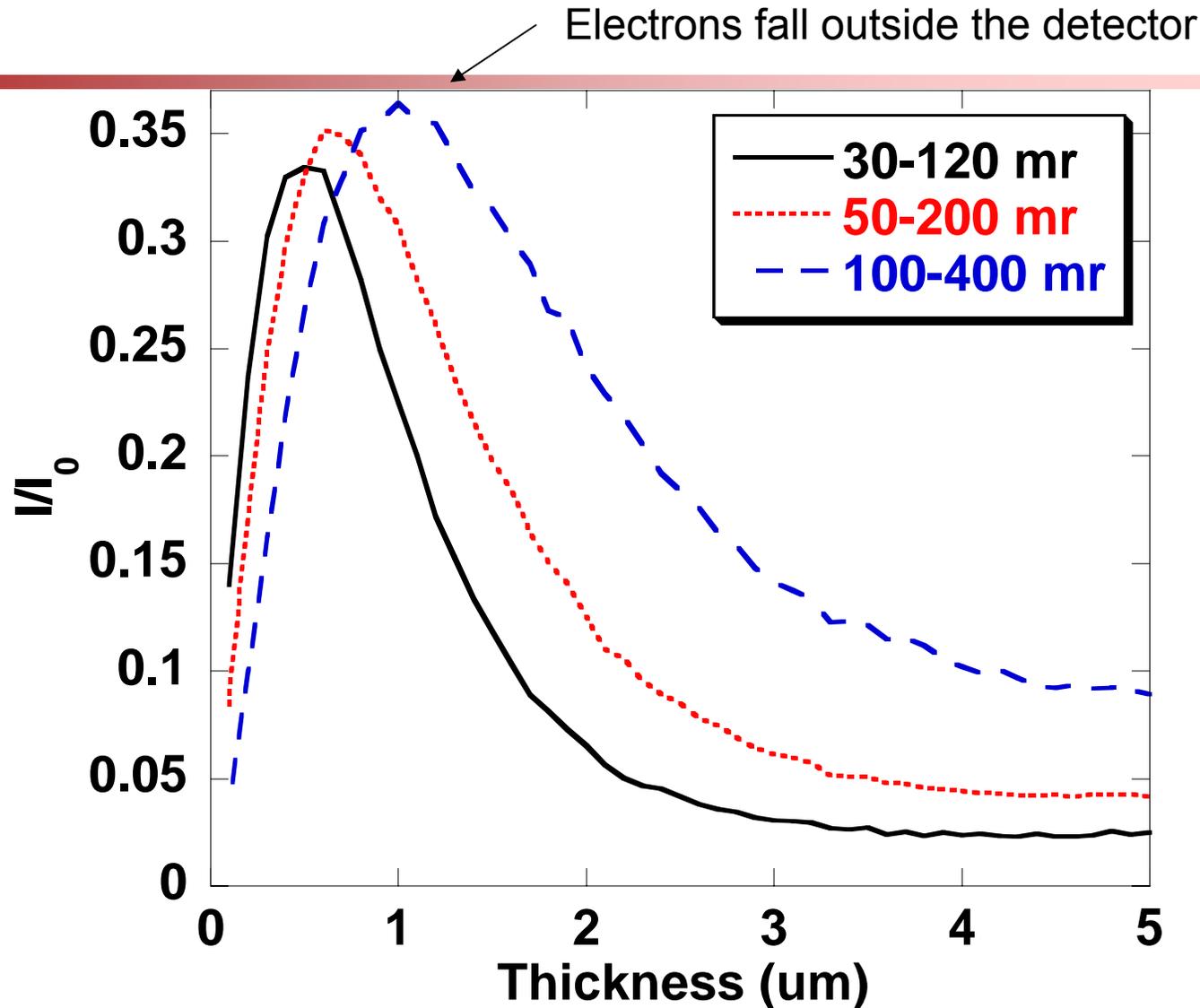


ADF-STEM ($\theta_c > 75$ mr)



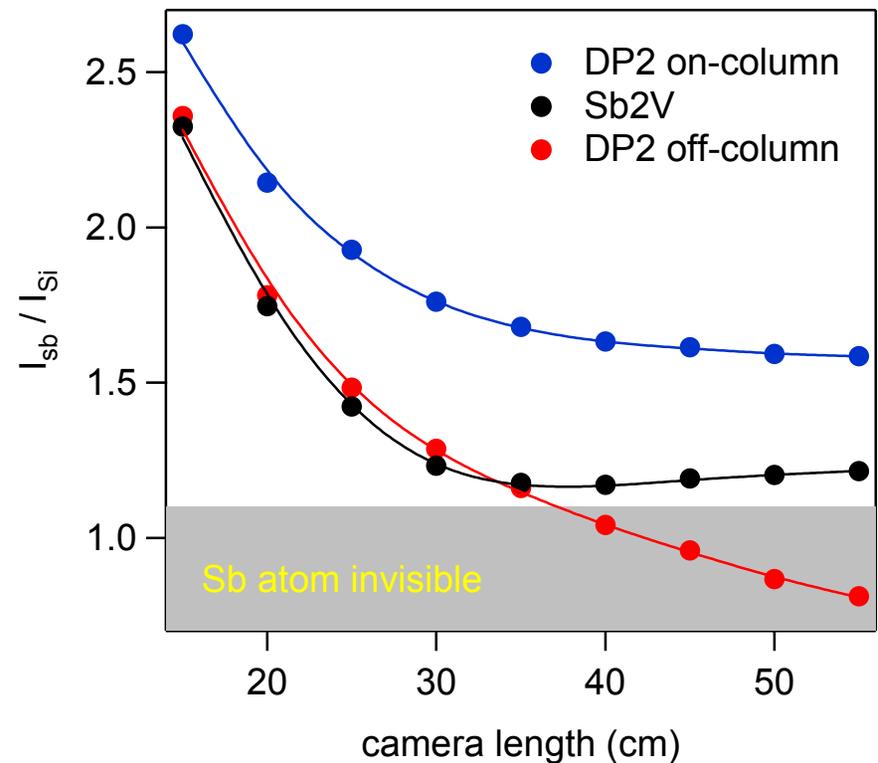
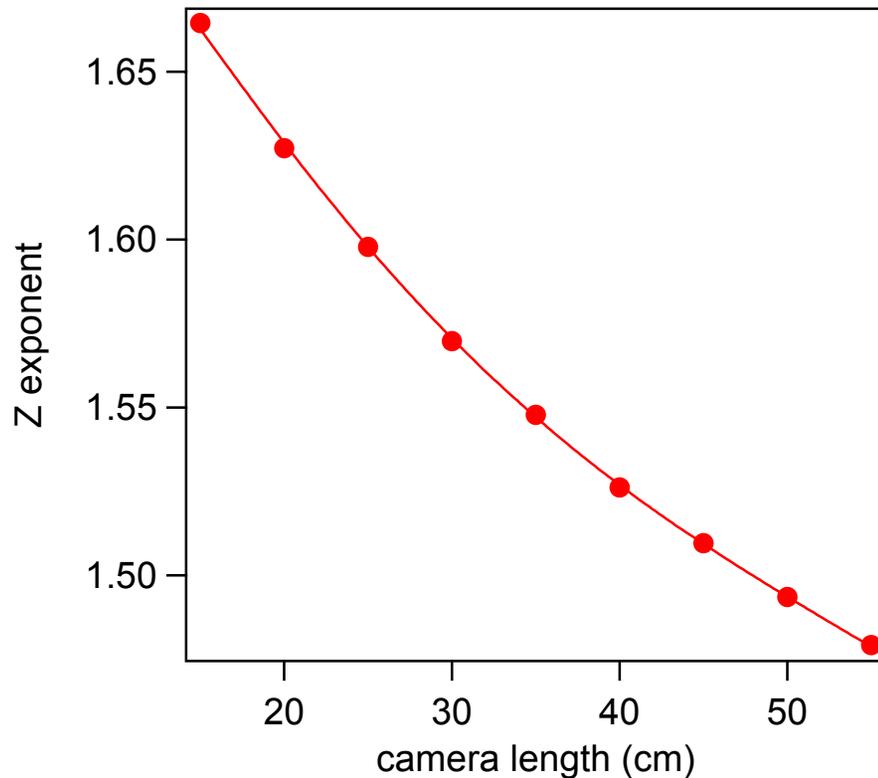
- No more diffraction contrast
- Signal in W plug not monotonic, could be mistaken for voids
- Effect reduced by increasing the collector angle

Annular Dark Field STEM at 200 kV



- Interpretable (monotonic, single valued) signal in Silicon to $\sim 1 \mu\text{m}$ depth
- There is a geometric limit to the detector angles ($\sim 200\text{-}400 \text{ mr}$)

Effect of Camera Length



Channeling enhances on-column Sb intensity.

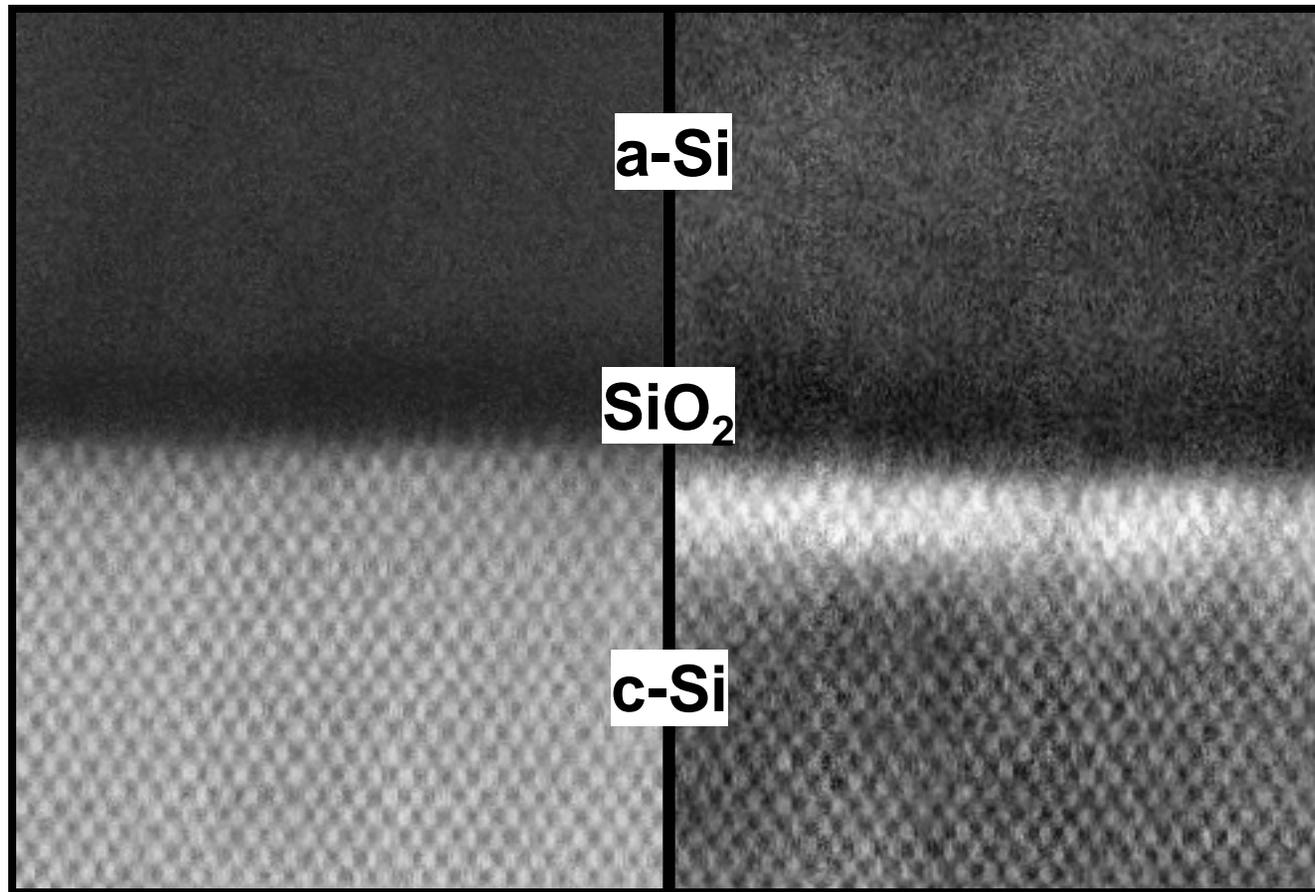
Strain Contrast at Si/SiO₂ Interfaces

(JEOL 2010F, 200 kV, C_s=1mm)

ADF Inner angle:

50 mrad

25 mrad



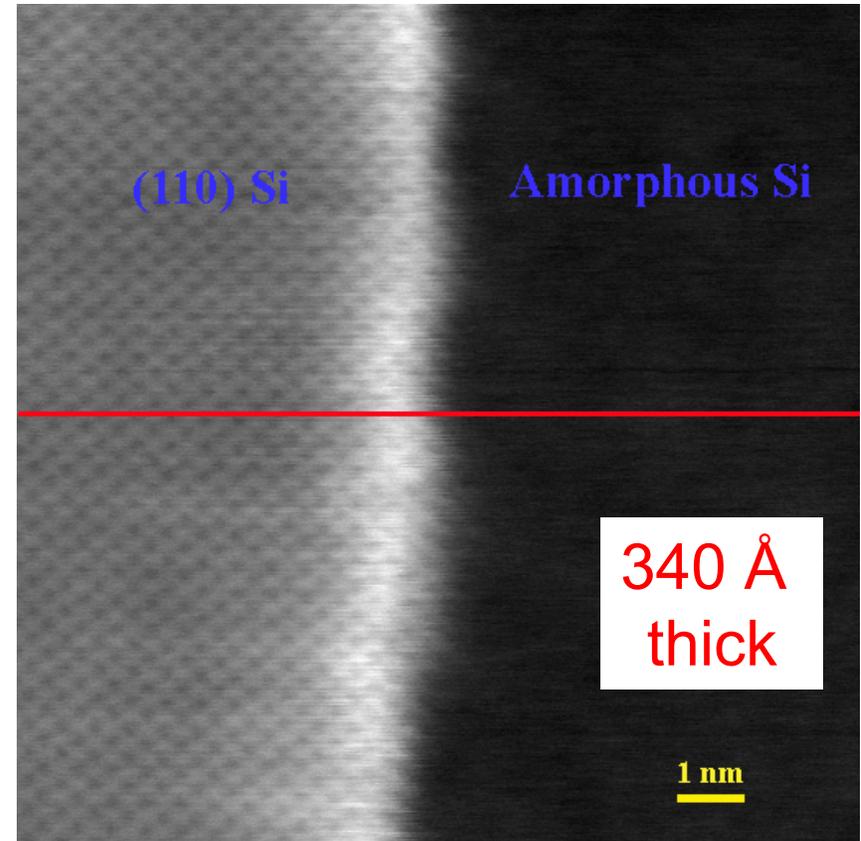
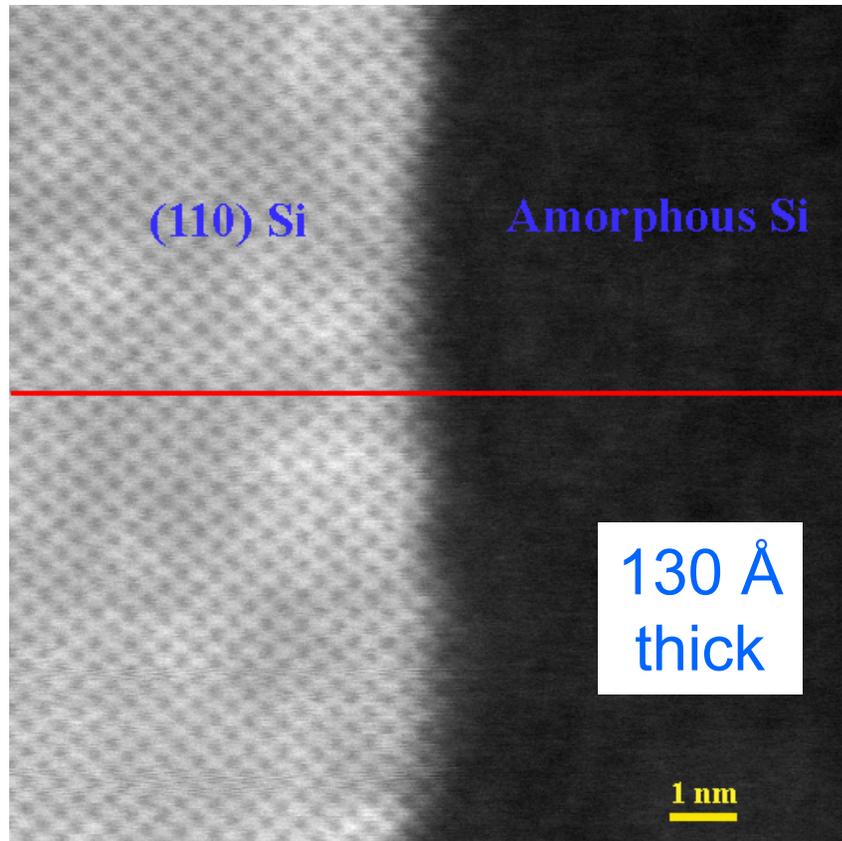
Strain Fields cause dechanneling (and scattering to small angles)

Z. Yu, D. A. Muller, and J. Silcox, *J. Appl. Phys.* **95**, 3362 (2004).

Strain Contrast vs. Sample Thickness

Contrast at a c-Si/-aSi is strongly depends on sample thickness

100 kV, 45 mrad ADF inner angle



Strain Contrast effects at the interface:

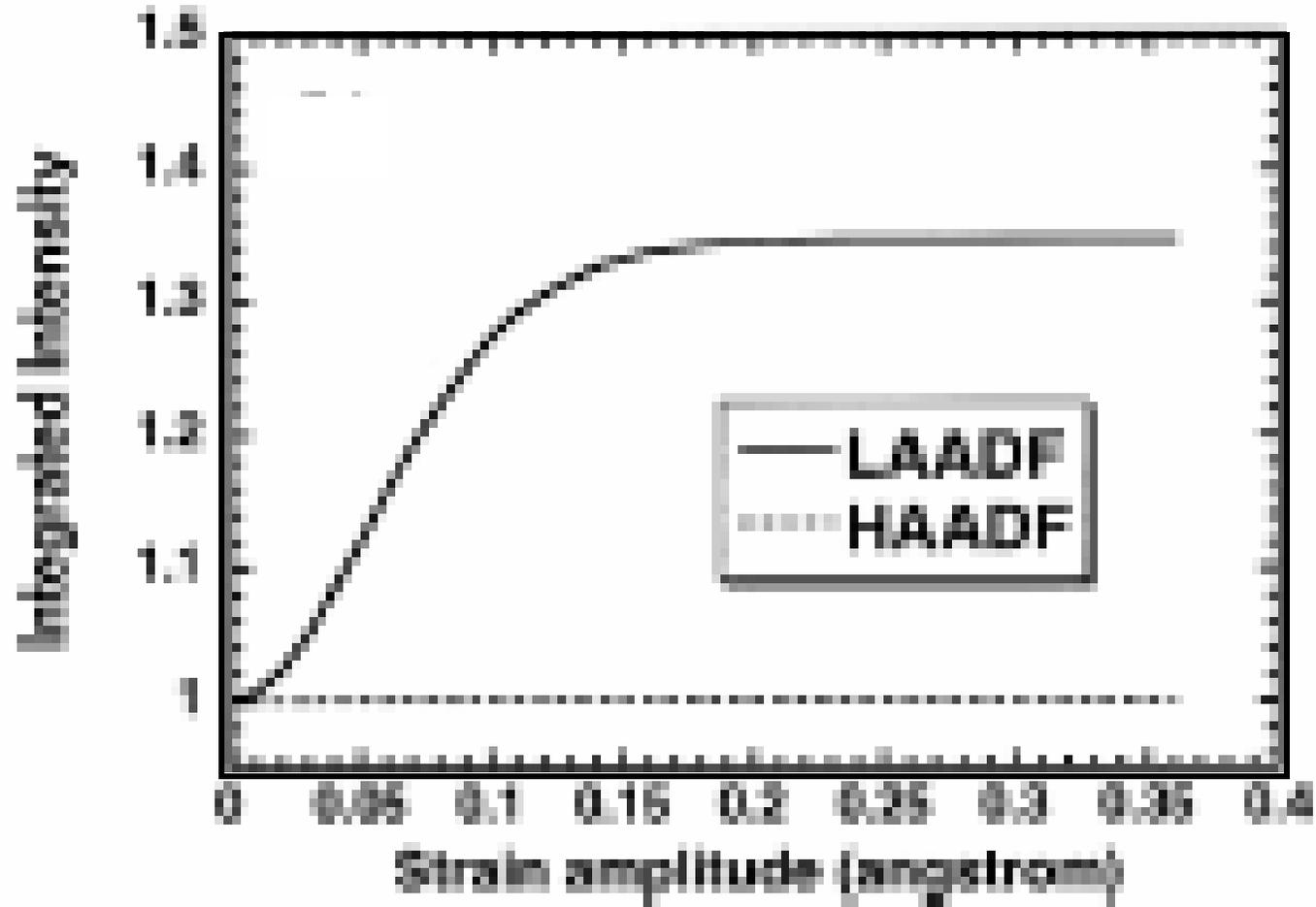
for 130 Å thick sample, ~0%; for 340 Å thick sample, 15%.

Z. Yu, D. A. Muller, and J. Silcox, *J. Appl. Phys.* **95**, 3362 (2004).

Contrast from Random Strain Fields



(treated as a static Debye-Waller Factor)

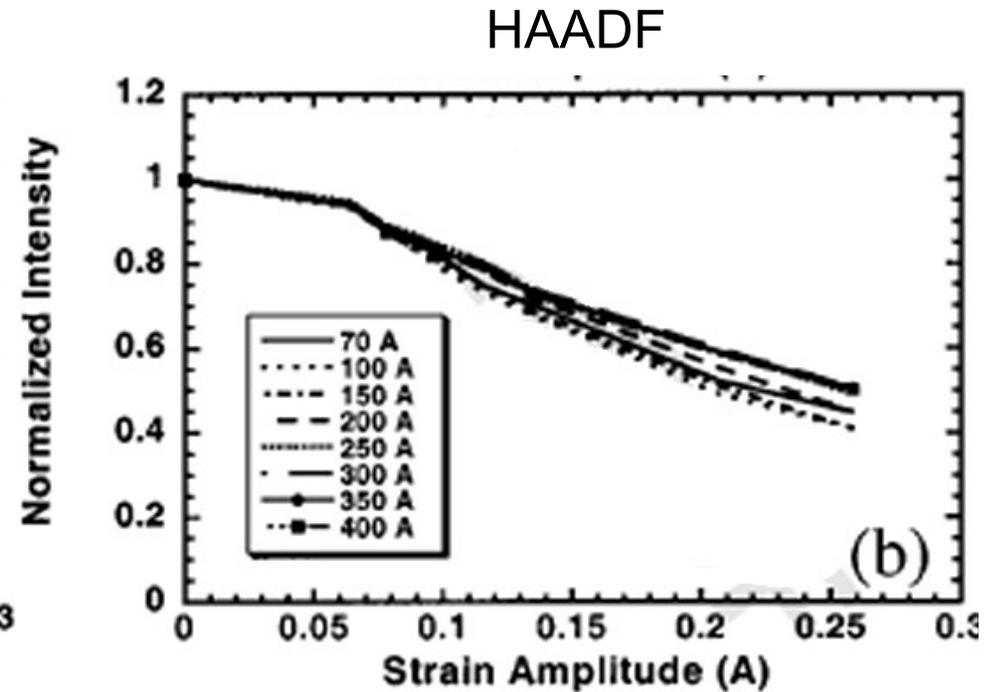
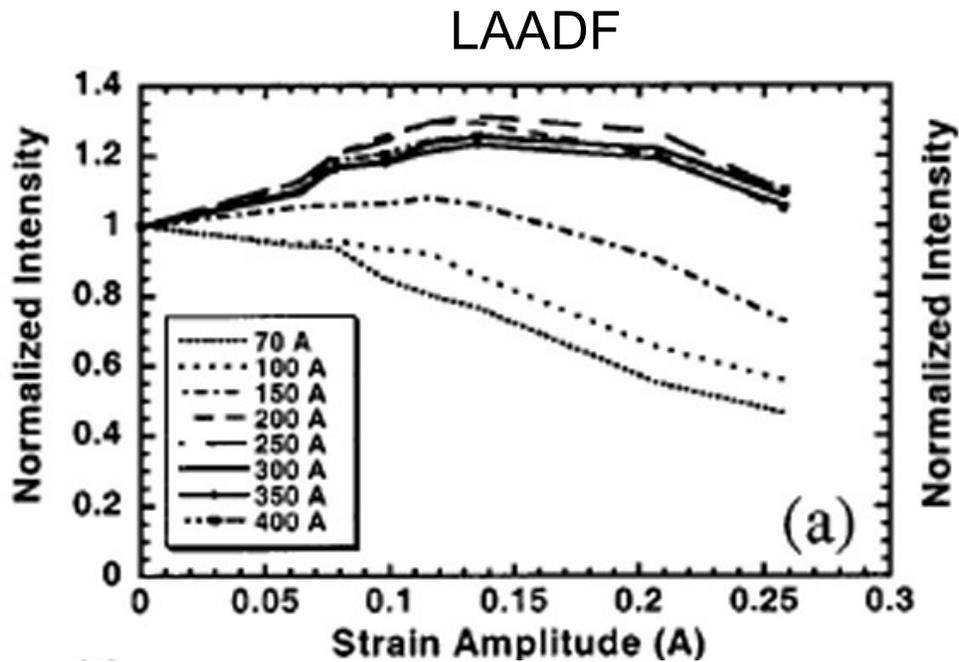


No channeling  No thickness dependence

Contrast from Random Strain Fields



(using frozen phonons in multislice)

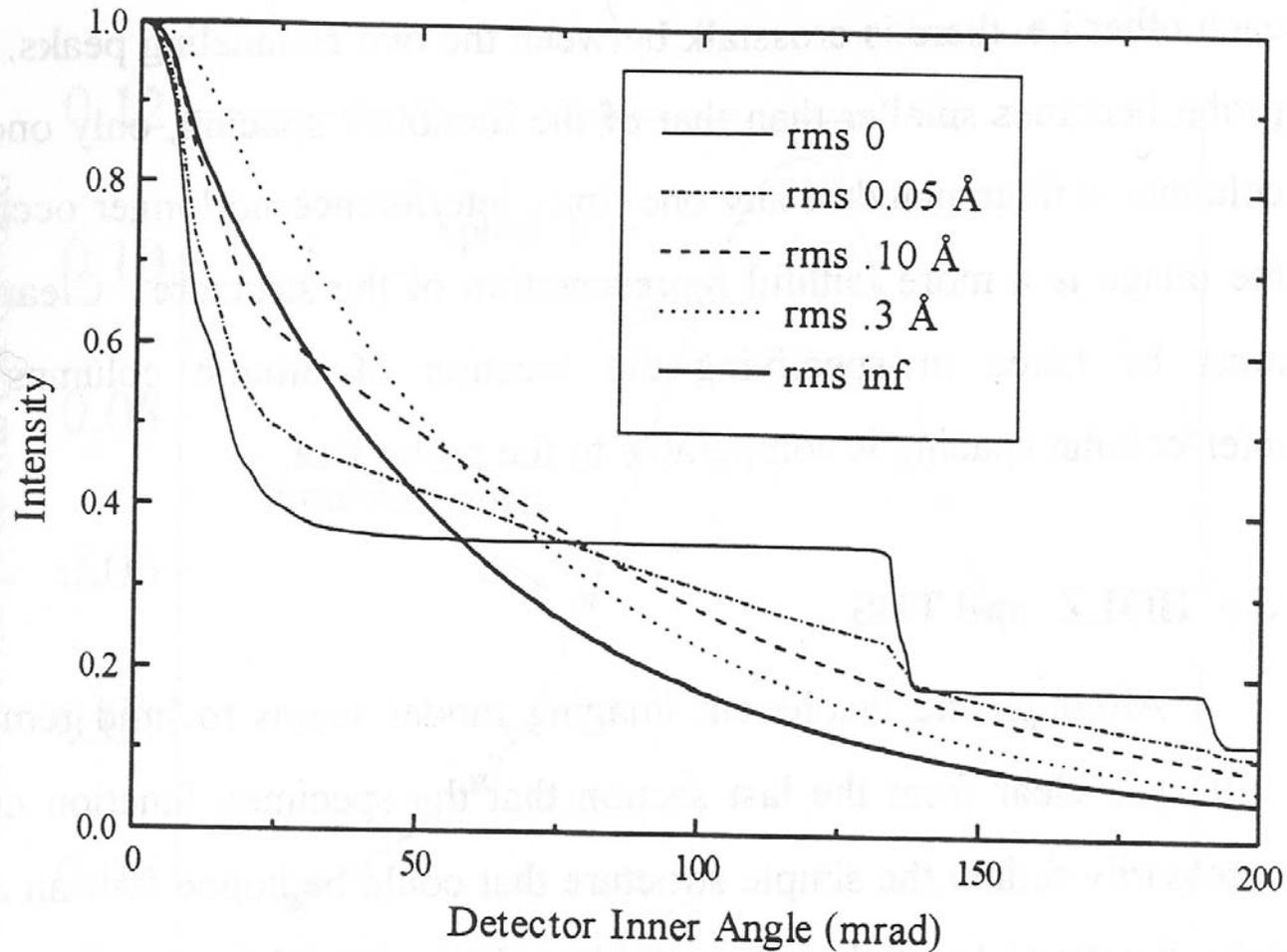


Channeling  Thickness dependence

Contrast from Random Strain Fields



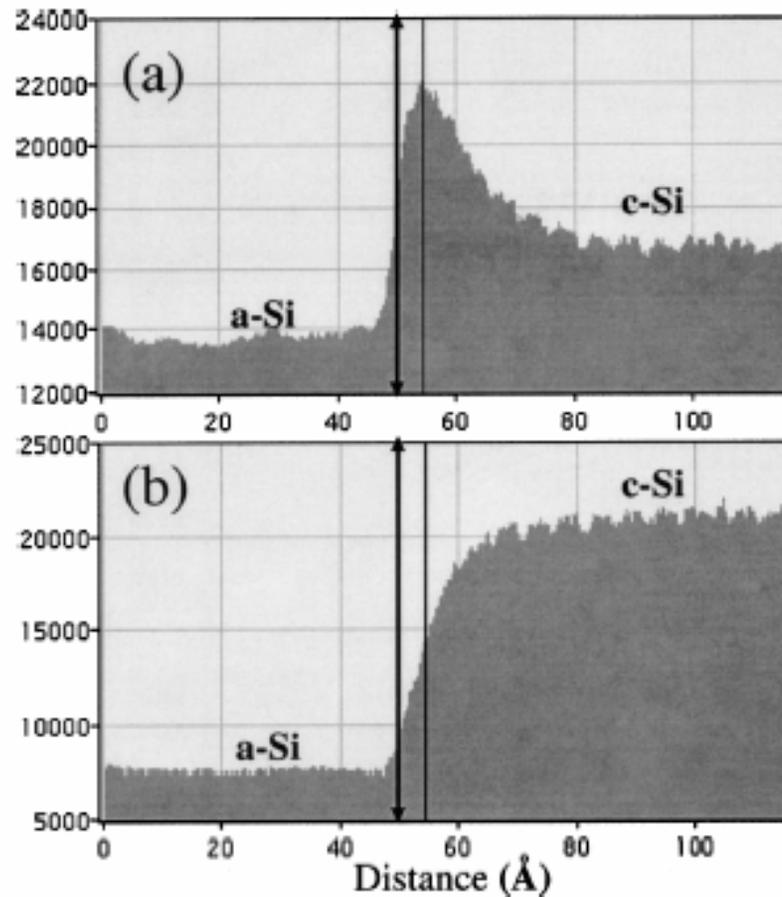
(using frozen phonons in multislice)



Contrast from Random Strain Fields



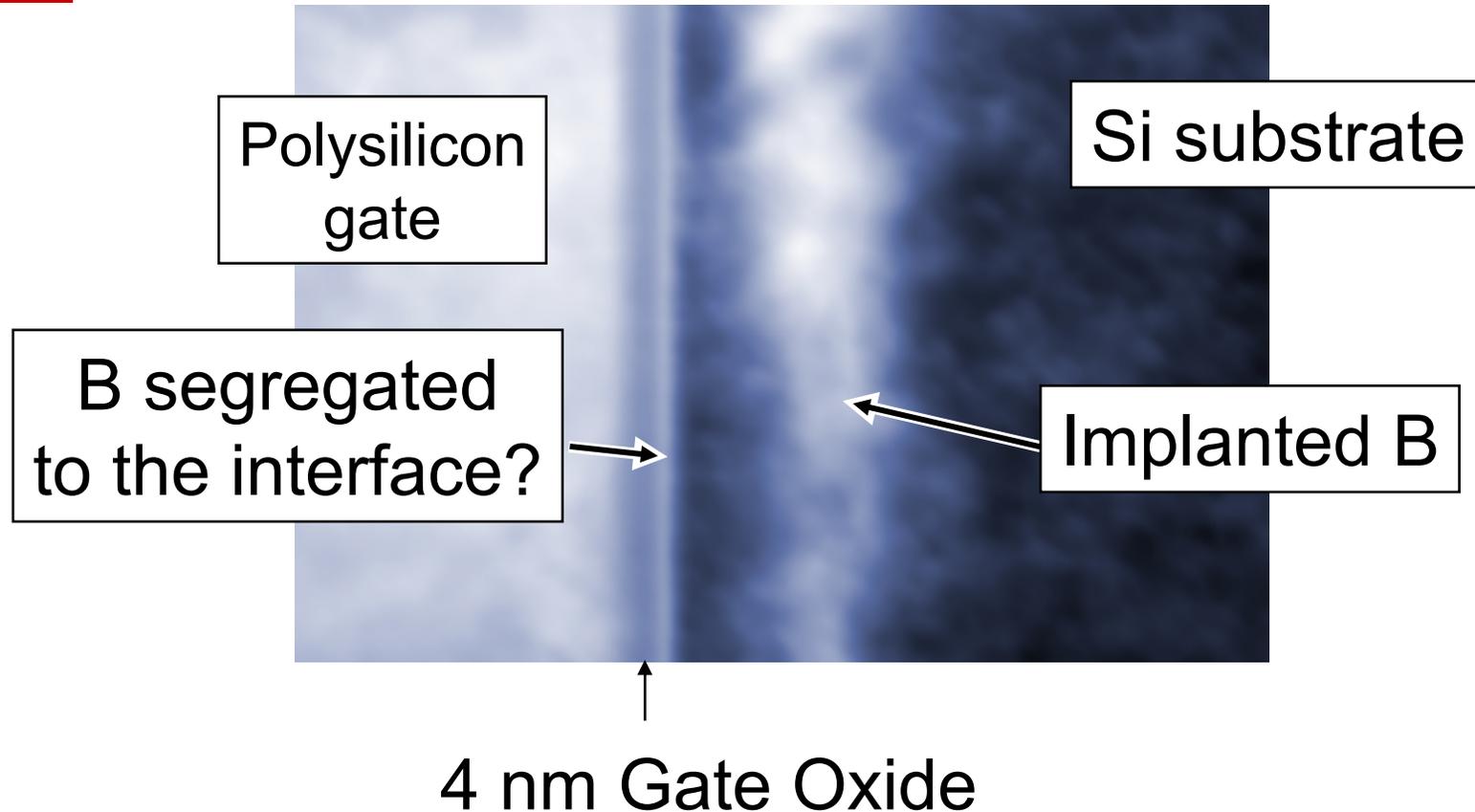
(treated as a static Debye-Waller Factor)



Imaging Light Atoms



Dechanneling contrast from the Strain Field around impurities



Single atom contrast is expected at 77K (Hillyard and Silcox)

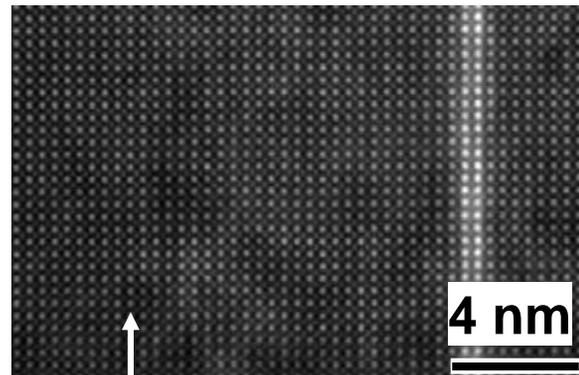
Imaging Vacancies?

(grow 25 layers of $\text{SrTiO}_{3-\delta}$ on SrTiO_3)

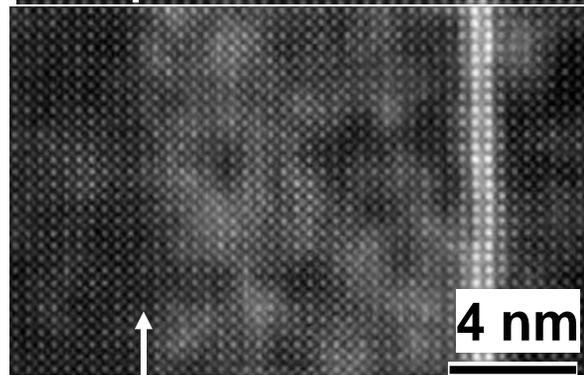
D. A. Muller et al *Nature* **430**, 657-661 (2004).



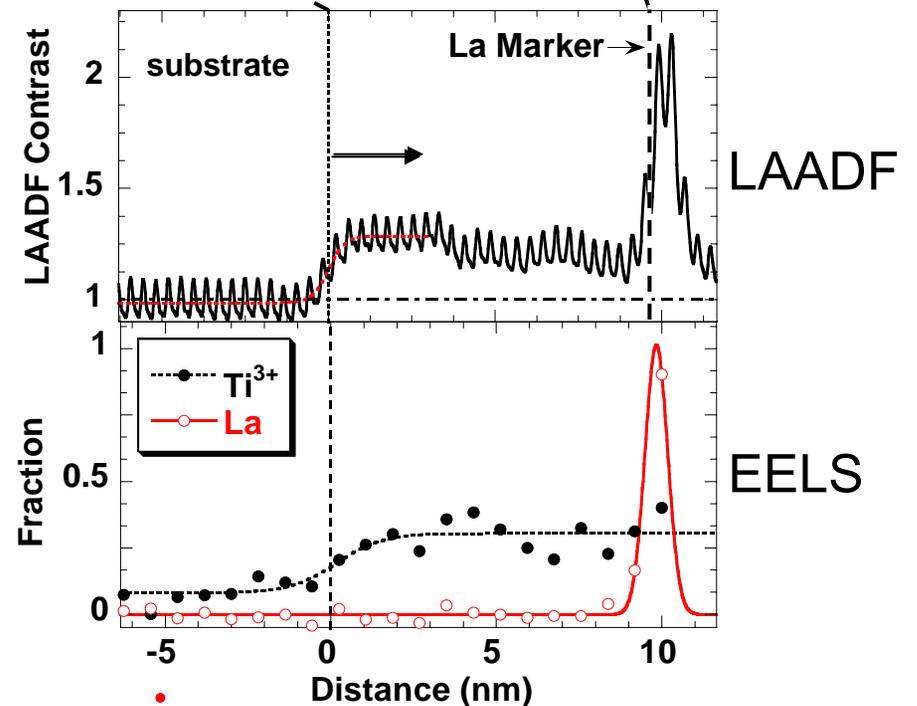
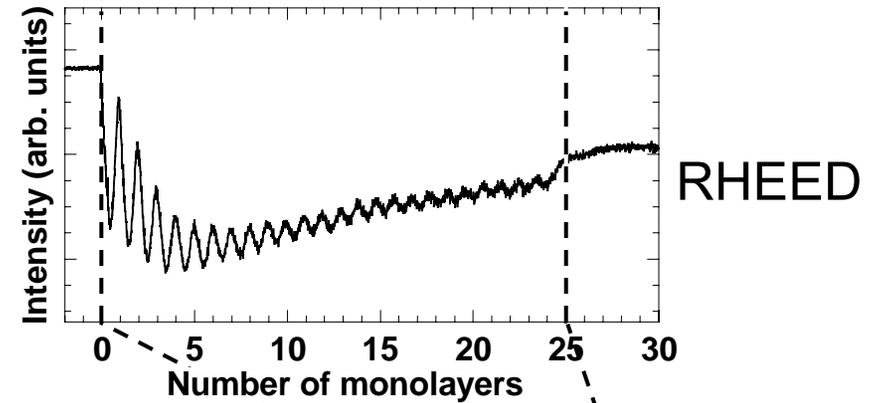
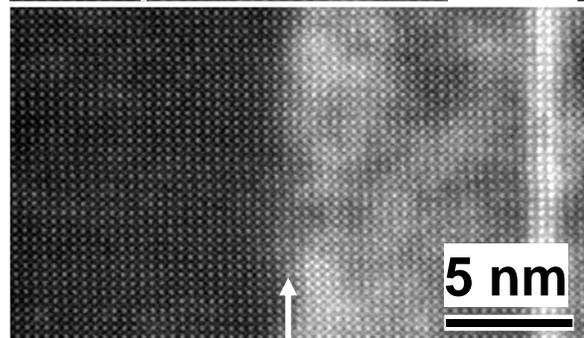
HAADF
“Z” map



LAADF
“Strain” map
Thin x/s



LAADF
“Strain” map
Thick x/s



Detection sensitivity: 1-4 Oxygen vacancies

Ronchigrams

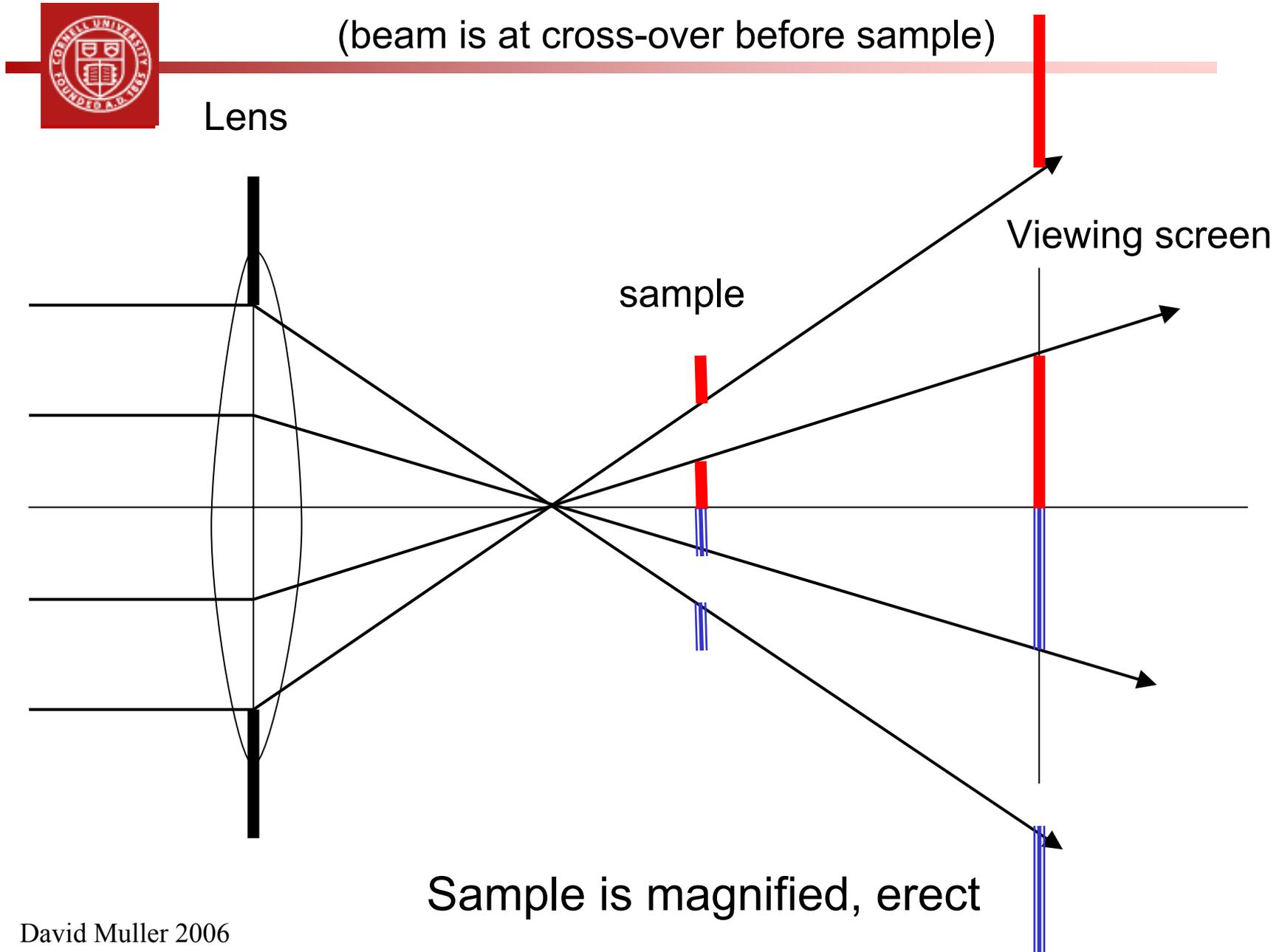


- Most accurate manual method of alignment
- Easy to find the optic axis
- Easy to correct serious astigmatism
- Easy to bring the sample into focus
- Works best on an amorphous layer
- Start with the largest aperture

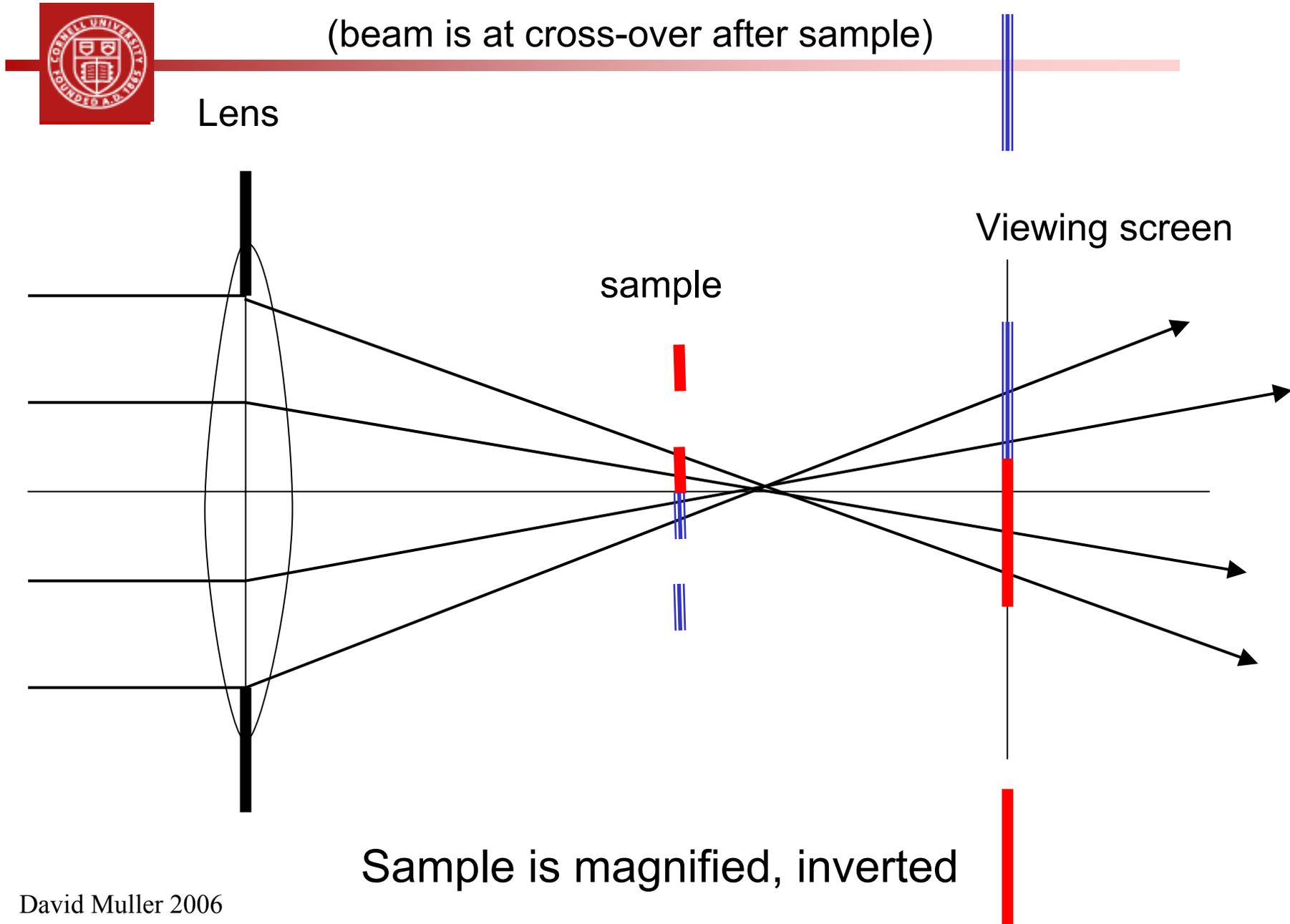
J. M. Cowley, *Ultramicroscopy* **4**, 413-418.(1979)

E. M. James, N. D. Browning, *Ultramicroscopy*, **78** (1999) 125-139

Ronchigrams – no C_s



Ronchigrams – no C_s

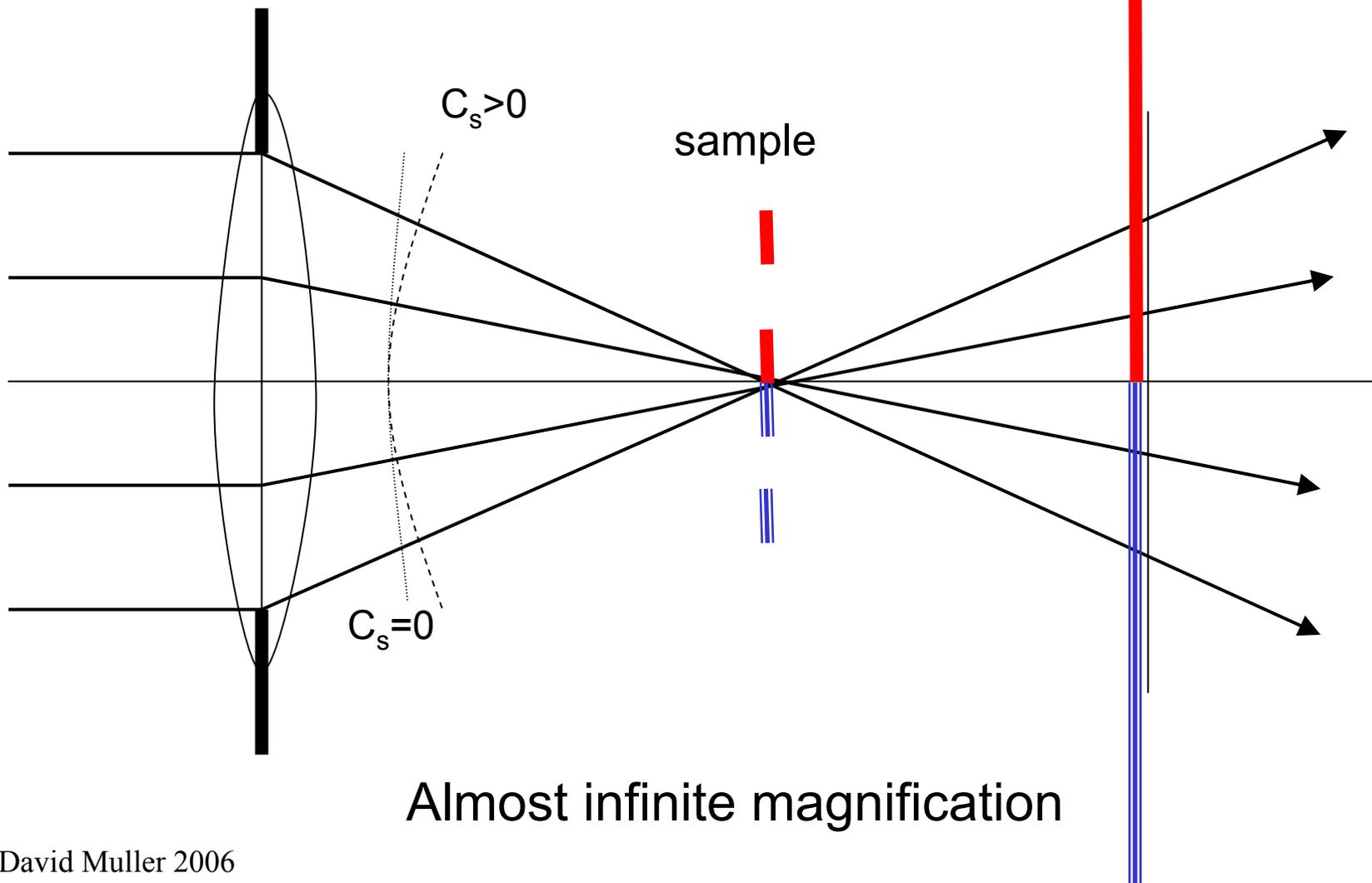


Ronchigrams – no C_s

(beam is at almost cross-over on the sample)



Lens

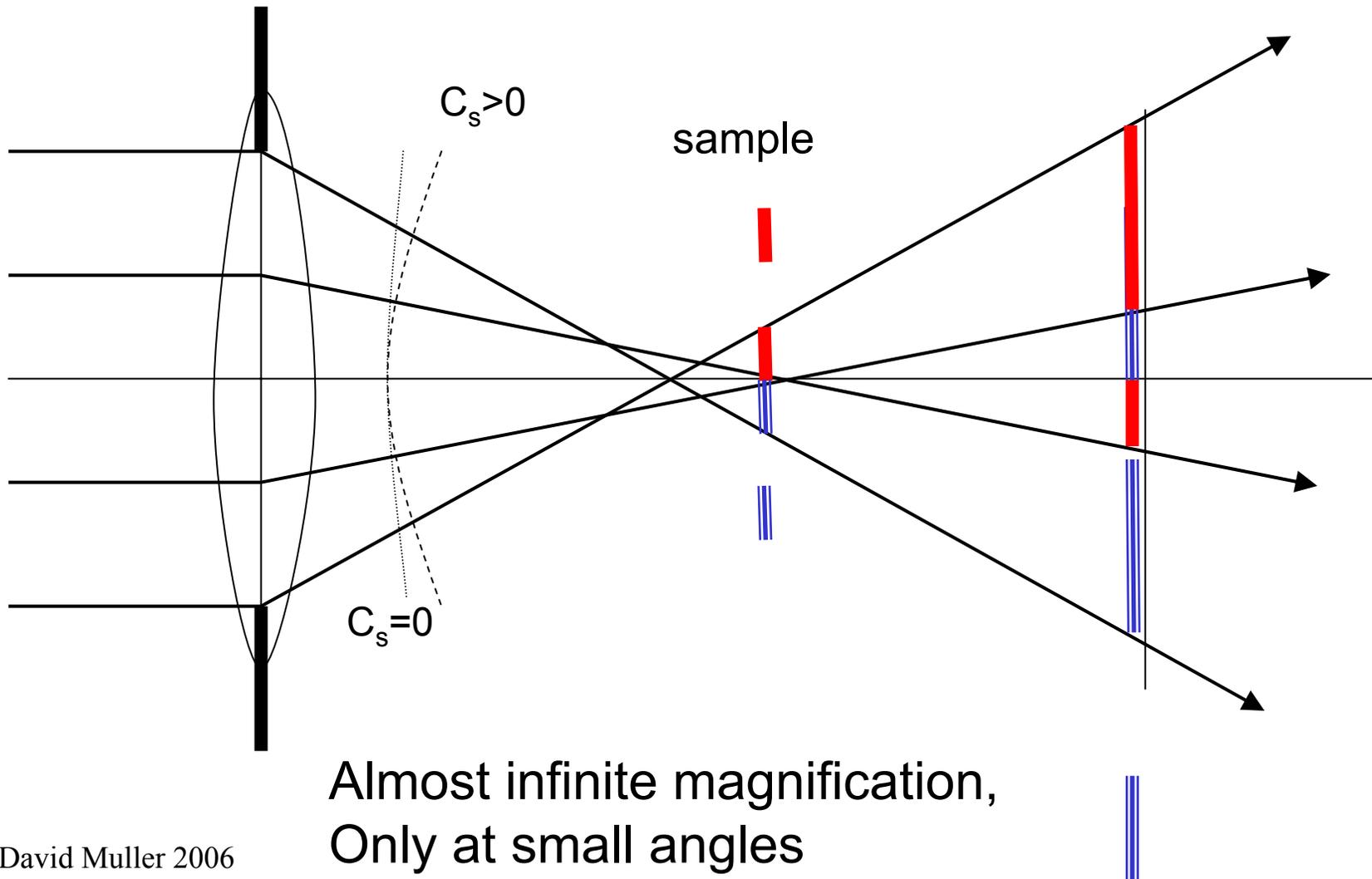


Ronchigrams with Spherical Aberration, C_s

For $C_s > 0$, rays far from the axis are bent too strongly and come to a crossover before the gaussian image plane.

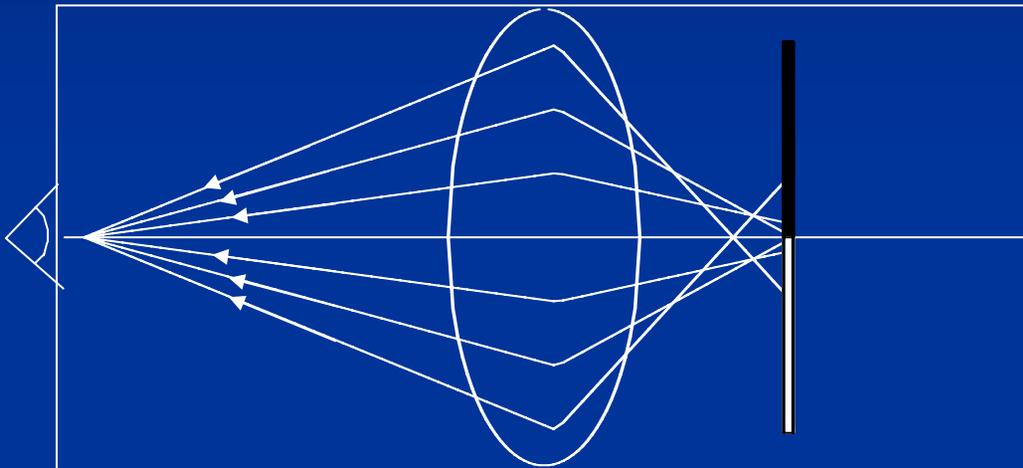


Lens



Almost infinite magnification,
Only at small angles

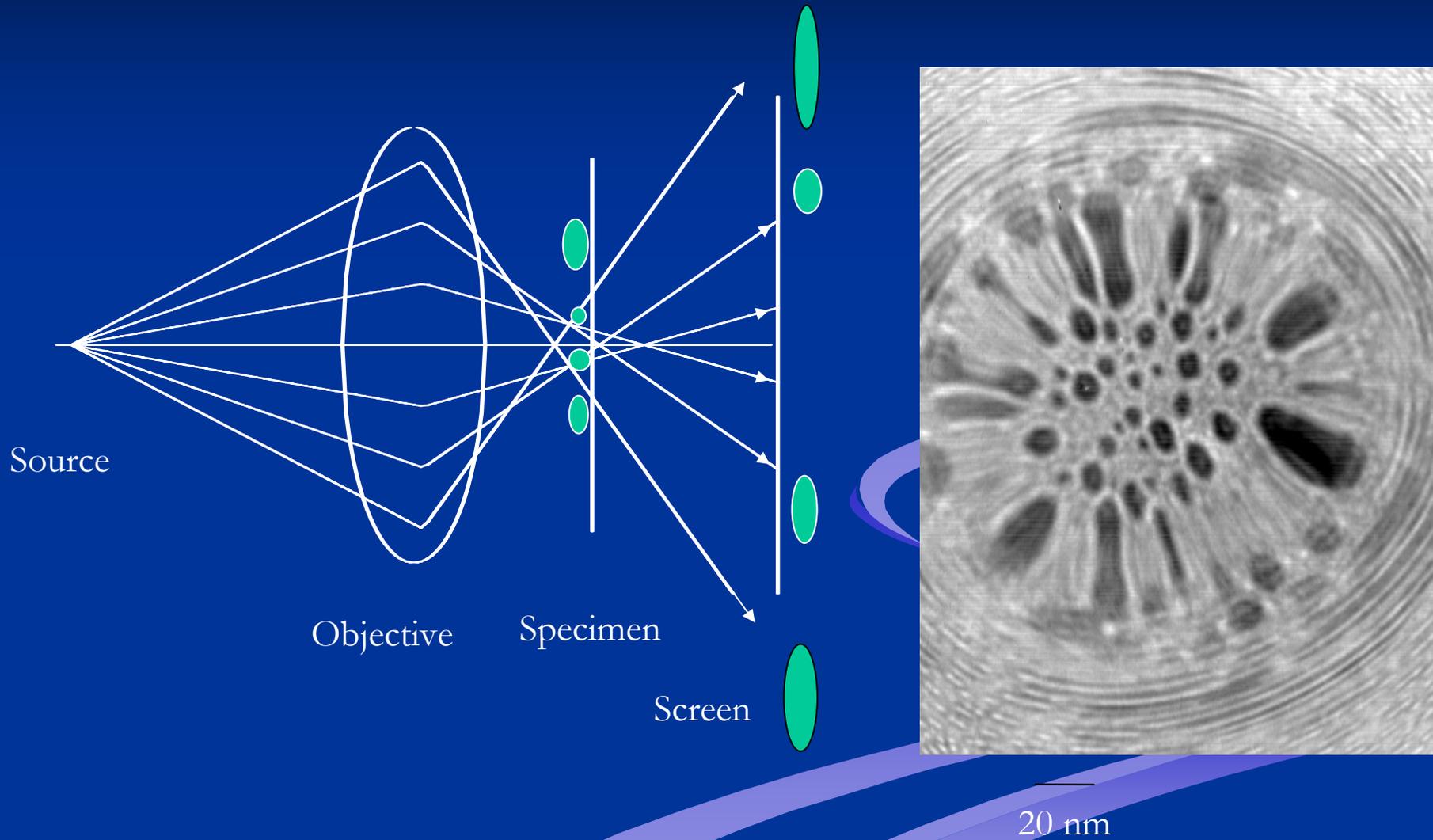
Spherical Aberration



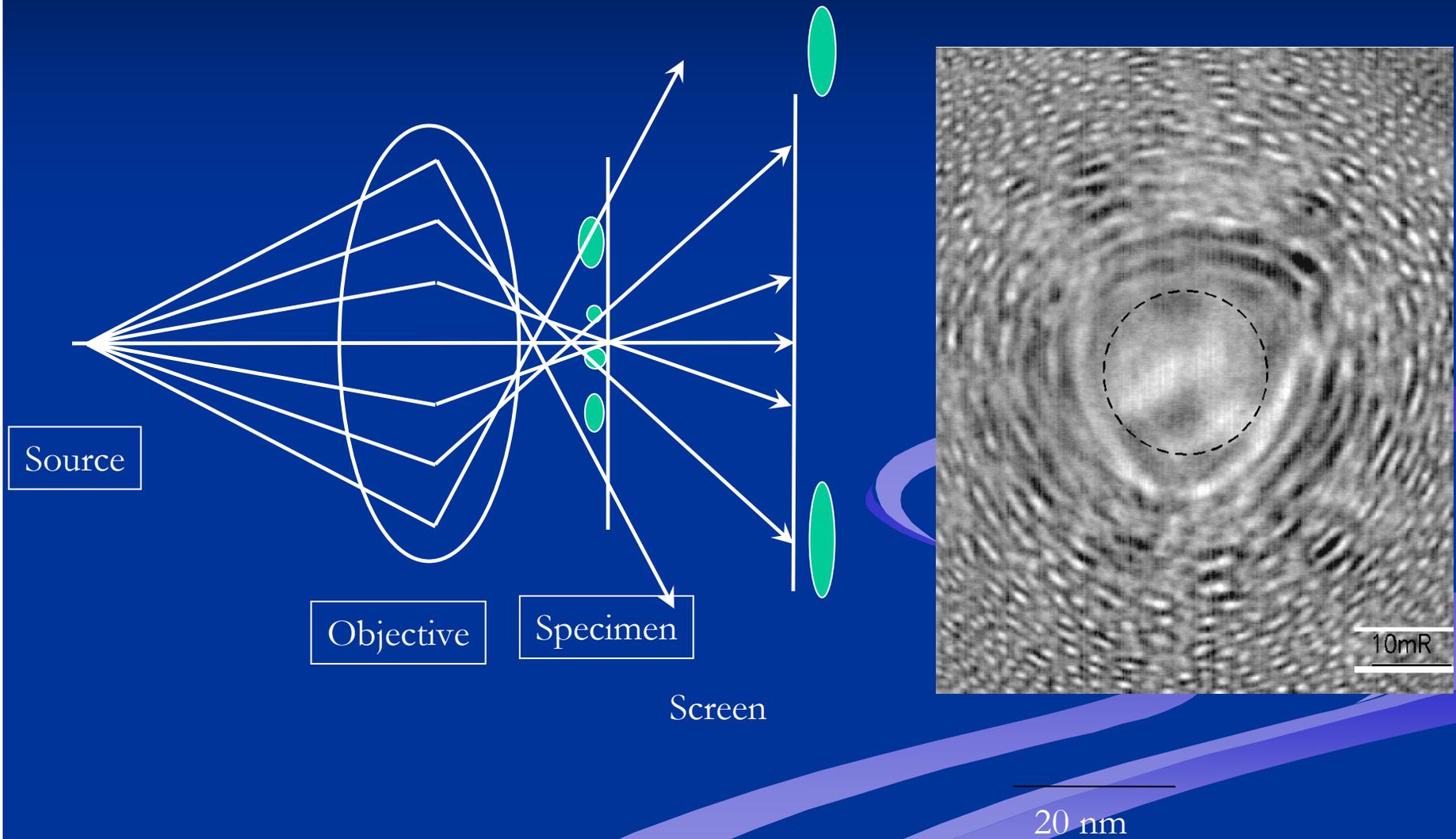
Apparent deflection at the object is proportional to the cube of the distance off-axis within the imaging lens. Deflection towards axis is always too strong.



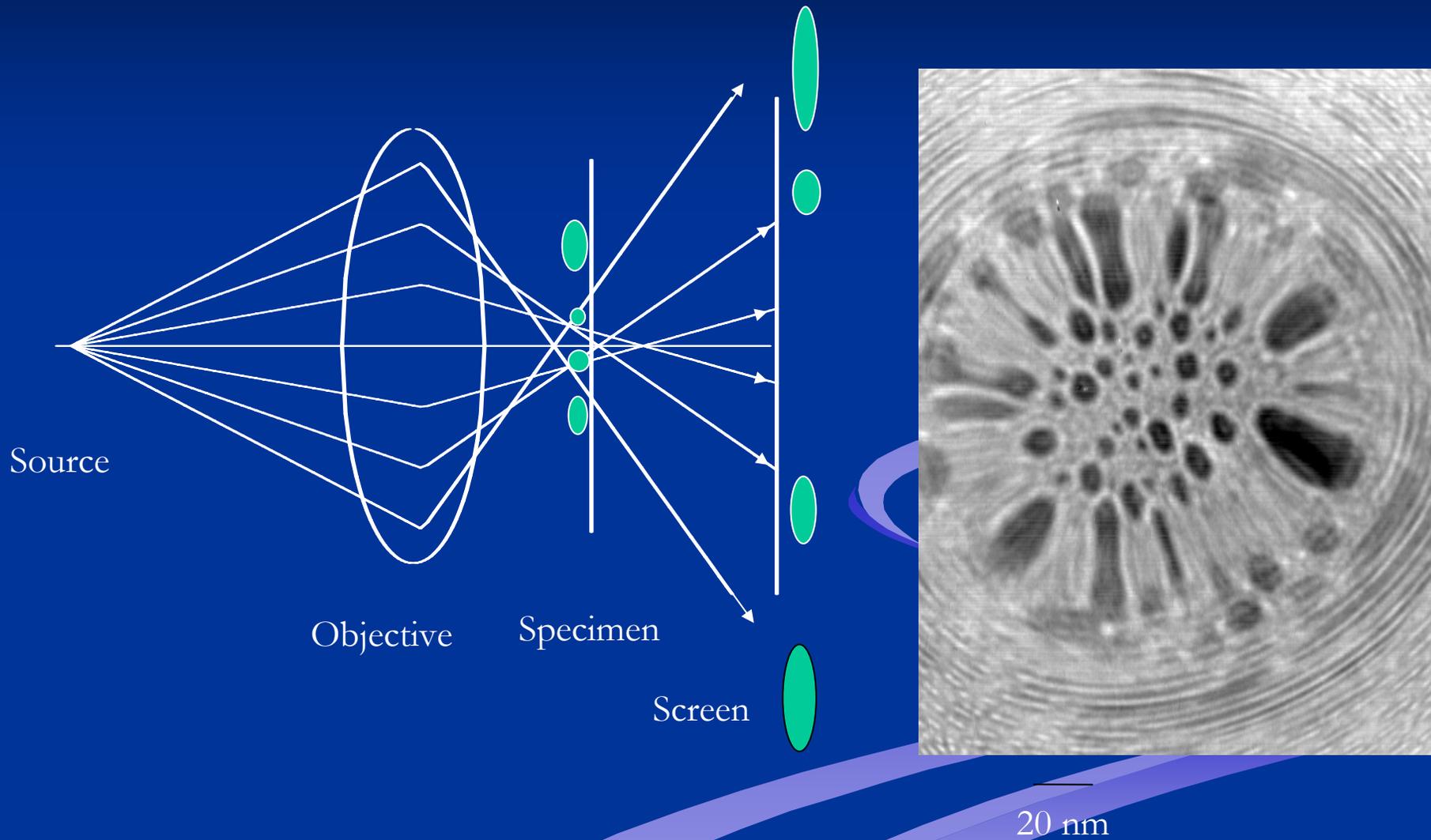
Shadow Map: “Ronchigram”



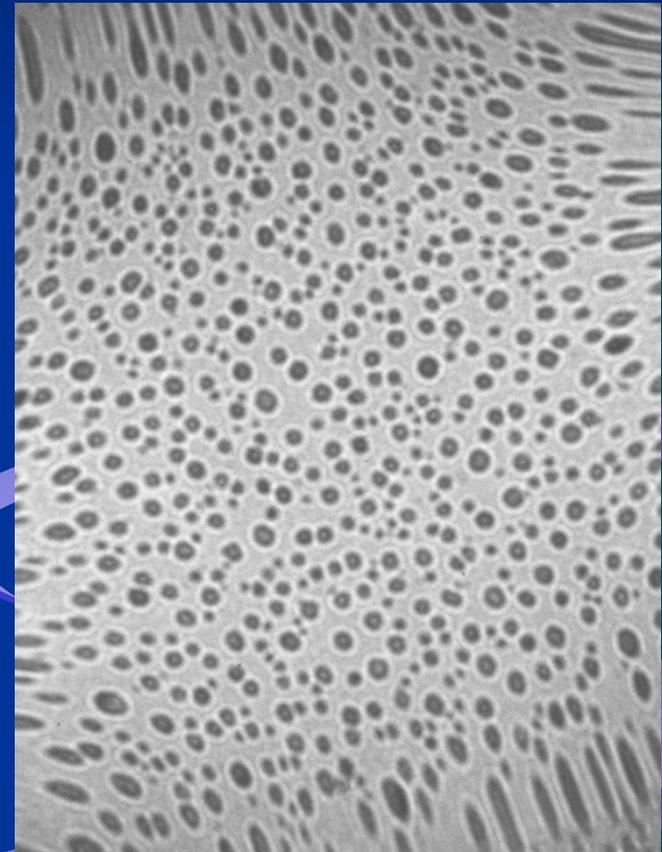
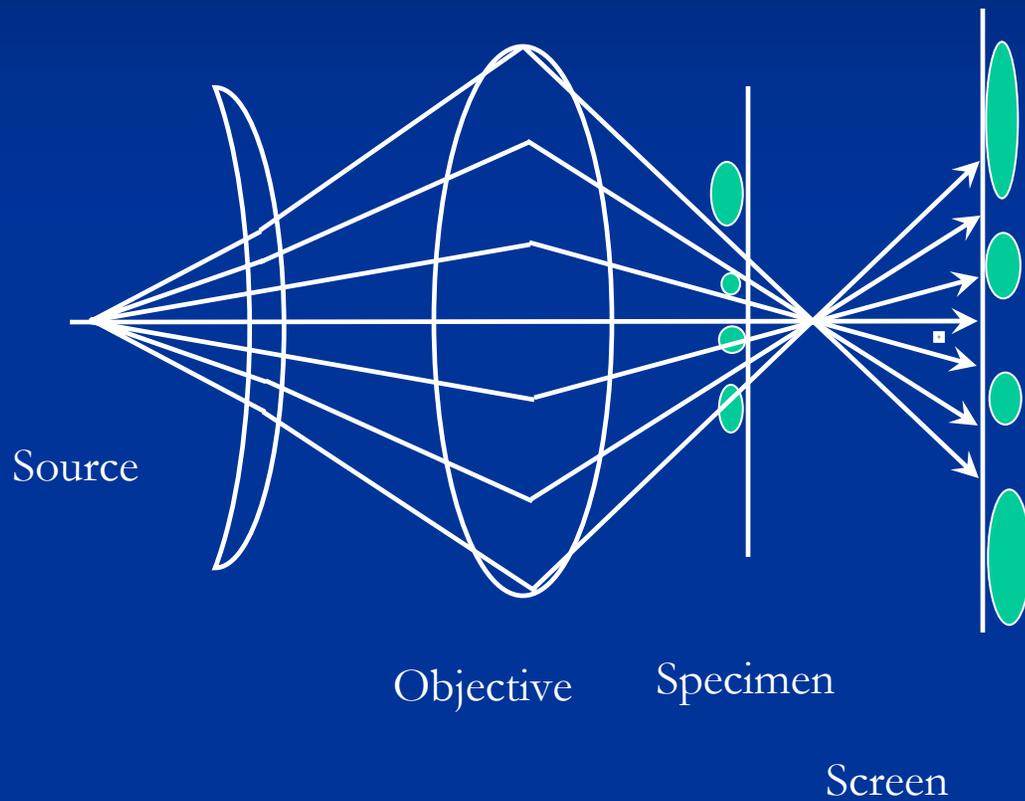
Shadow Map: “Ronchigram”



Shadow Map: “Ronchigram”

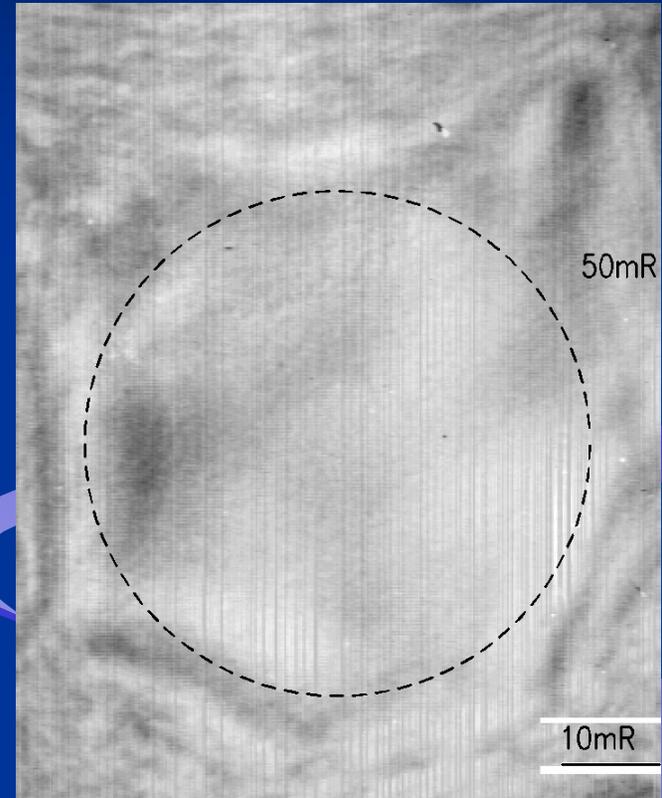
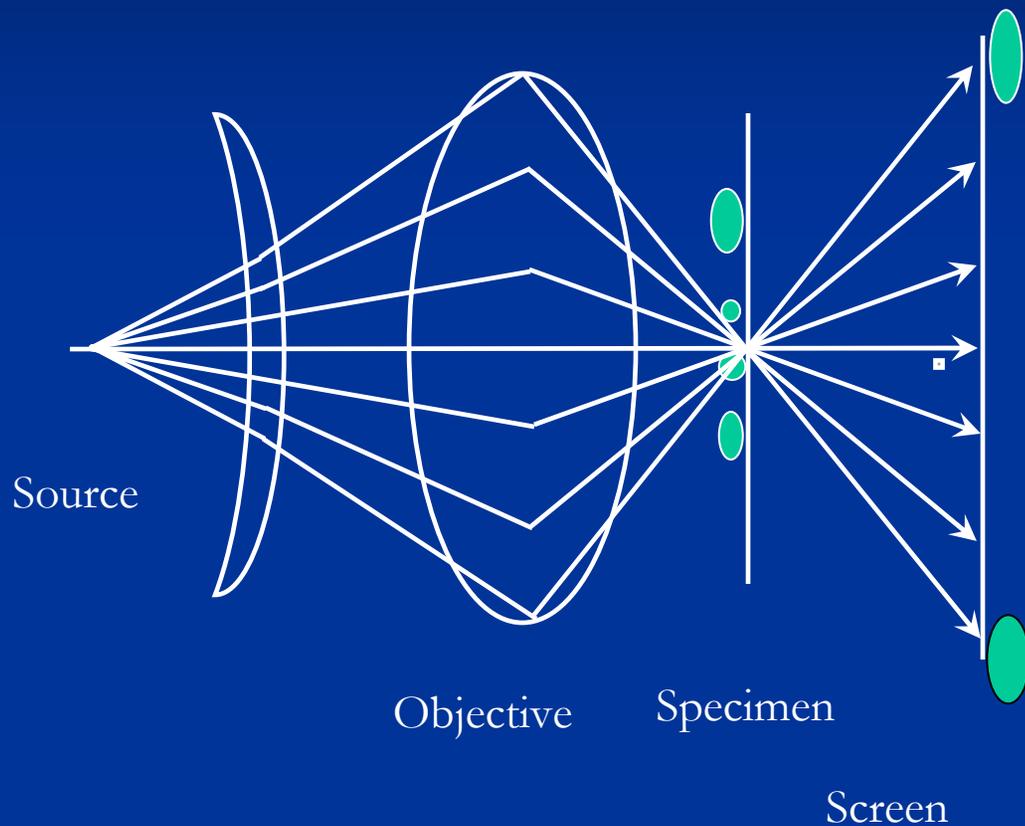


Shadow Map: “Ronchigram”



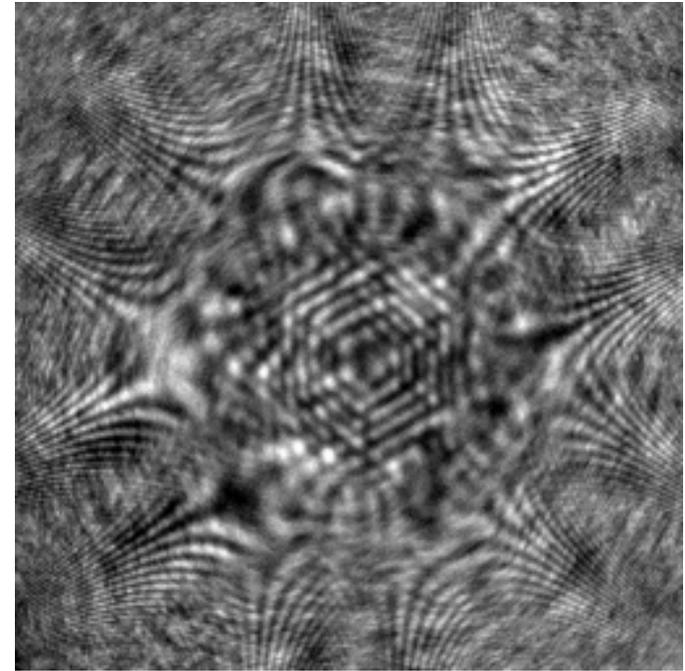
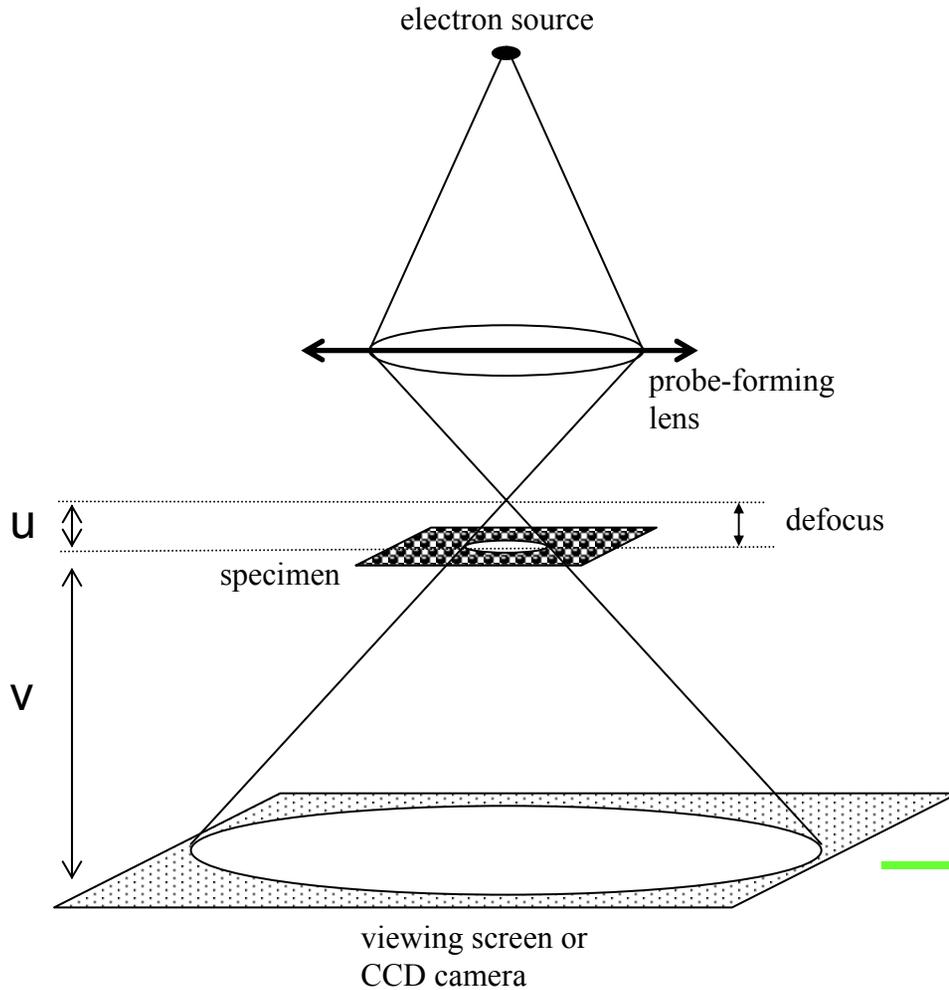
20 nm

Shadow Map: "Ronchigram"



50 nm

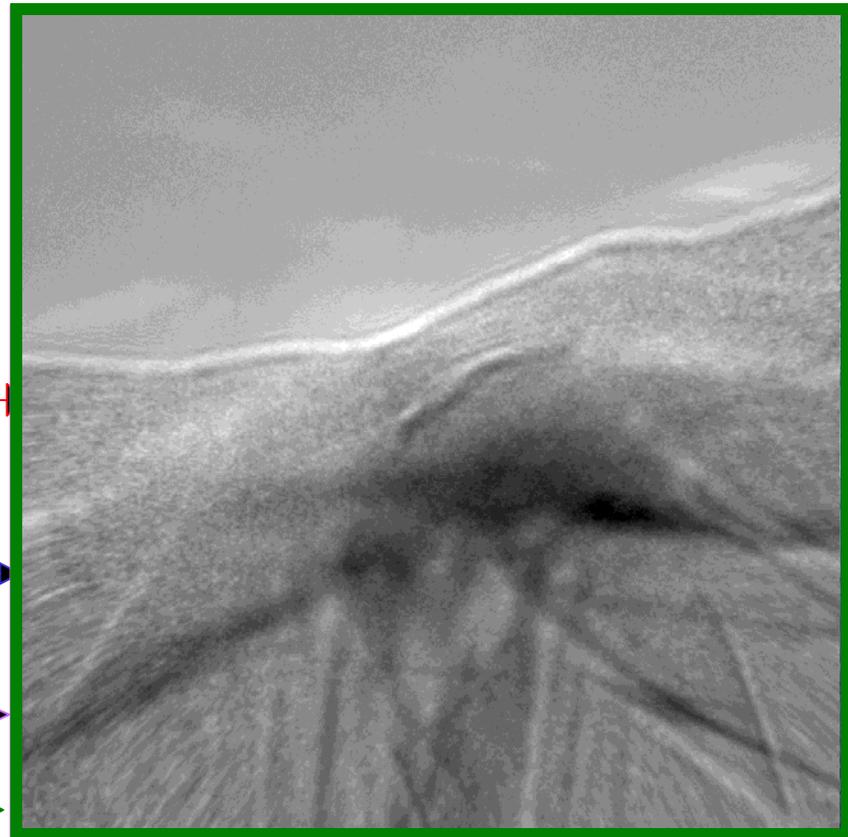
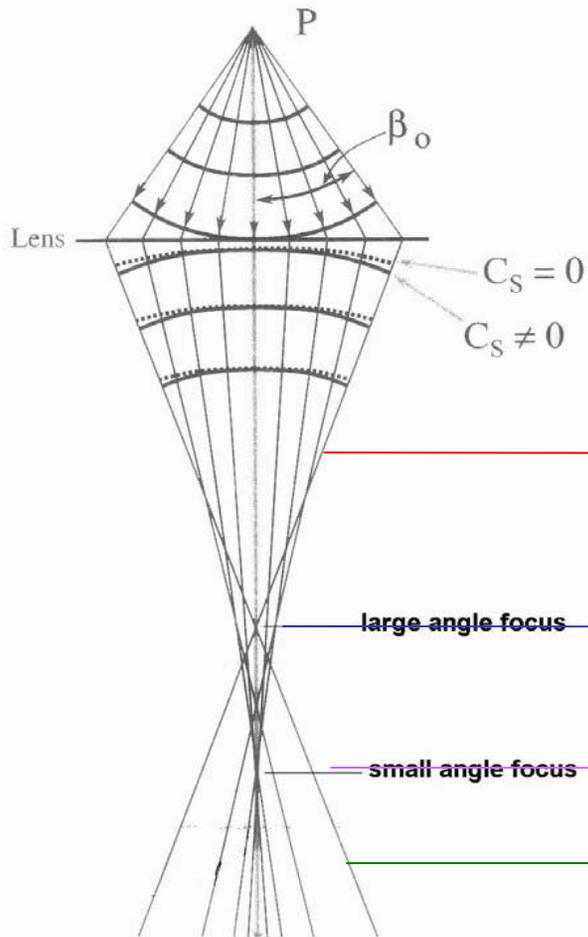
The Electron Ronchigram



$$M = \frac{v}{u}$$

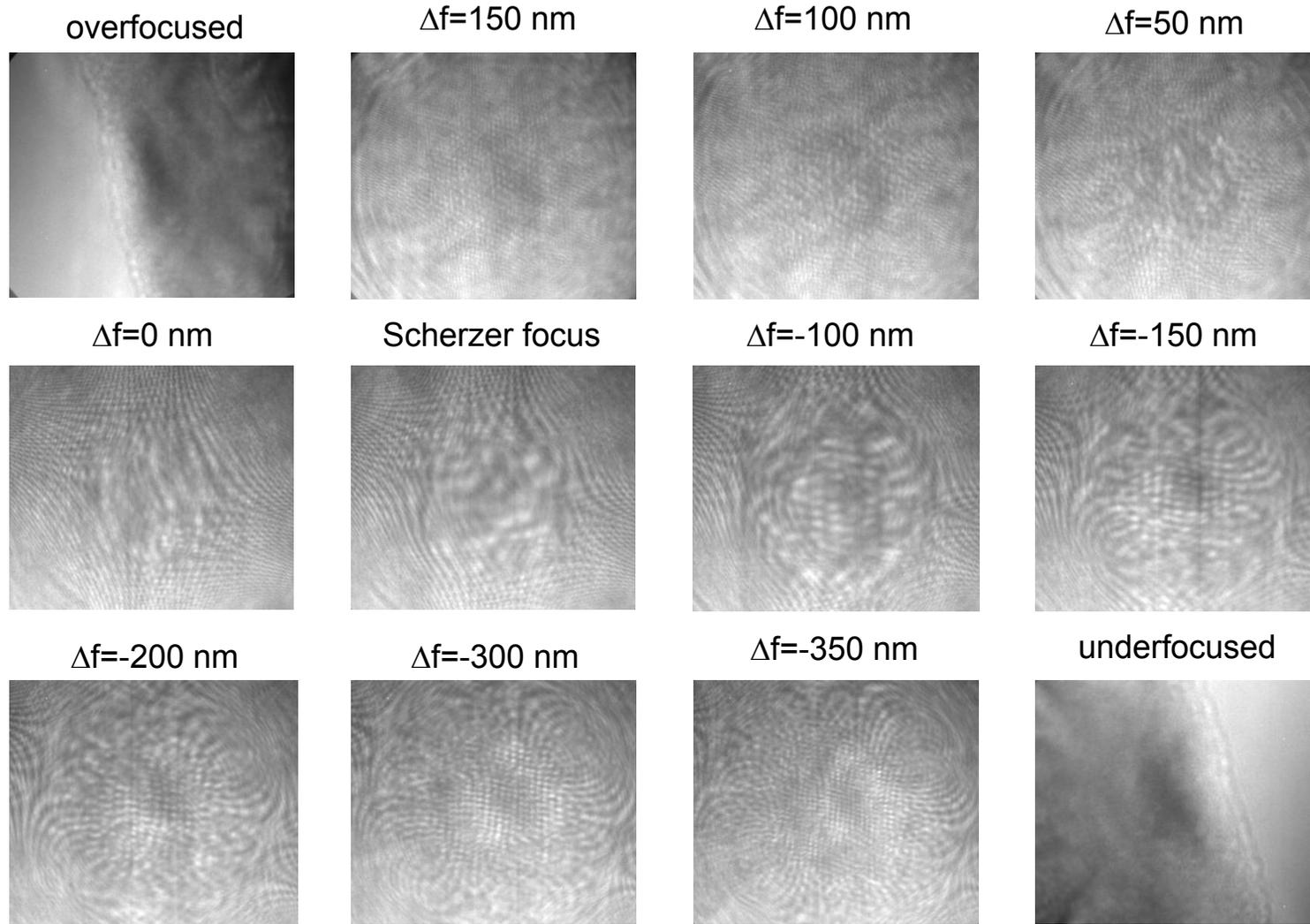
Cowley, *J. Elec Microsc Tech* 3, 25 (1986)

Effect of C_s on Ronchigram



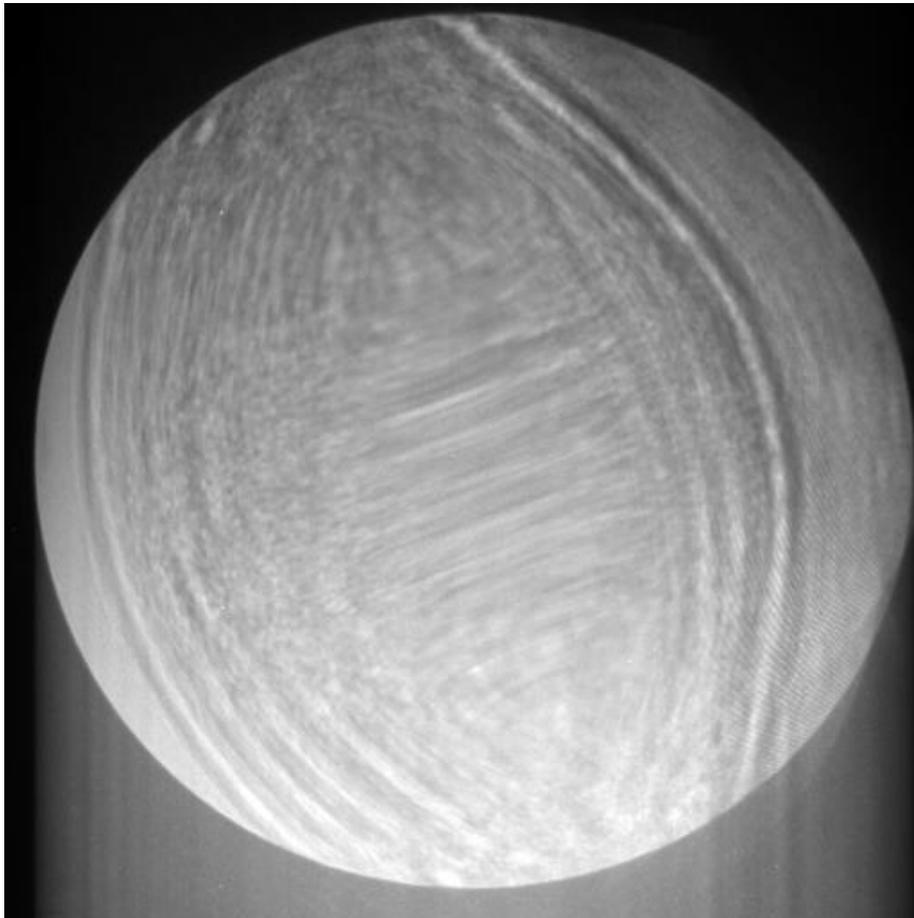
James and Browning, *Ultramicroscopy* **78**, 125 (1999)

Ronchigrams from Si $\langle 110 \rangle$

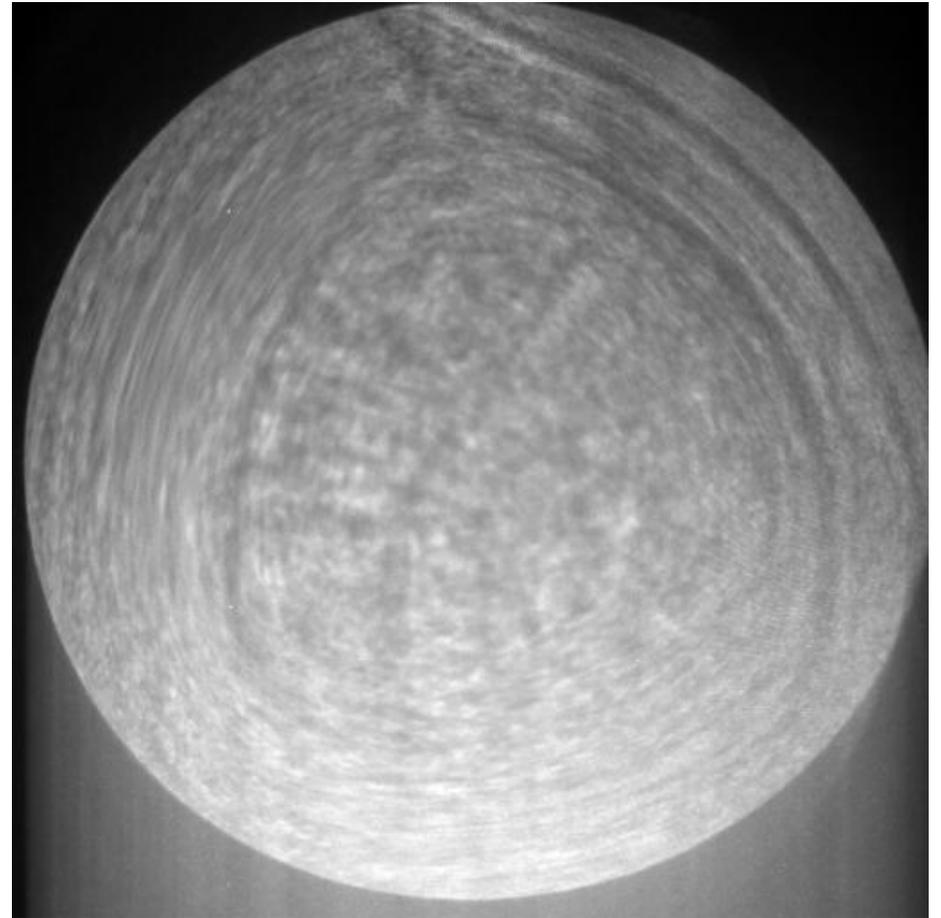


Correcting for Astigmatism

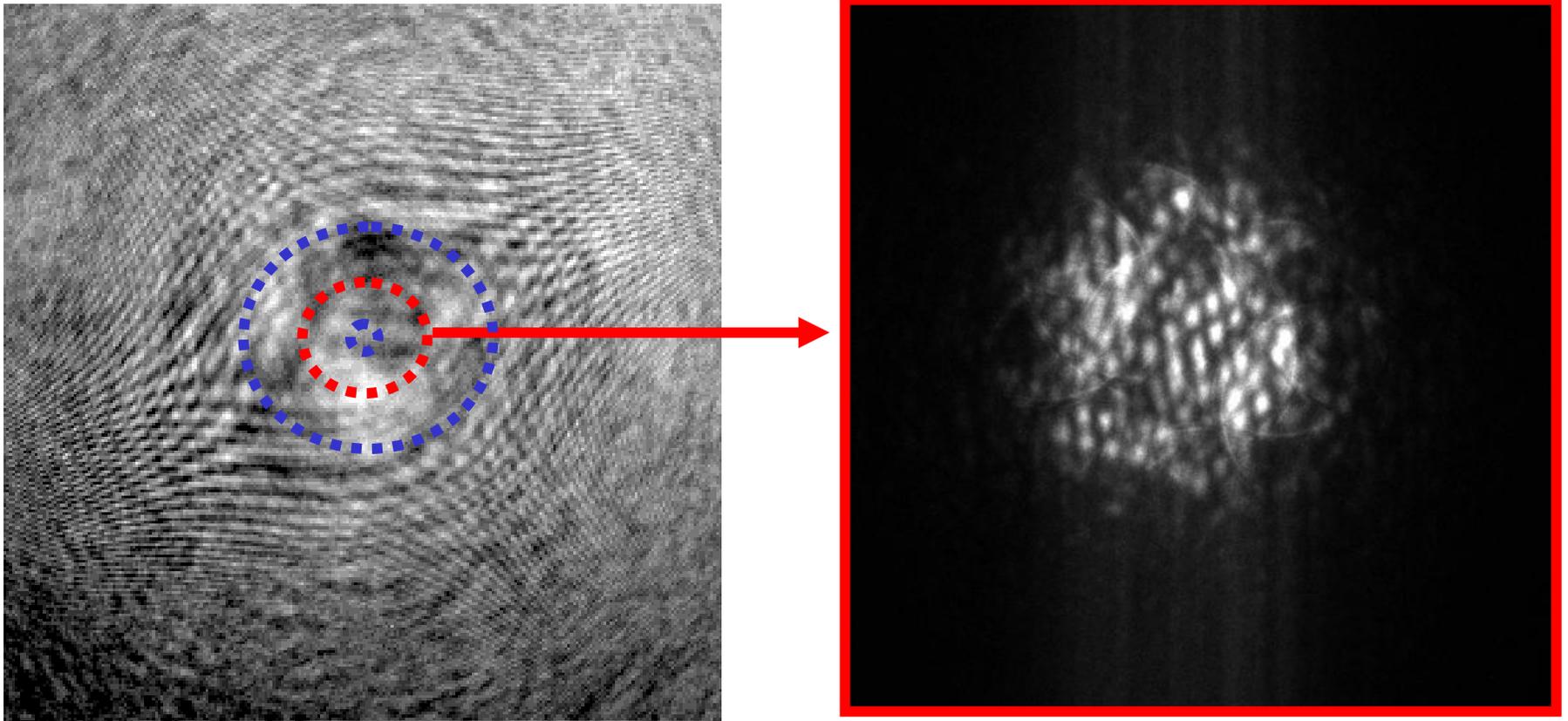
Two fold astigmatism



Three fold astigmatism

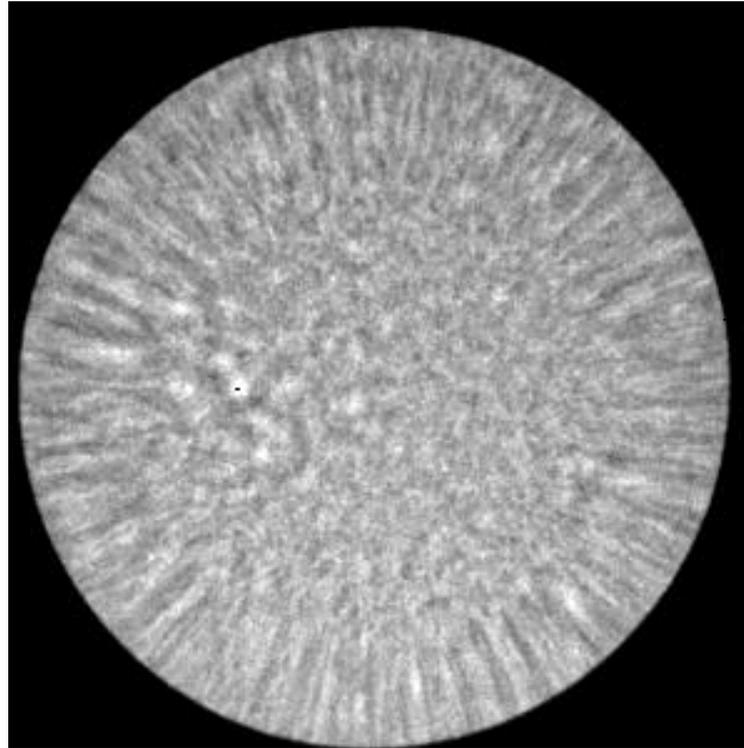


Forming the Smallest Probe

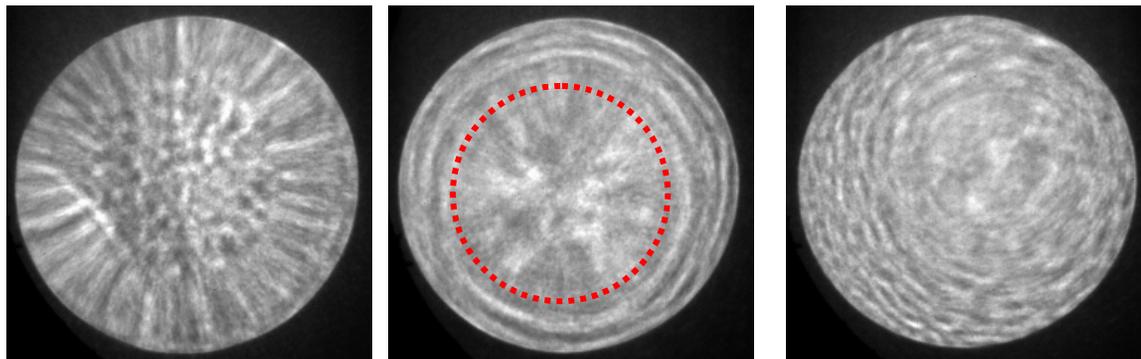


Put aperture over area of constant phase in Ronchigram to give CBED pattern

Ronchigram focus series on a-C



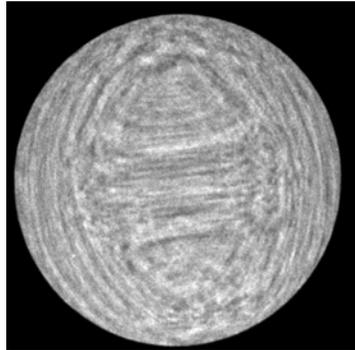
→ This aperture
Is too big



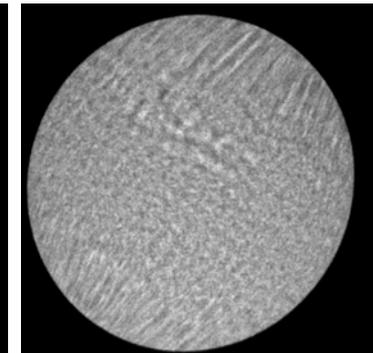
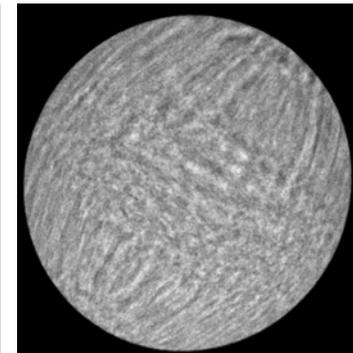
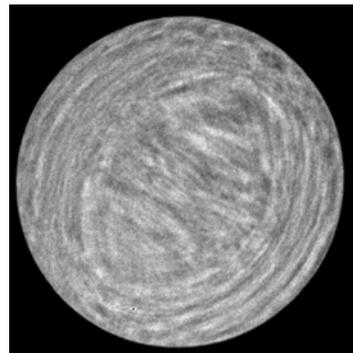
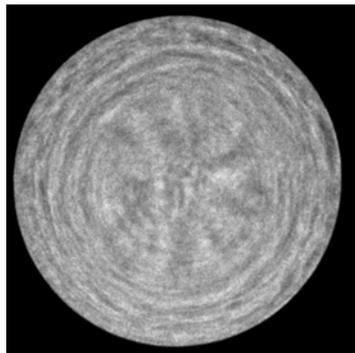
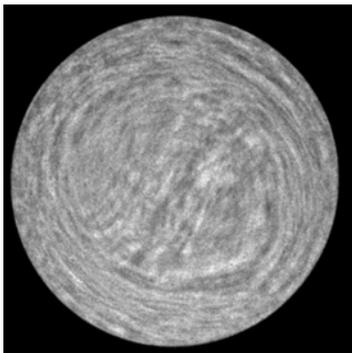
Correcting Severe Astigmatism in Ronchigrams



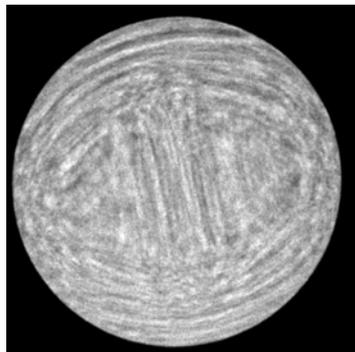
-y (don't image probe)



-X



+X

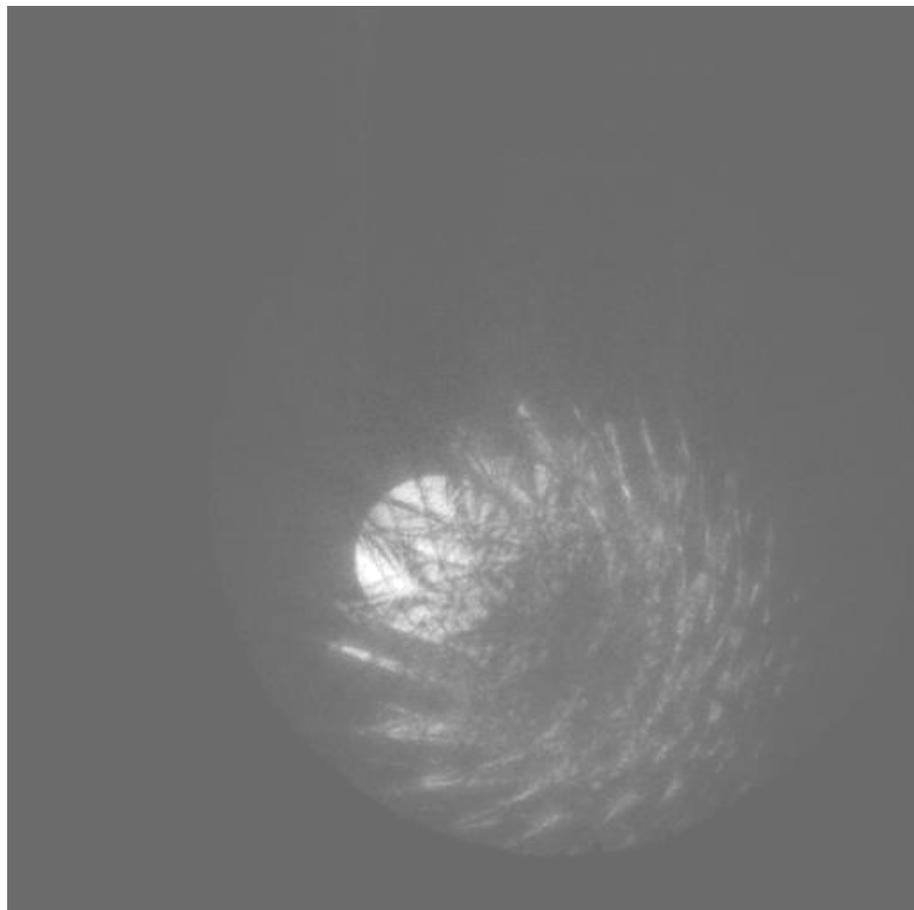


+y

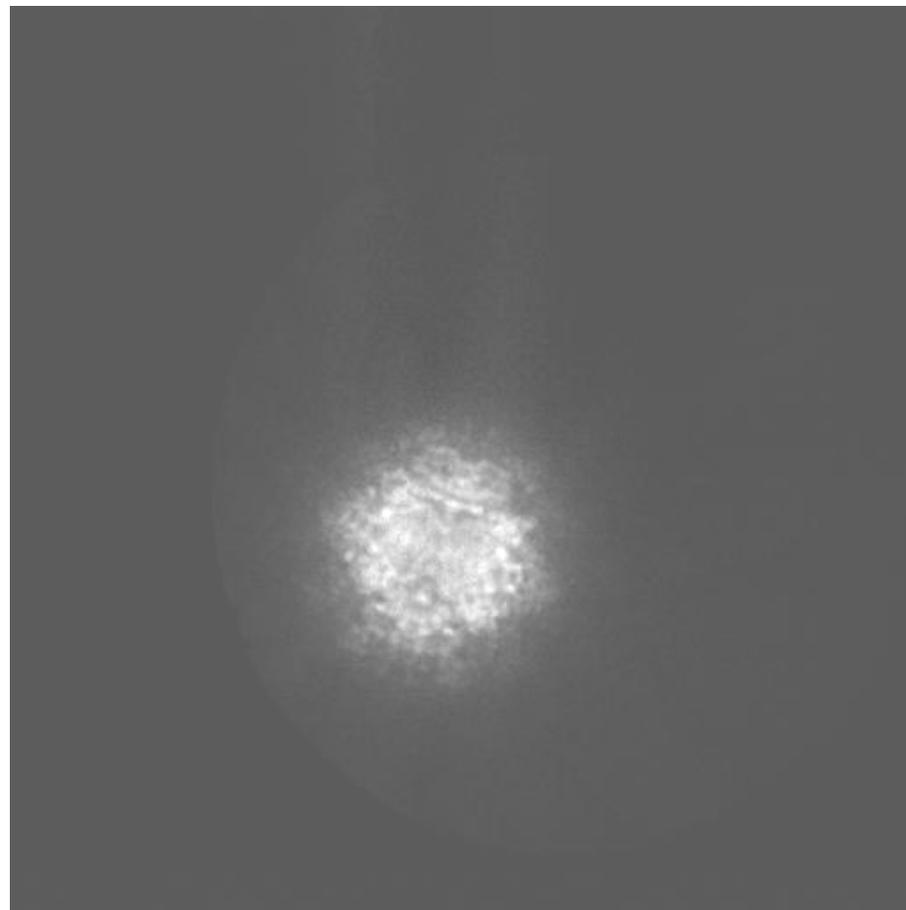
Ronchigrams on Crystals



Tilted

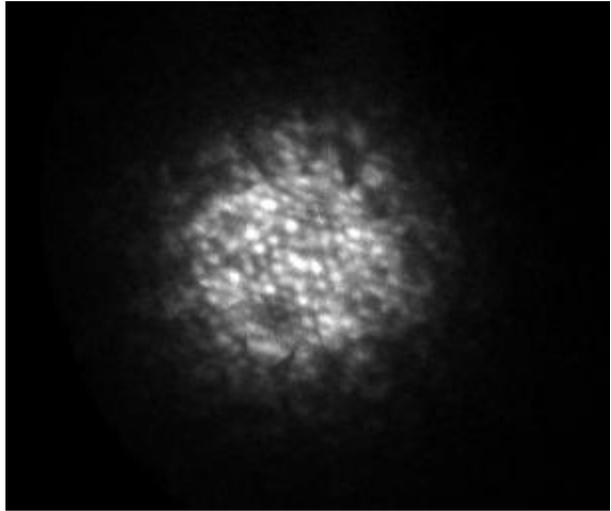


On Axis (not in focus)

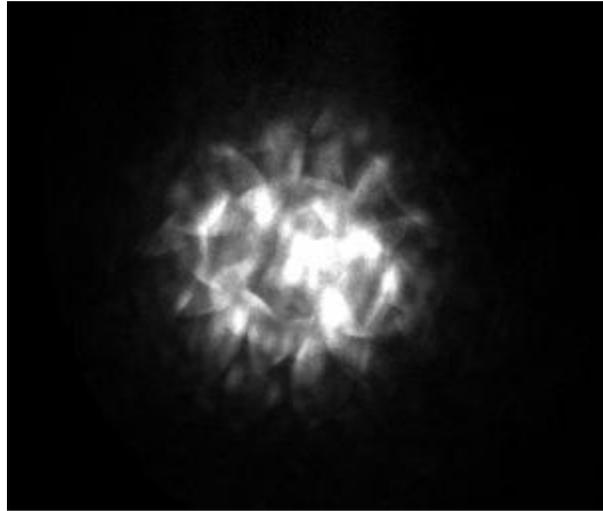


Ronchigrams on Crystals

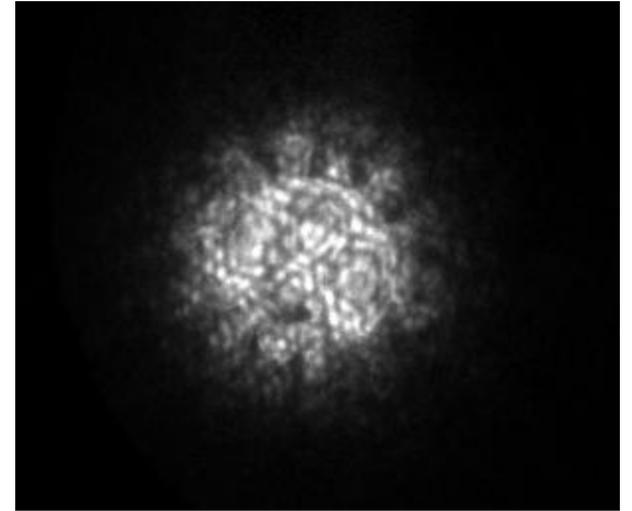
under



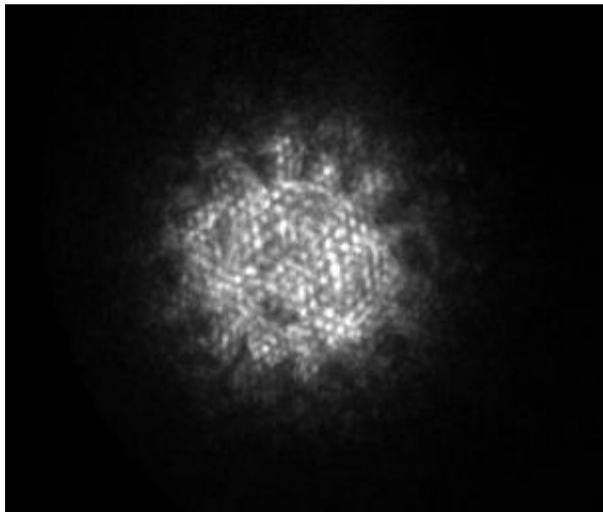
In focus



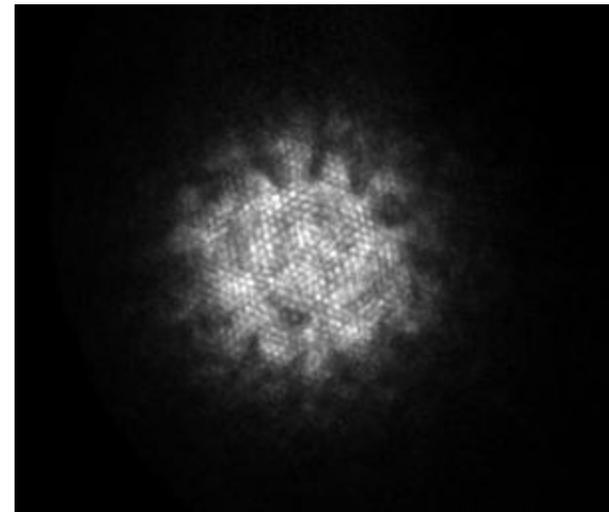
over



More over



way over

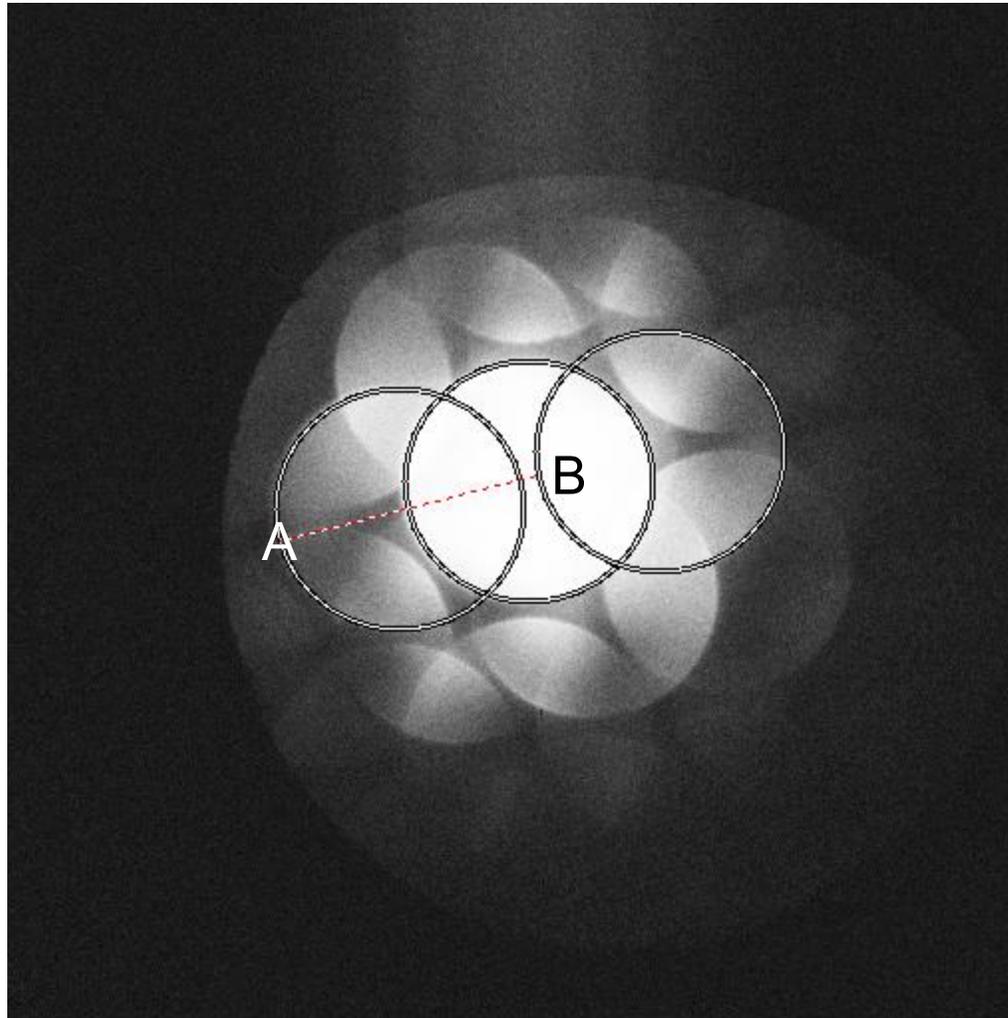


Measuring the Aperture Size

(Using [110] Silicon as a reference)



Scan the beam over a small area to remove ronchigram structure



Distance AB
Is 4 x Bragg Angle

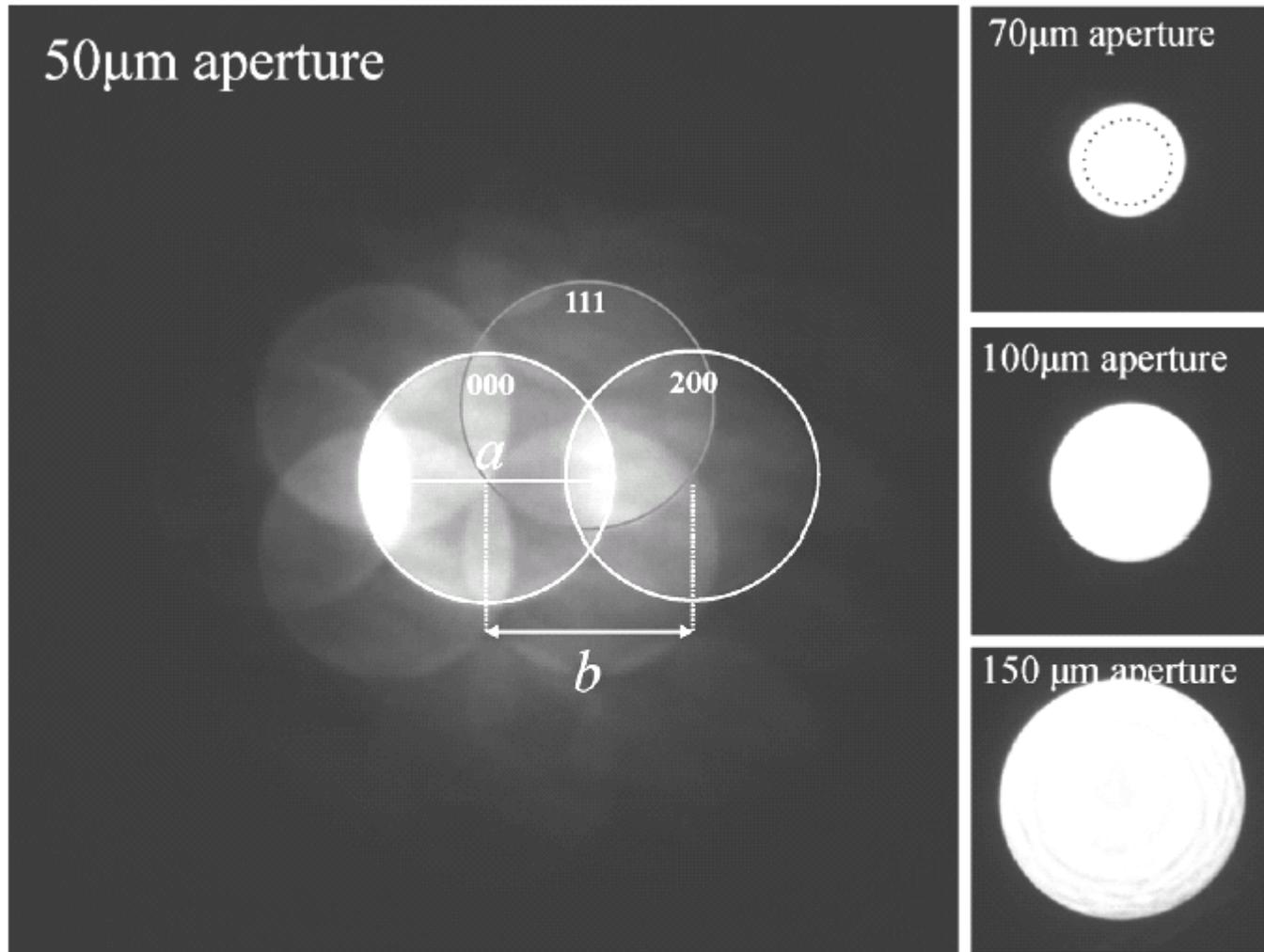


Figure 10. Measurement of STEM convergence angles in an FEI F20 SuperTWIN. The diffraction pattern is “calibrated” on the the 200 reflection of Si, oriented onto to the 110 axis. The convergence semi-angle (α) is proportional to the ratio of the disc width to the disc spacing (a/b). As b is independent of the chosen aperture the other three apertures can be calibrated by just recording the width of the zero order disk (a). The dotted line inside the 50 μm aperture represents the relative scale of the 50 μm aperture.

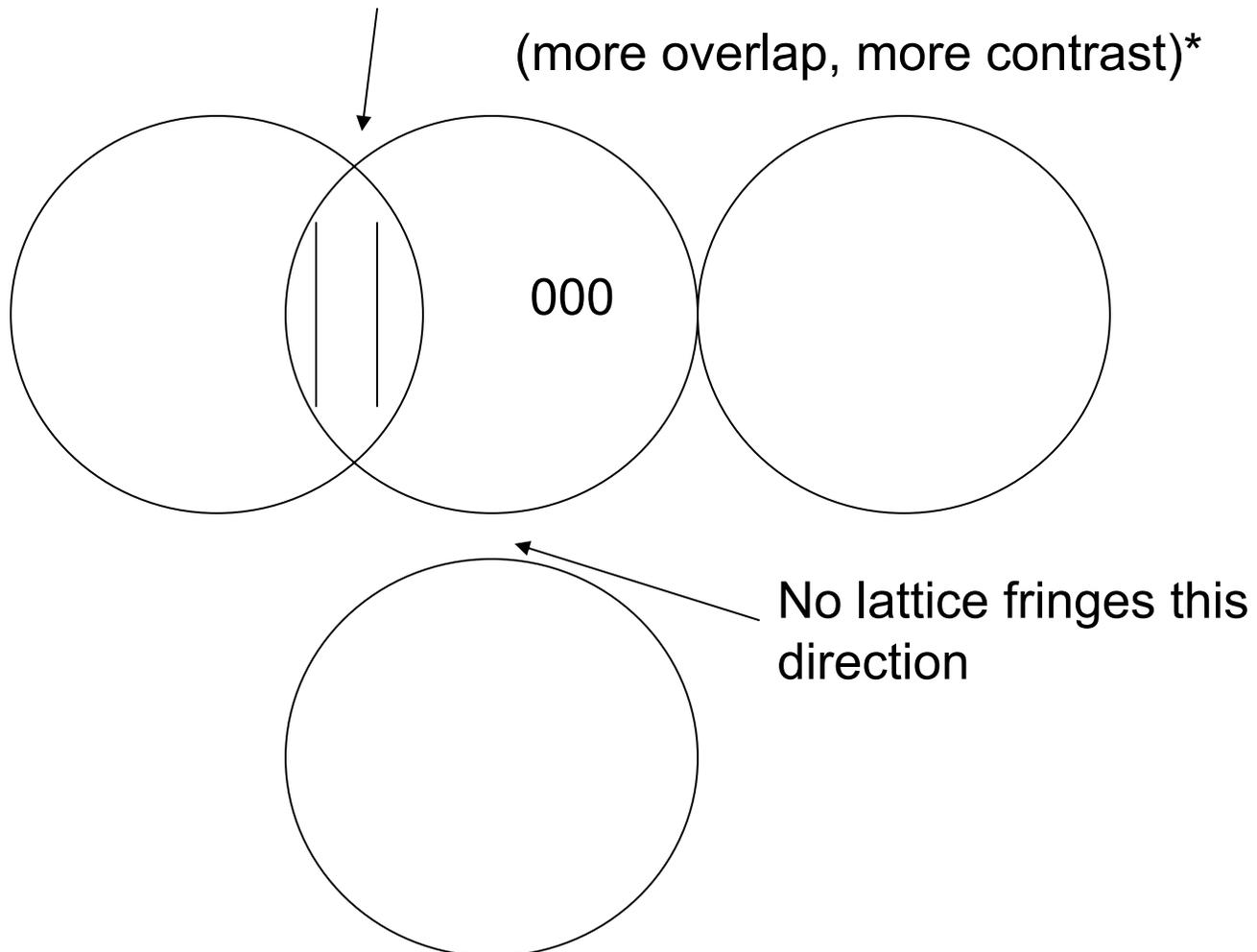
Reality Check

(Can I see a lattice spacing)



Disks must overlap to form a lattice fringe

(more overlap, more contrast)*



Balancing Spherical Aberration against the Diffraction Limit



(Less diffraction with a large aperture – must be balanced against C_s)

A more accurate wave-optical treatment, allowing less than $\lambda/4$ of phase shift across the lens gives

Minimum Spot size: $d_{\min} = 0.43 C_s^{1/4} \lambda^{3/4}$

Optimal aperture: $\alpha_{\text{opt}} = \left(\frac{4\lambda}{C_s} \right)^{1/4}$

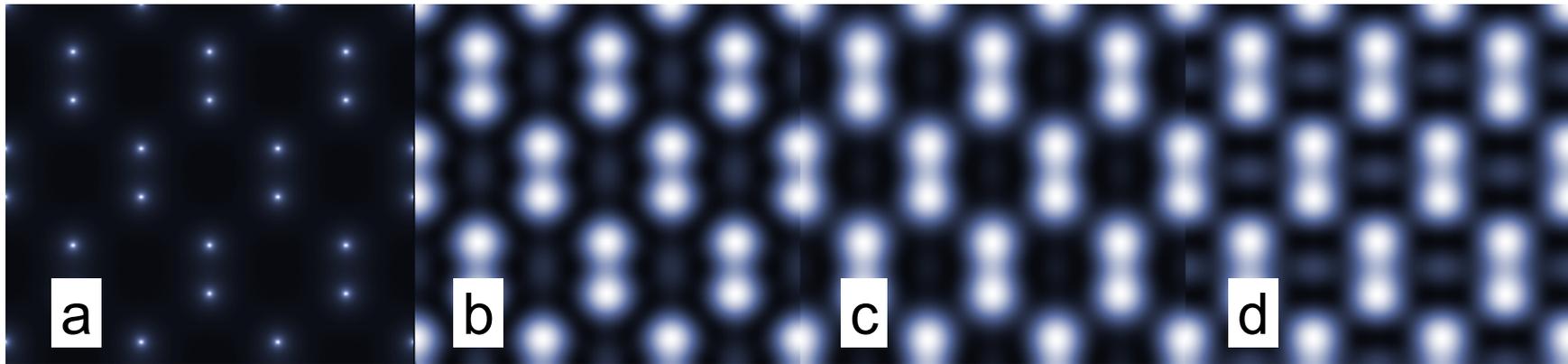
At 200 kV, $\lambda=0.0257 \text{ \AA}$, $C_s = 1.0 \text{ mm}$, $d_{\min} = 1.55 \text{ \AA}$ and $\alpha_{\text{opt}} = 10 \text{ mrad}$
 $C_s = 1.2 \text{ mm}$, $d_{\min} = 1.59 \text{ \AA}$ and $\alpha_{\text{opt}} = 9.6 \text{ mrad}$

$C_s = 0.5 \text{ mm}$, $d_{\min} = 1.28 \text{ \AA}$ and $\alpha_{\text{opt}} = 12 \text{ mrad}$
 $C_s = 0.6 \text{ mm}$, $d_{\min} = 1.34 \text{ \AA}$ and $\alpha_{\text{opt}} = 11 \text{ mrad}$

Multislice simulated Annular-Dark-Field Images of Silicon [110] in a 200 kV STEM



(Cs=0.5 mm, Probe forming aperture=11.9 mr, ADF inner angle=30 mr)



- (a) The projected potential along [110]
- (b) The ADF image for a 2.7 Å thick crystal
- (c) The ADF image for a 81 Å thick crystal
- (d) The ADF image for a 2.7 Å thick crystal (1.6 Å information limit)

Note: (i) The dumbbells are visible even when the (400) spot is excluded
(ii) Except the dumbbell spacing is not 1.36Å, but closer to 1.6Å

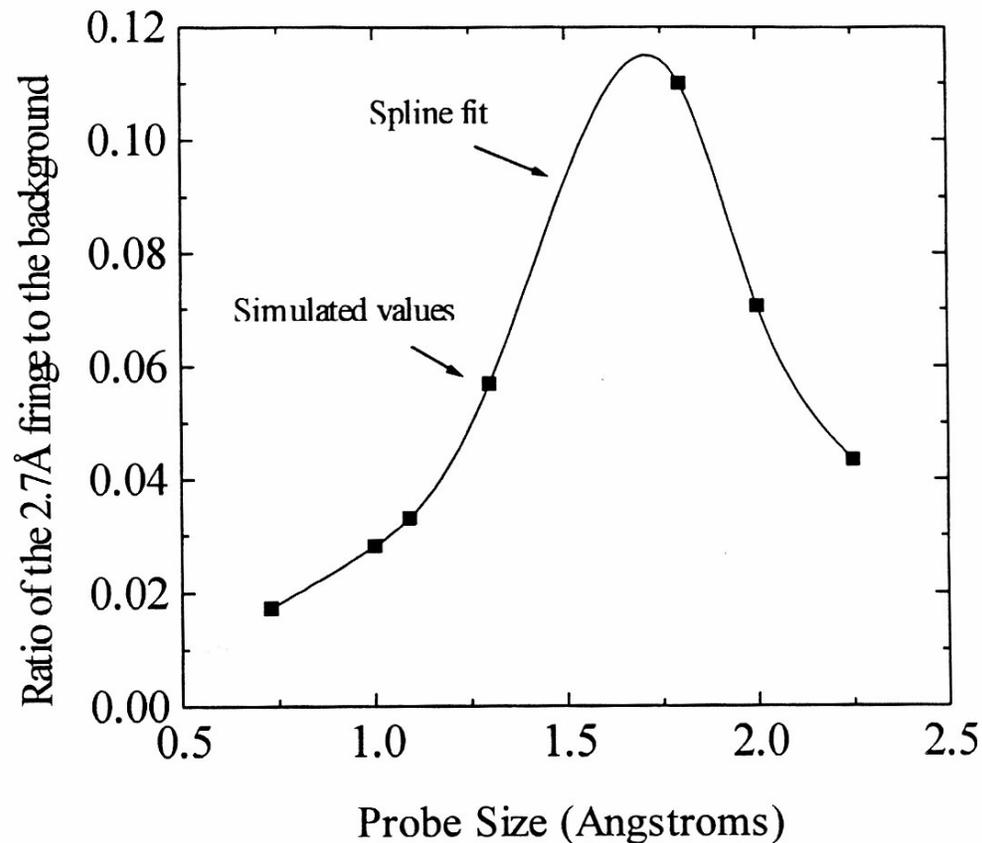


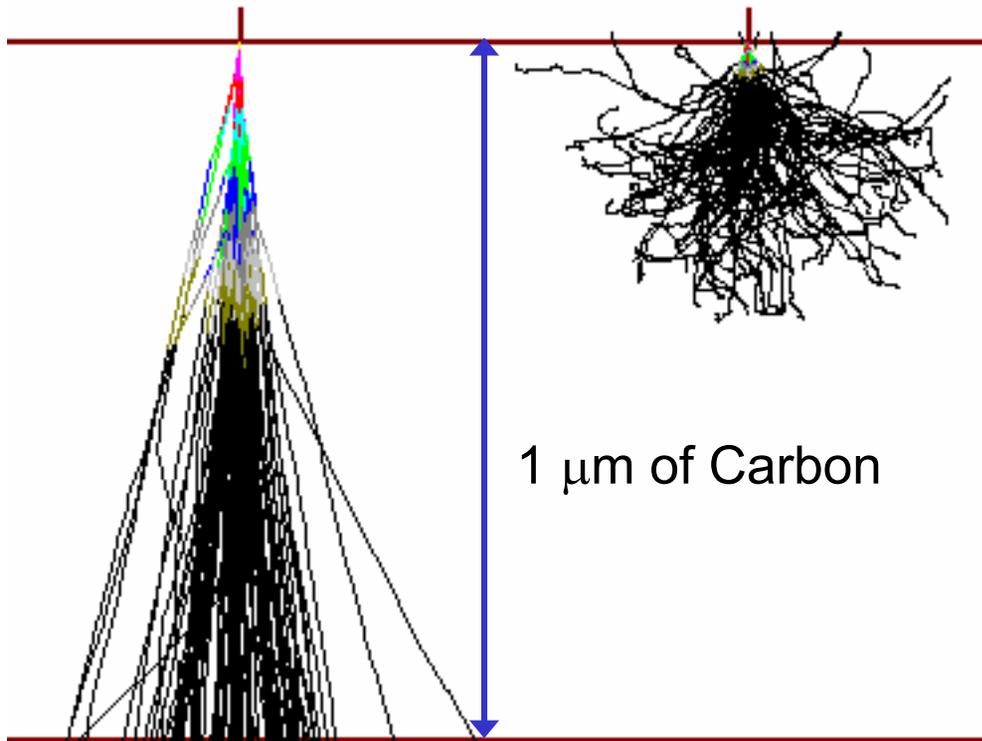
Figure 3.17: Simulated strength of 2.7 Å fringe (normalized with respect to overall linescan intensity) in 190 Å of Si (110) versus nominal probe size. For large probe sizes the fringe is beyond the resolution and is not visible, for small probes there is no 'crosstalk' between the atomic columns located 1.36 Å apart and the 'forbidden' fringe is again not visible.



Beam Spreading

$E_0=200$ keV

$E_0=20$ keV



Electron Range (in μ m):

$$R \approx \frac{0.064}{\rho} E_0^{1.5}$$

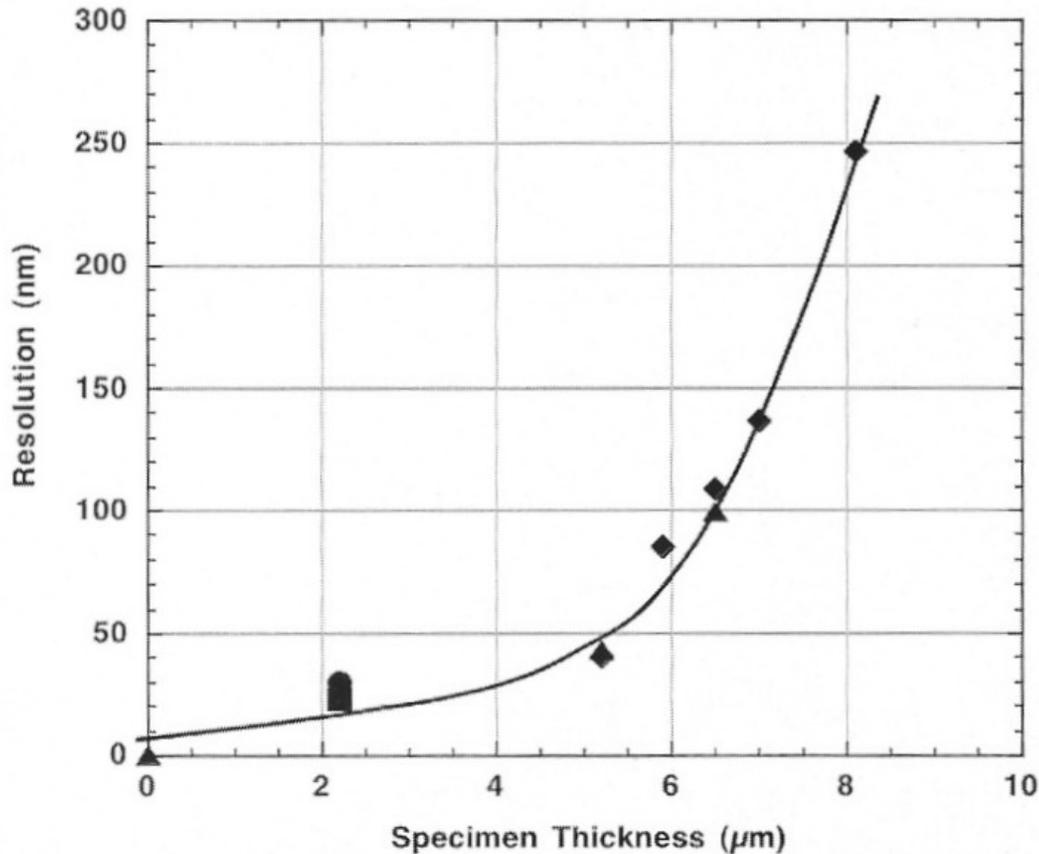
(density ρ in g/cm^3 , E_0 in keV)

$R \sim 100 \mu\text{m}$ at 200 keV



Beam Spreading

At 300 kV



$$\text{Beam Spreading} \propto \frac{(Zt)^{1.5}}{E_0}$$

At 100 kV

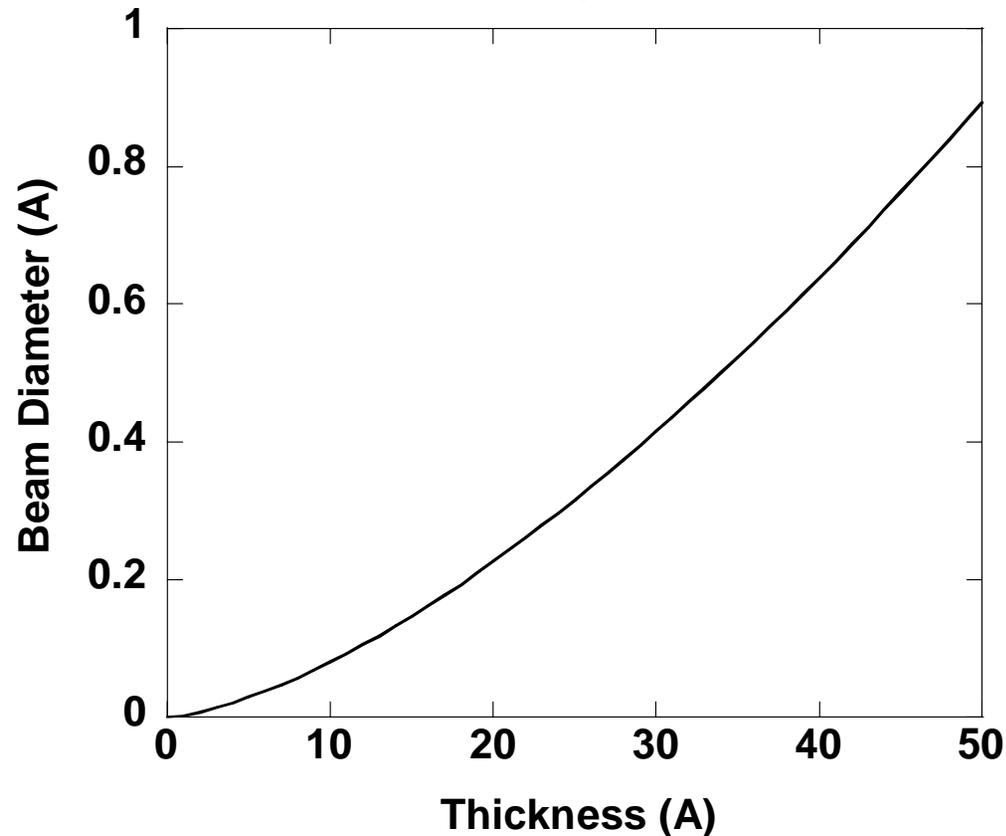
0.16 nm for 10 nm thick C
1.8 nm for 50 nm thick C

N. Zaluzec, Microscopy Today (2004)

How does an amorphous layer on the entrance surface degrade resolution?



Beam Broadening in a-Si at 100kV

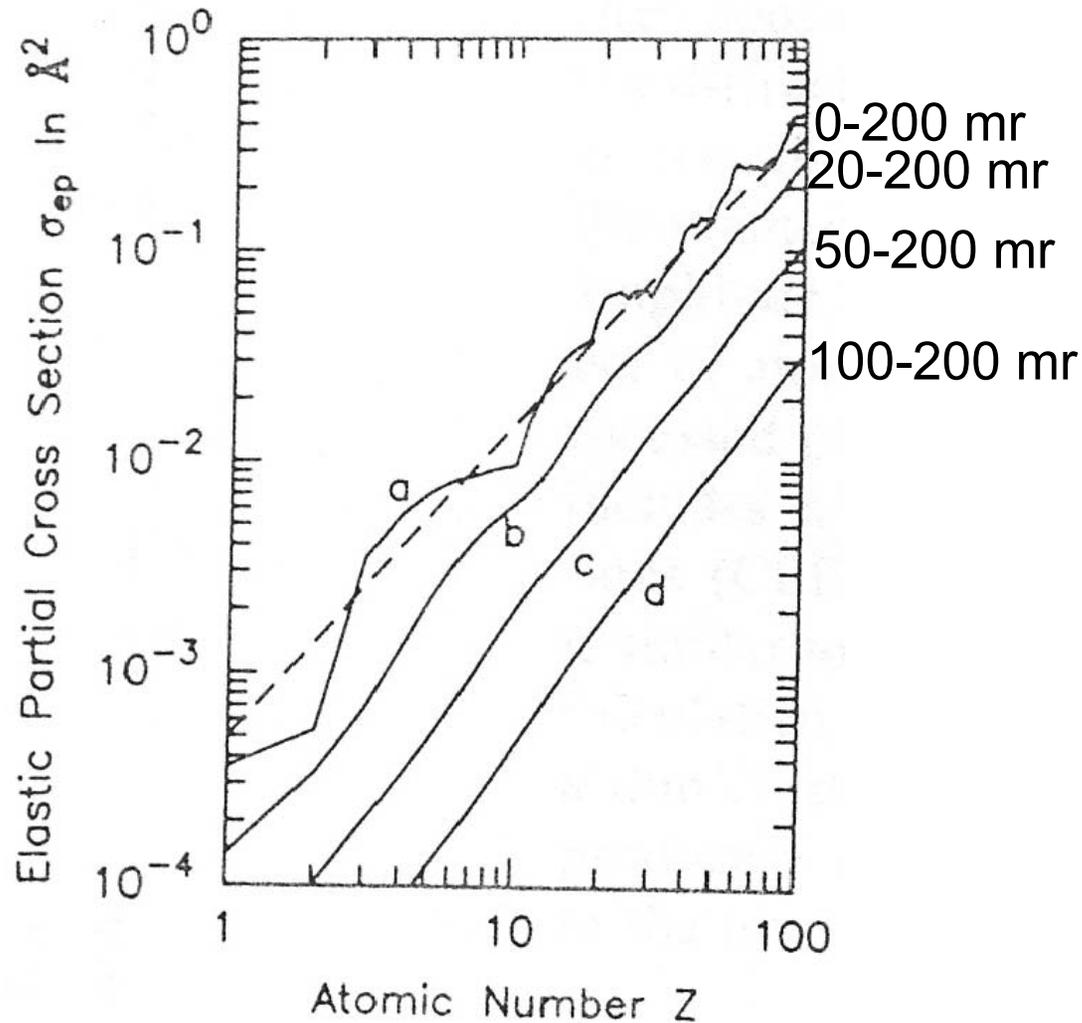


Increased Apparent Source size \Rightarrow Loss of resolution, loss of apparent brightness

•No FIB'ed samples!

•Ignore for probes larger than 0.4Å

Phase vs. ADF Contrast



ADF Signal is much weaker than HR-TEM

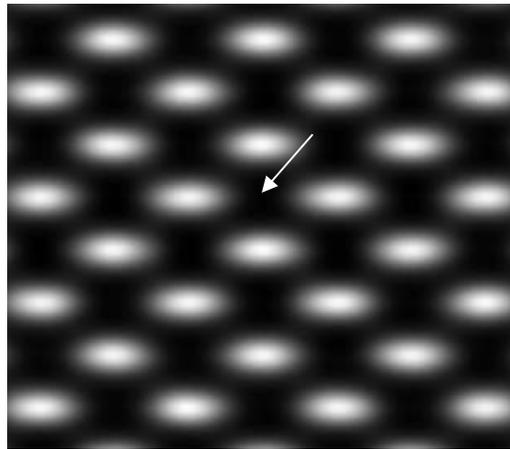
E. J. Kirkland et al, Acta Cryst, 1987

Imaging a Single Antimony Atom in 4.5 nm of Silicon

(the atom is 2.1 nm from the top surface)

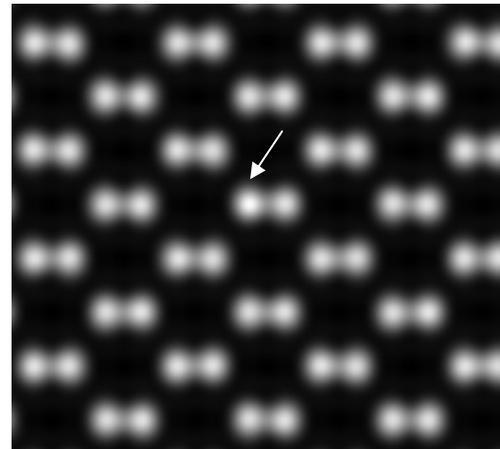


HRTEM



$C_s = 0.5$ mm
(JEOL 2010F URP)

Exit Wave Reconstruction



$C_s = 0$ mm
0.75 Å information limit

ADF-STEM



$C_s = 0.5$ mm
(JEOL 2010F URP)

Multislice simulations assume a 200 kV electron beam

Sb contrast: HRTEM 0%, EWR: 10% (5% at 1.2Å), ADF-STEM:65%

Why do we get more signal in ADF? Channeling!

ADF in Thicker Samples



- *Simple specimen transmission function model:*

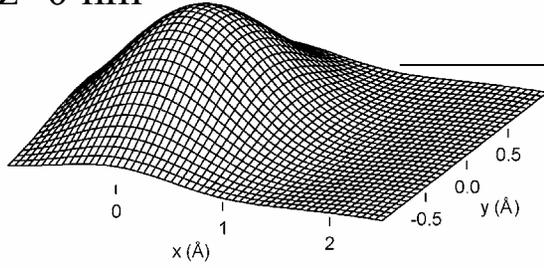
$$I_{ADF} \sim |h|^2 \otimes |t|^2$$

- Suggests that wave amplitude is important, not phase as in conventional HRTEM
- Interaction of the fast electrons with the periodic lattice including phonons is difficult
- Numerical simulations

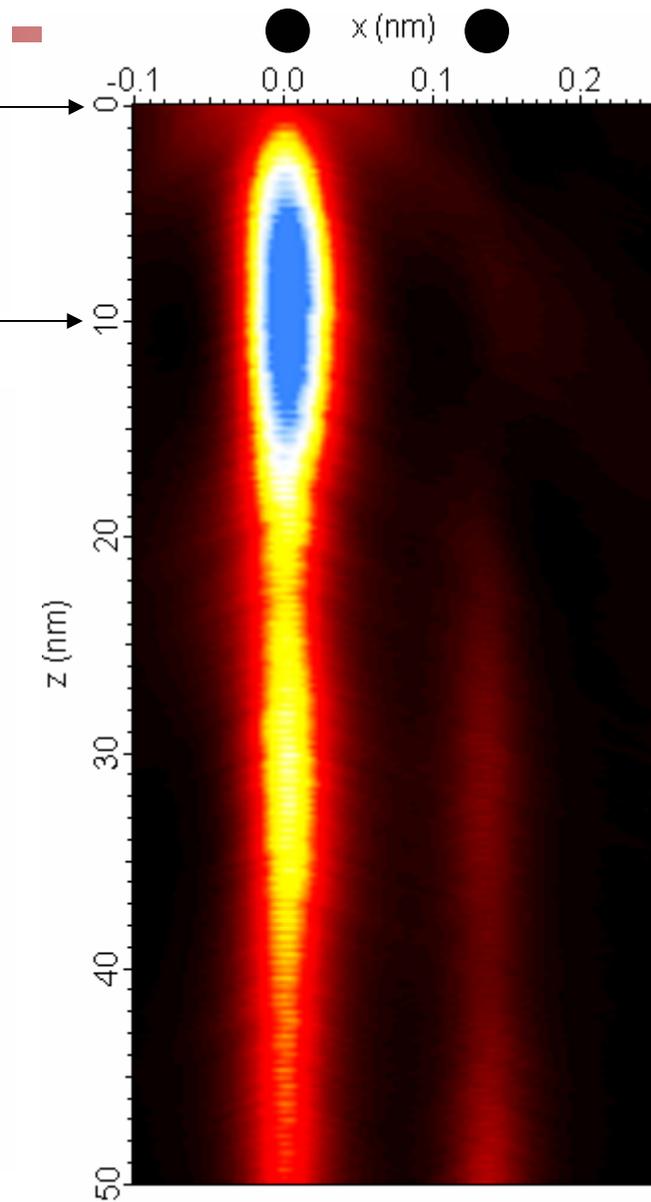
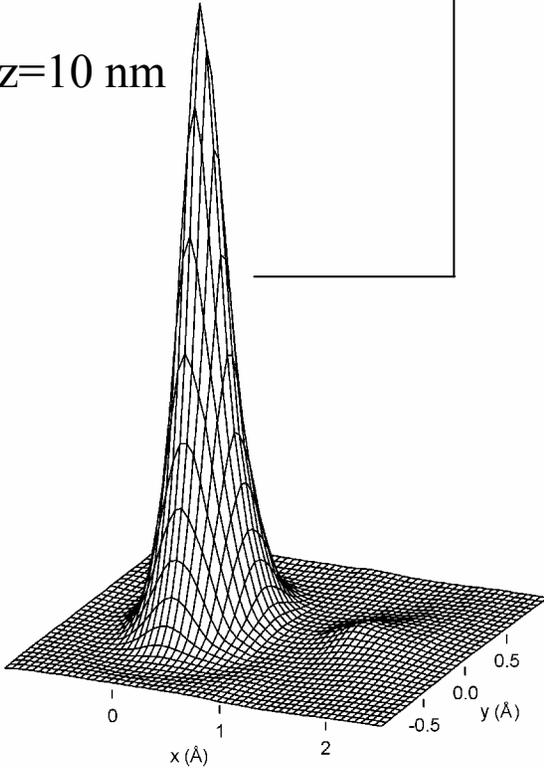
Probe Channeling



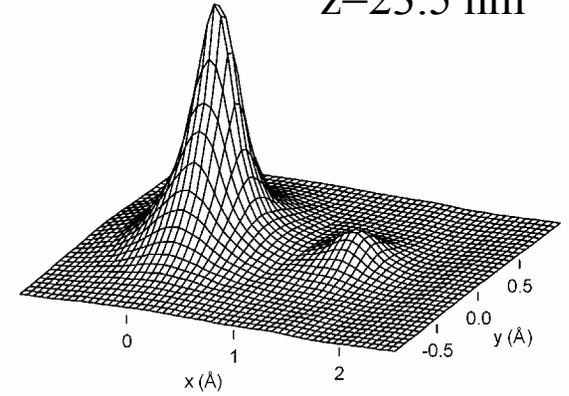
$z=0$ nm



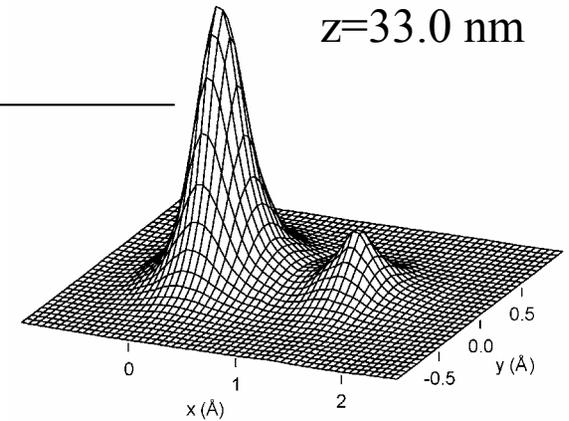
$z=10$ nm



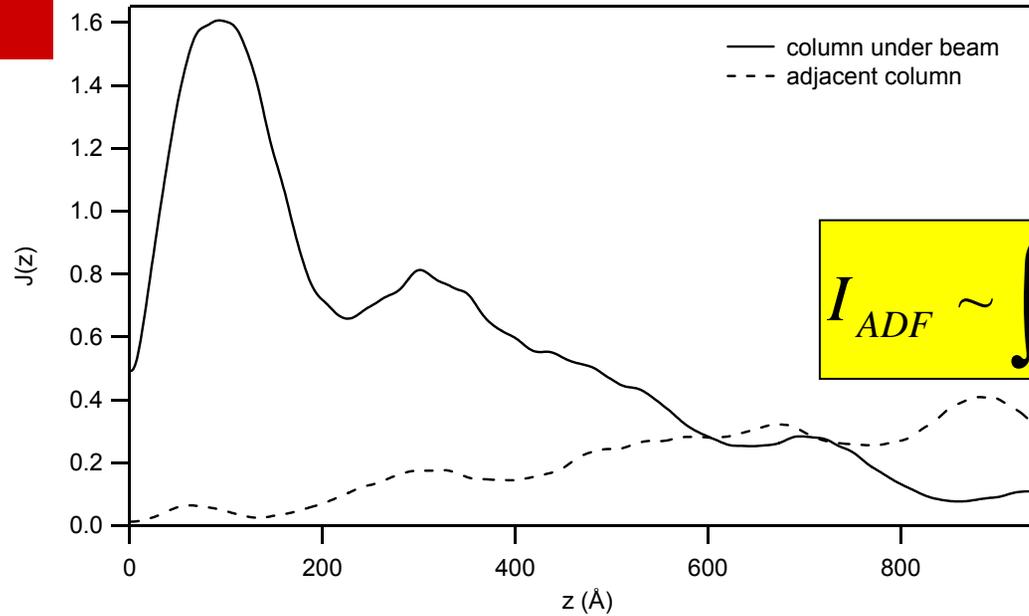
$z=23.5$ nm



$z=33.0$ nm

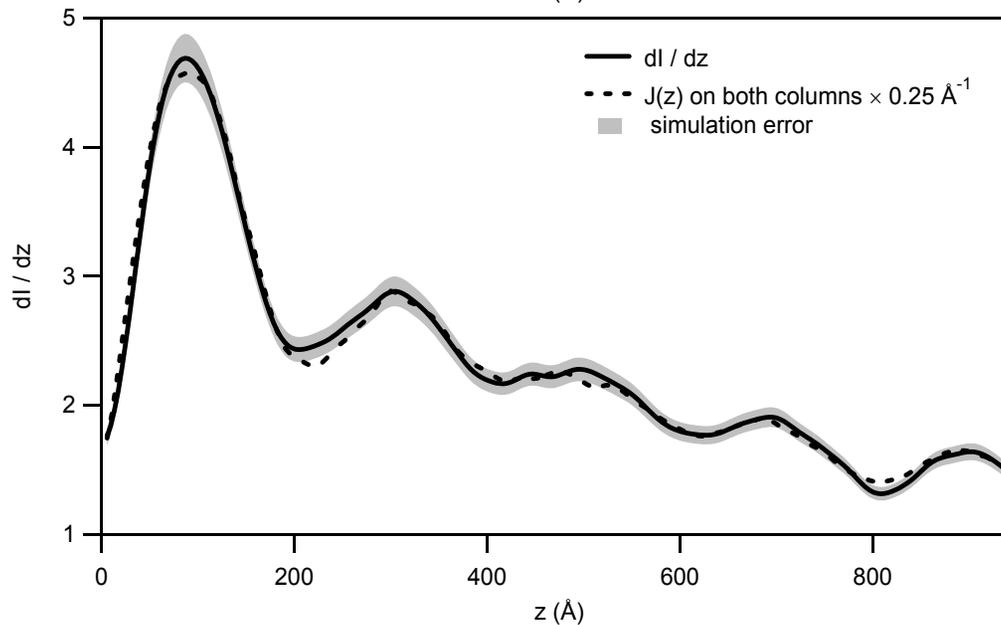


ADF Signal tracks Probe Amplitude

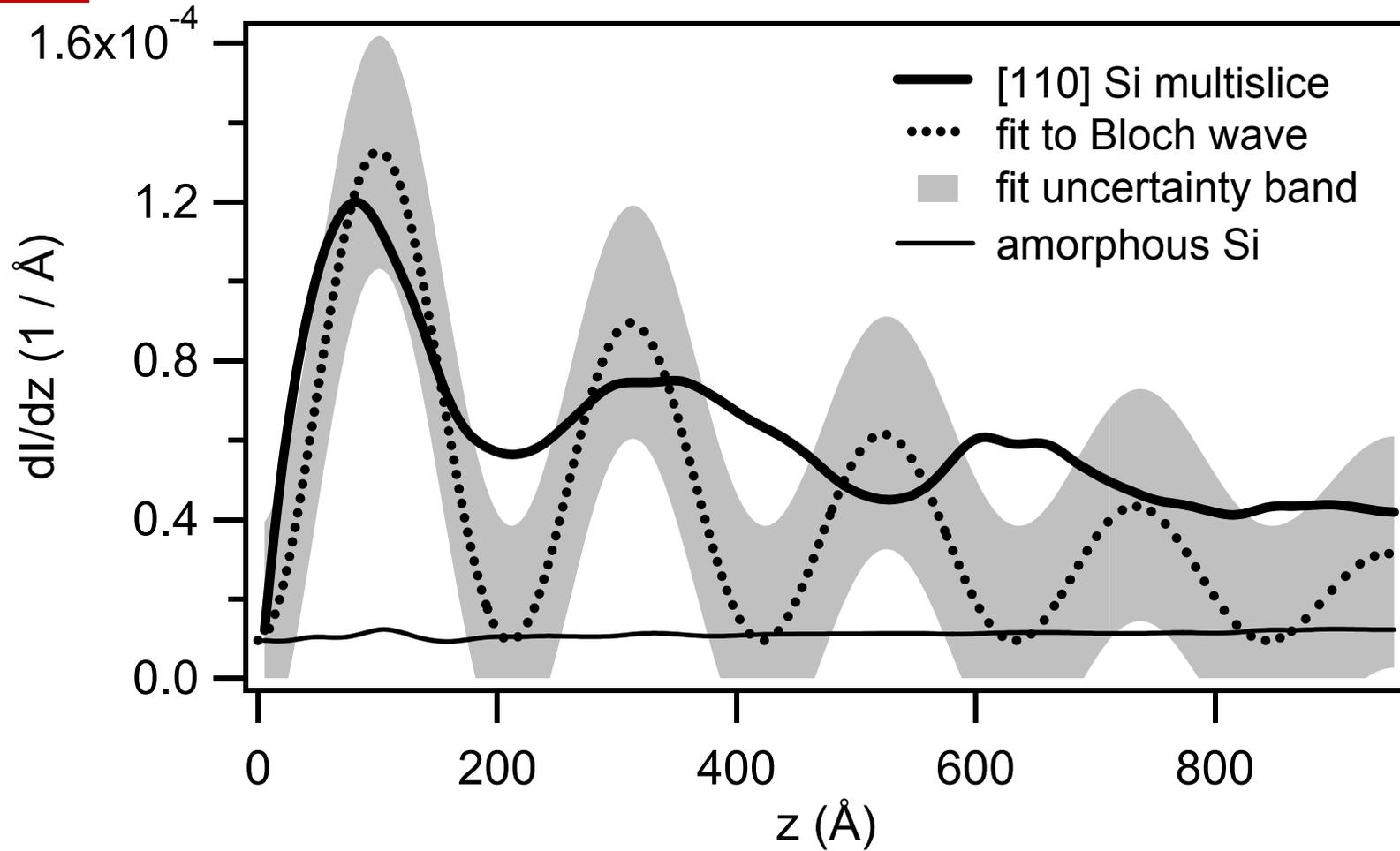


Si [110] at 300K
(200 kV, $C_s=1$ mm)

$$I_{ADF} \sim \int_0^{z_0} |h(\vec{r}, z)|^2 \otimes_r |t(\vec{r}, z)|^2 dz$$



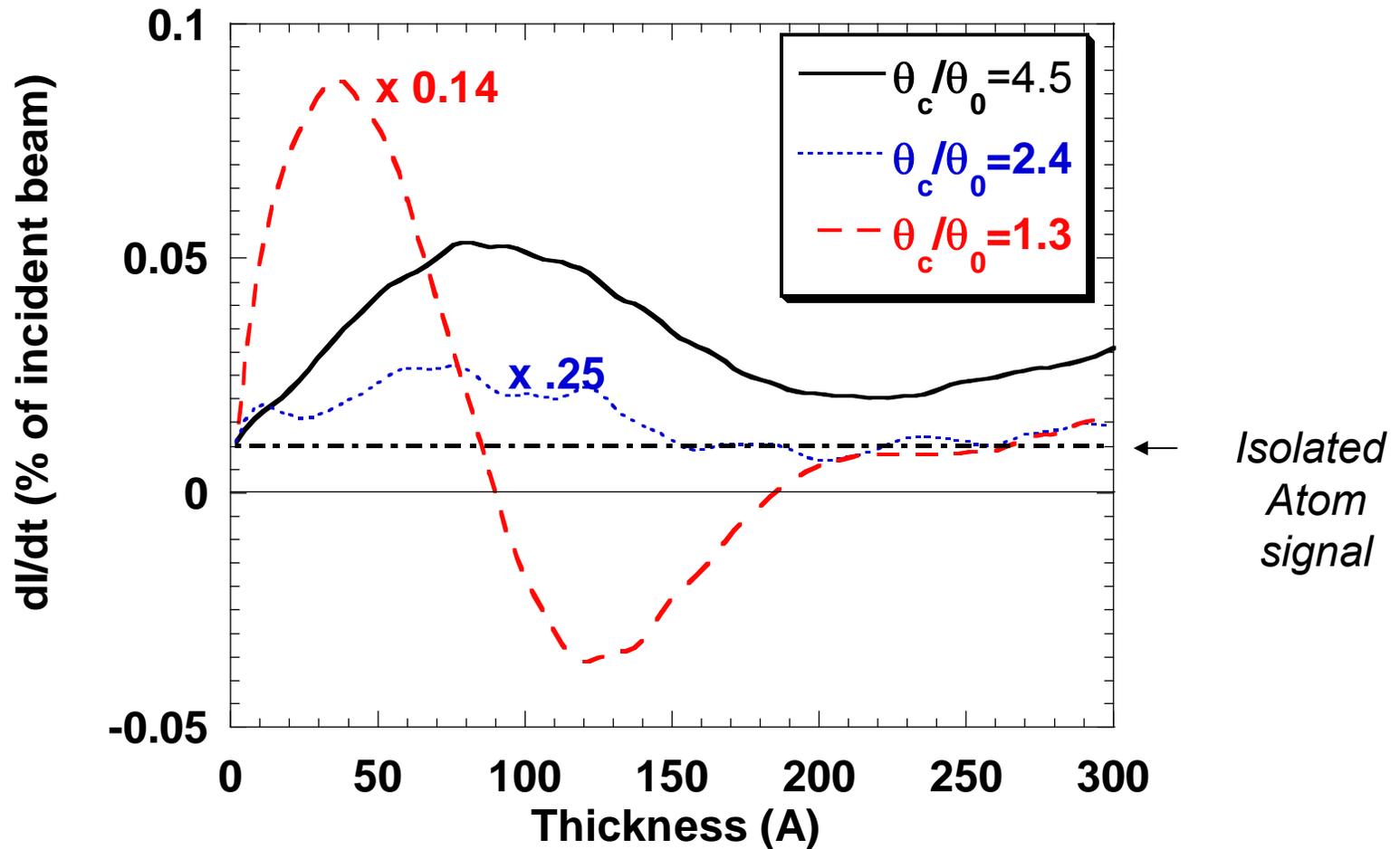
Channeling down



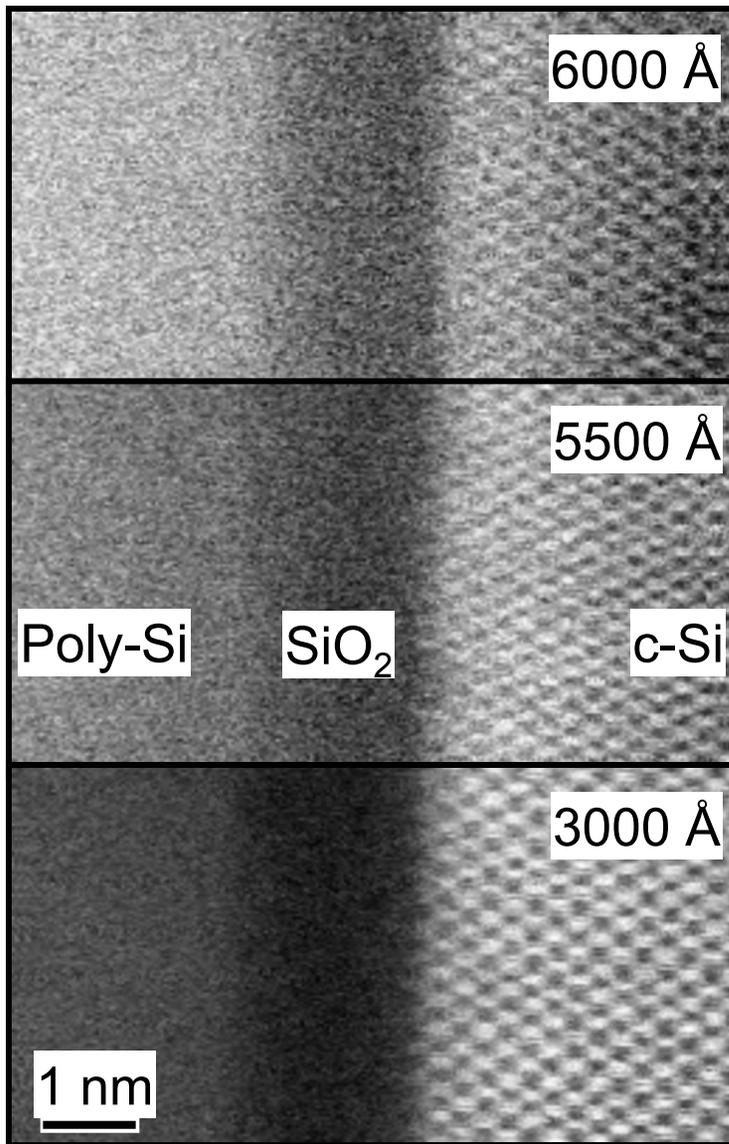
Signal vs Collection Angle



[011]Si, 300 kV, 9 mr probe angle



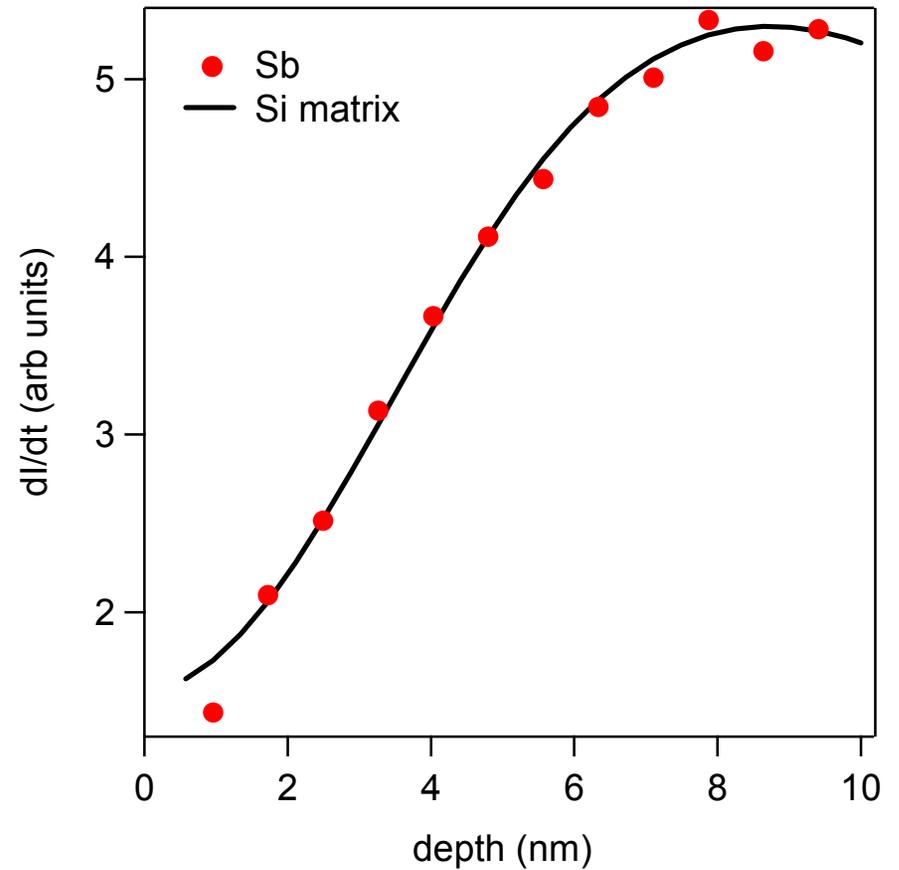
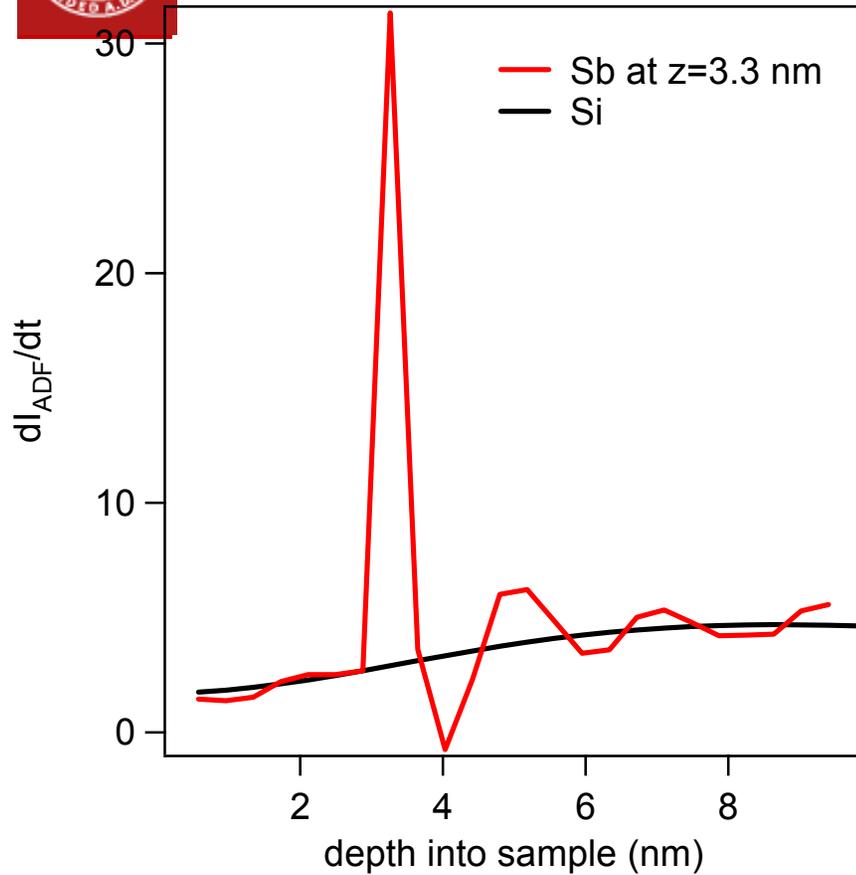
Imaging Thick Cross-Sections



- ADF Images decay gracefully with increasing thickness
- Apparent Oxide Thickness is unchanged with thickness
- Apparent Interface Roughness increases from 1.6 to 2.7 Å rms
- “white band” develops (depends on thickness and ADF angles)

Gate Oxide Thickness: 20 Å

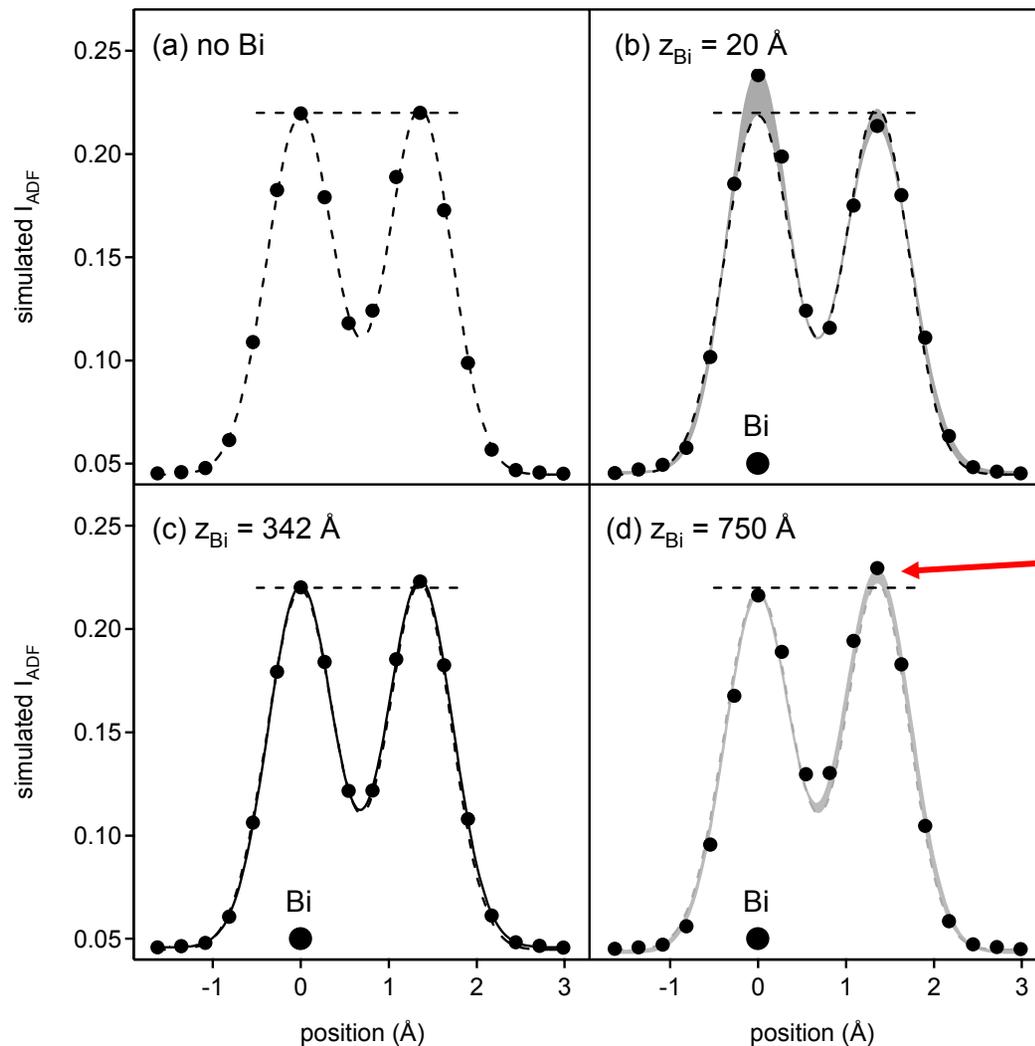
One Sb Atom vs. Depth



Scattering from one Sb atom \propto Si scattering at the same depth.

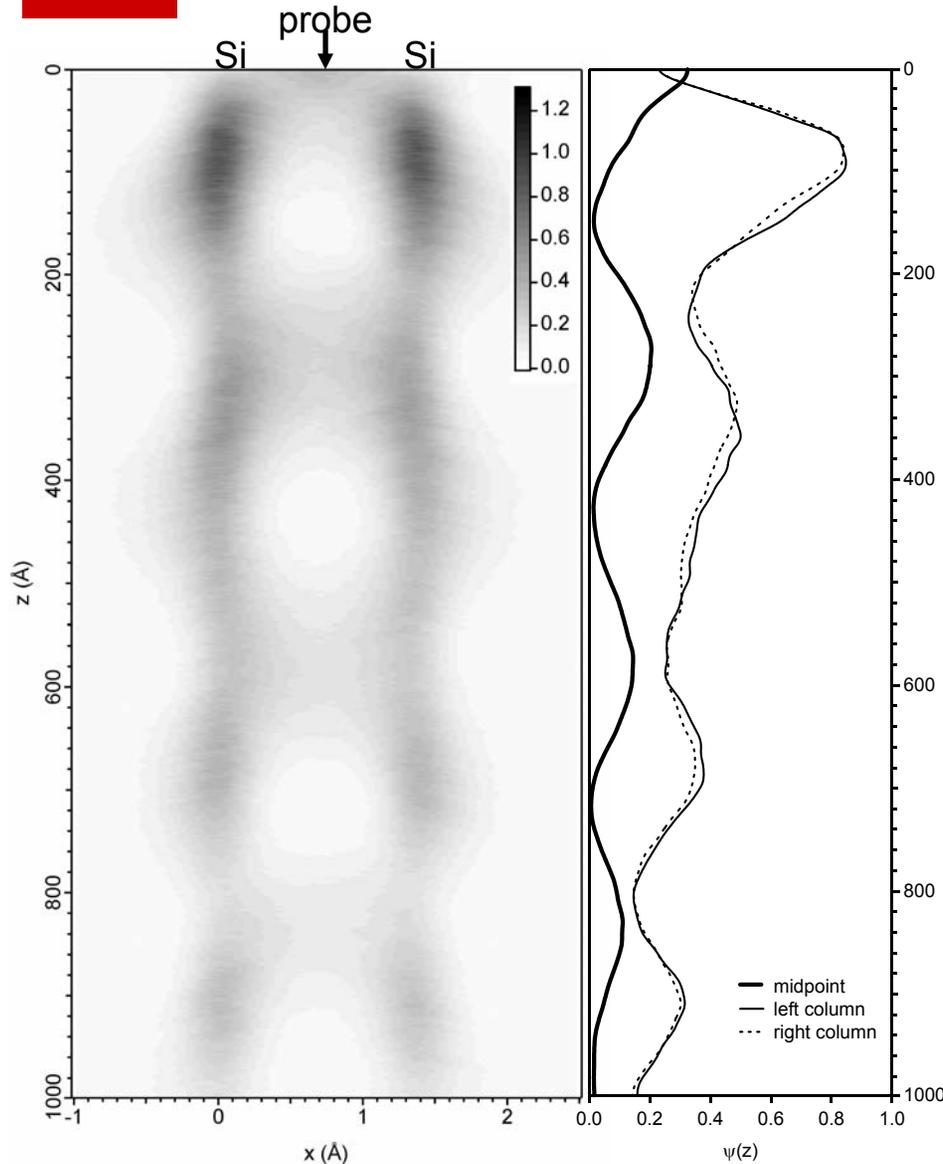
Dopants as probes of Beam Spreading

(Multislice for 75.8 nm Si in 100 kV C_s -corrected STEM)



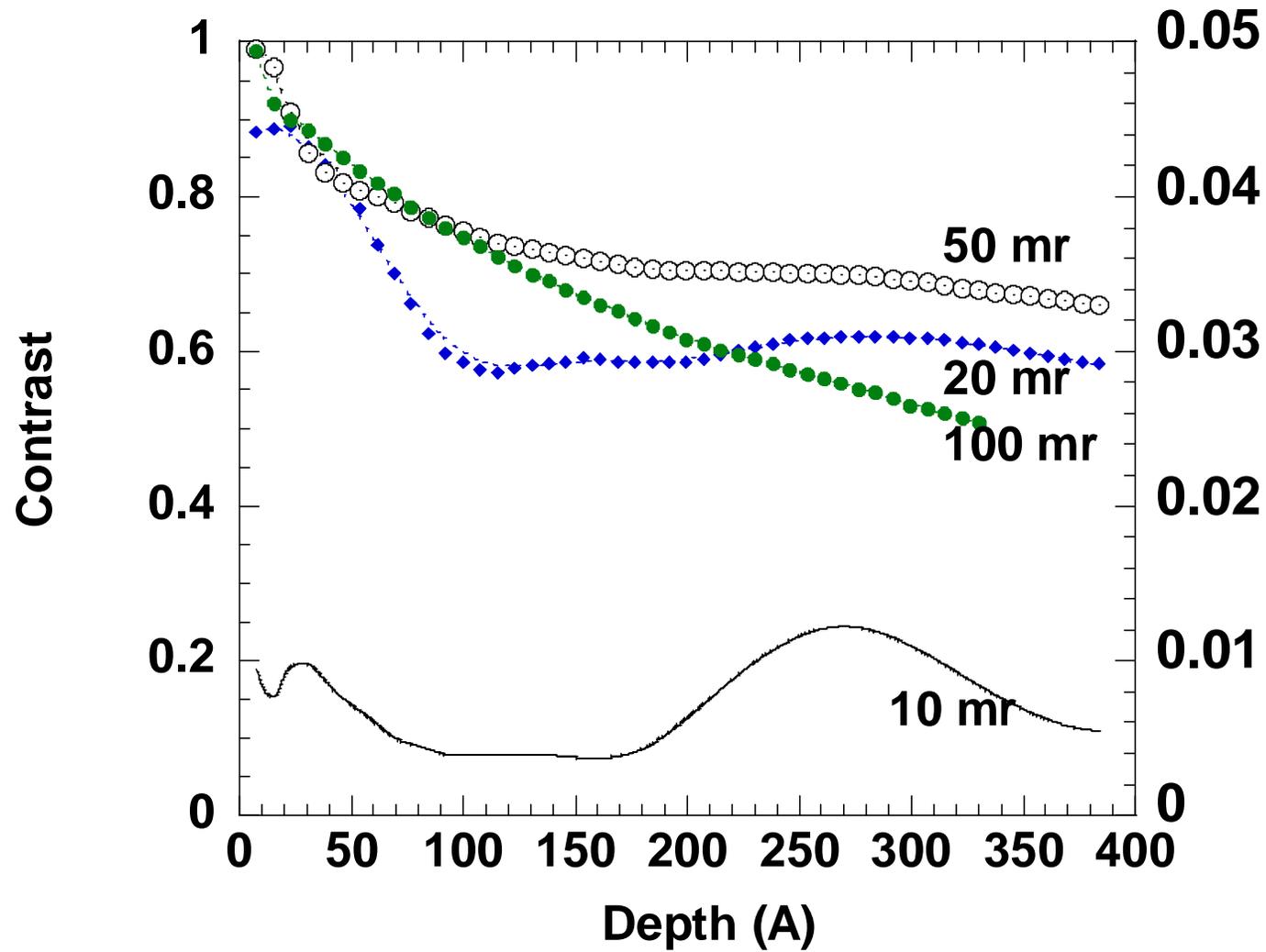
Wrong column
Appears bright!

Channeling Down Si [110]

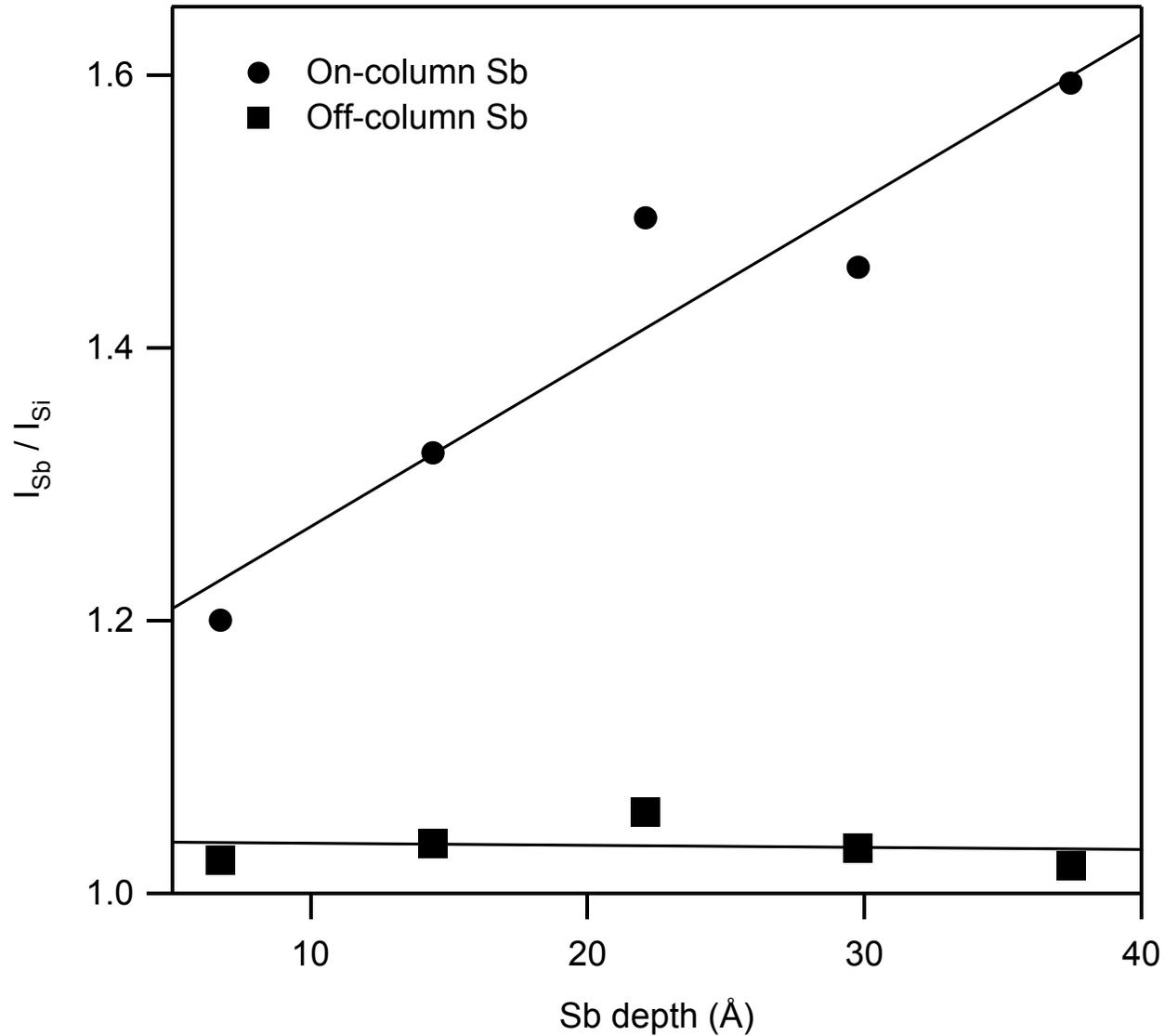


- Probe doesn't stay between atom columns -oscillates
- Almost entirely on atom columns at 100, 400 Å
- When on-column, scattering is large
Will reduce dumbbell contrast

Si Dumbbell Contrast vs. Probe Angle

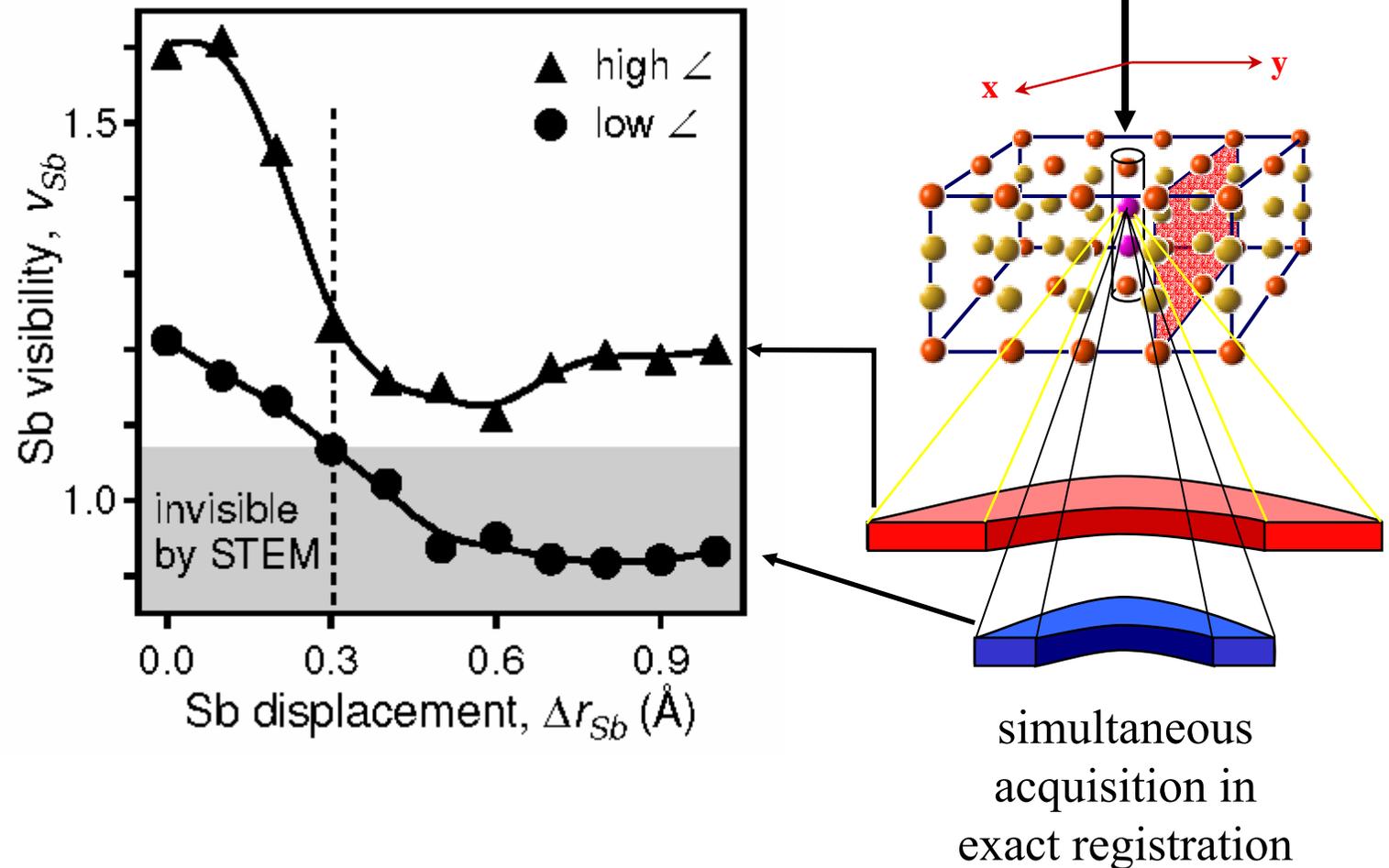


On-column vs Off

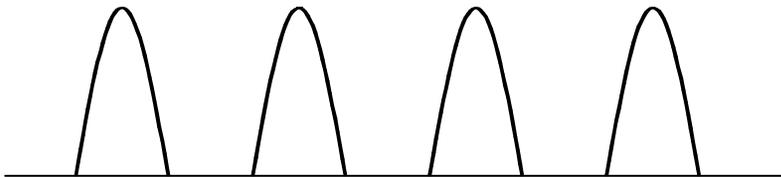
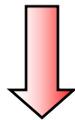
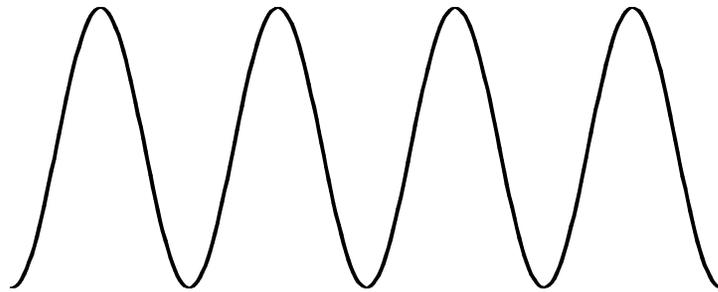




Effect of Camera Length

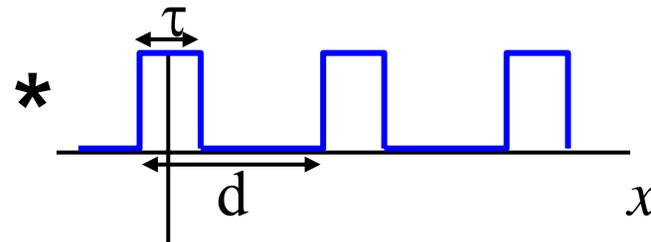
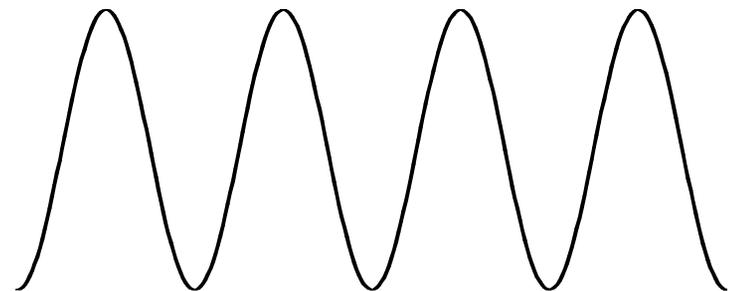


Clipping an Image is Bad (and easy to do)



Black level set too high

=

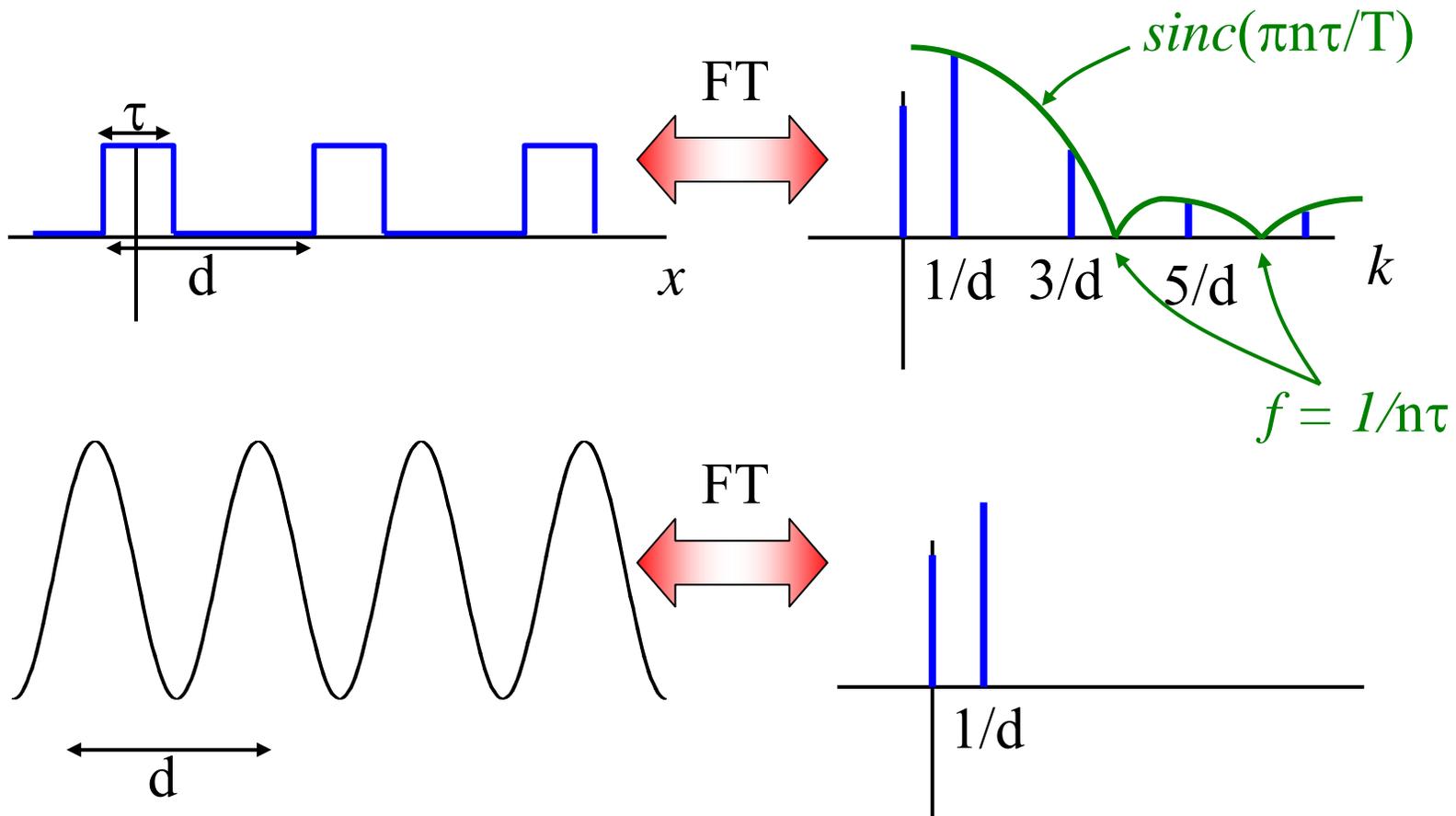


Equivalent to multiplying by square wave

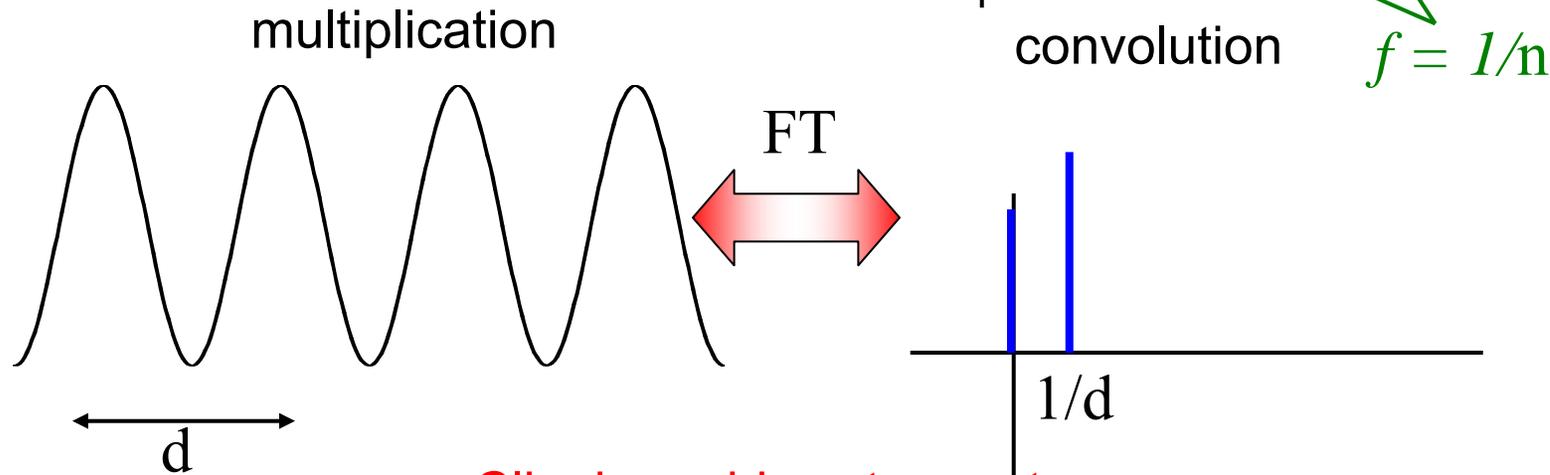
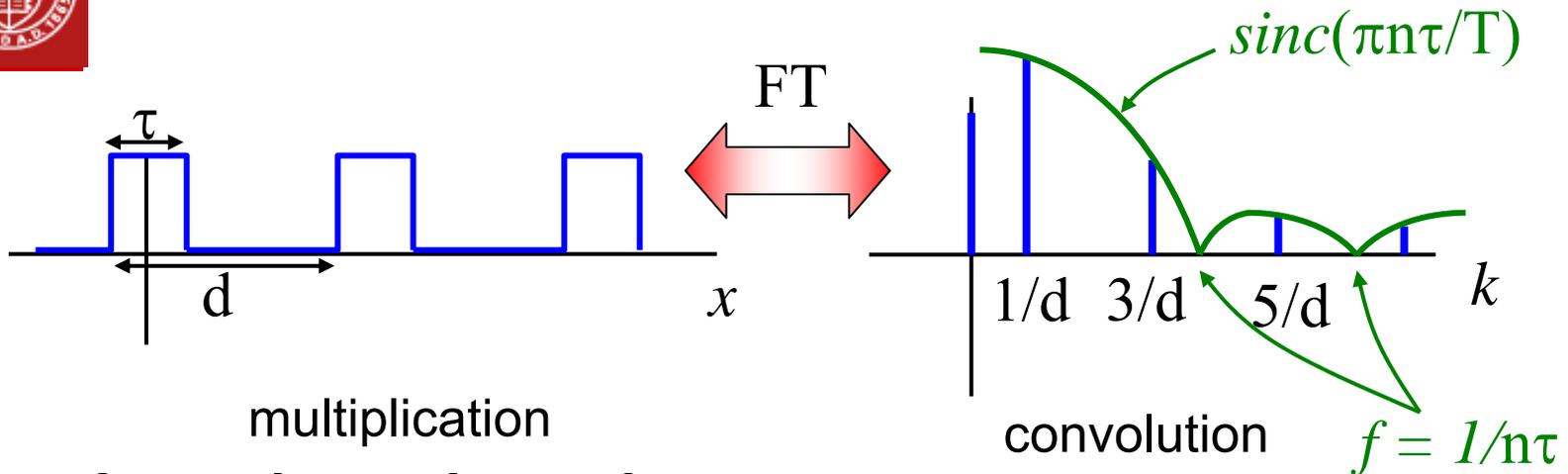
Fourier Transform of a Square Wave



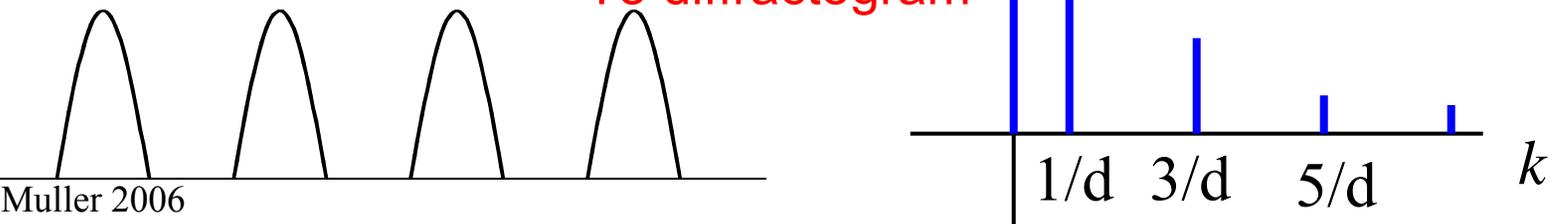
$$f(t) = \frac{A\tau}{T} + \sum_{n=1,3,5}^{\infty} \frac{2A\tau}{T} \frac{\sin(n\pi\tau/T)}{n\pi\tau/T} \cos(2\pi n f_0 t)$$

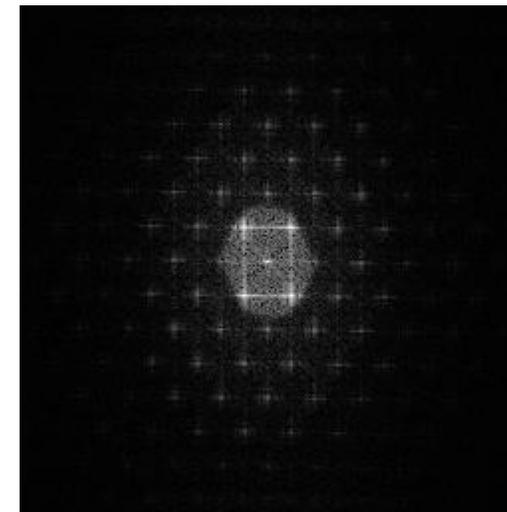
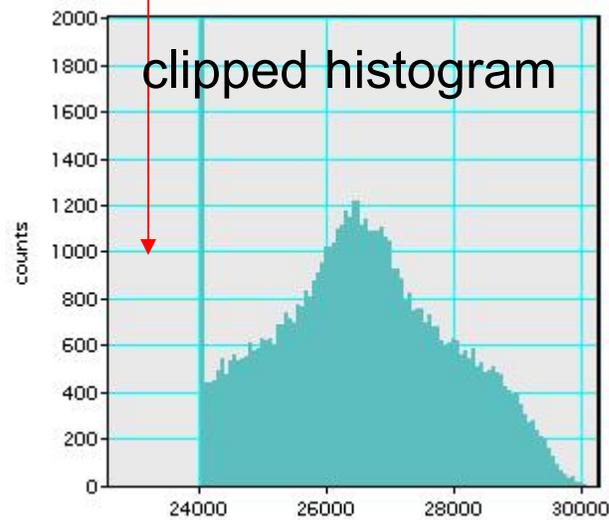
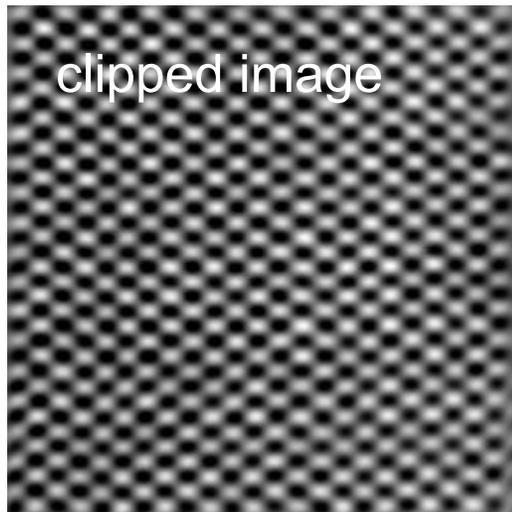
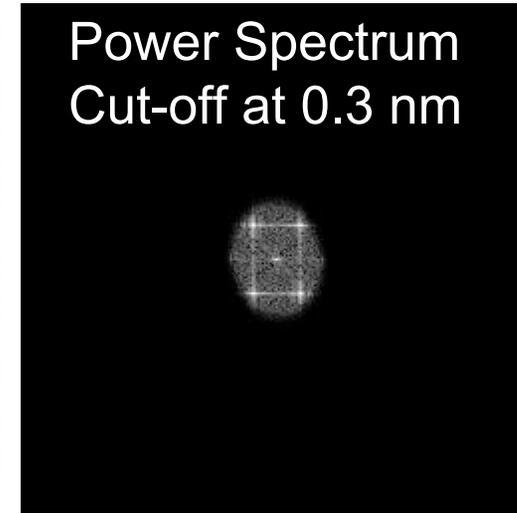
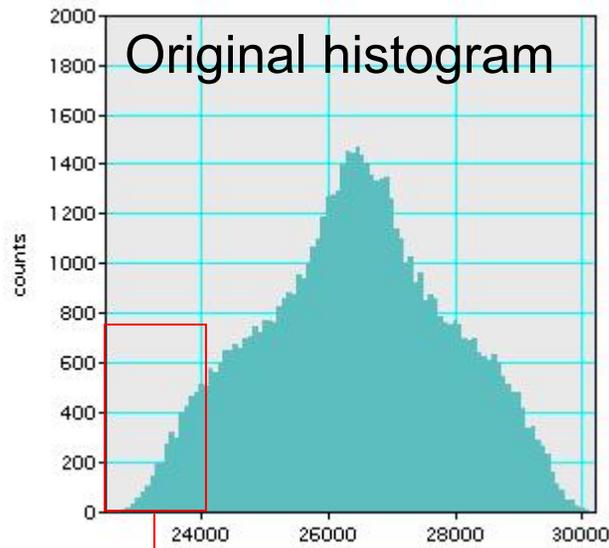
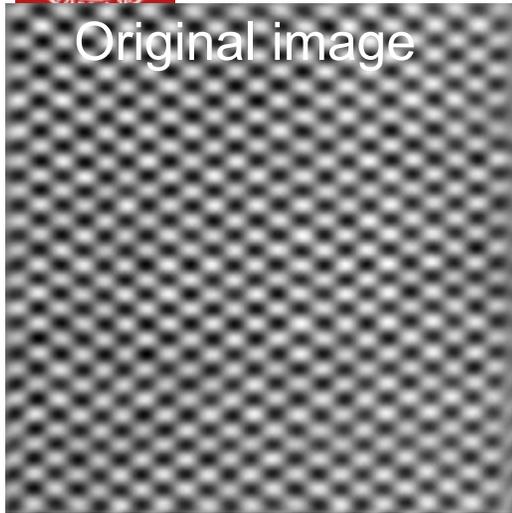


Fourier Transform of a Square Wave



Clipping adds extra spots
To diffractogram





Summary



- BF STEM – fake TEM
- LAADF STEM – strain contrast, single vacancy
- HAADF – depth dependent imaging of single dopants

- Check histograms to avoid clipping (extra spots)
- Ronchigrams – easier than imaging probe for align

Comparison of Brightness Measurements For Cold and Thermal Field Emitters



David Muller

Applied and Engineering Physics

Cornell University

Current State of the Art:

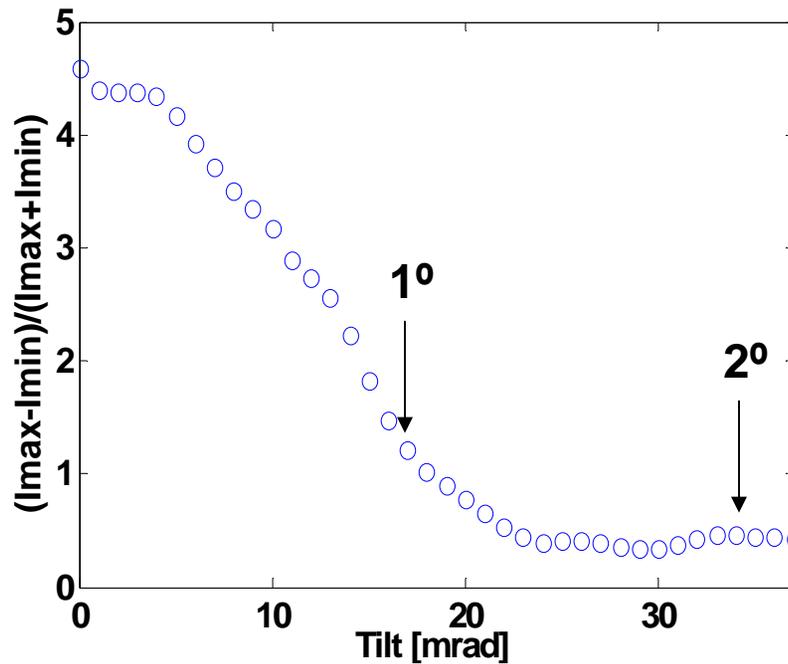
- Few good measurements of Brightness.
- Need to measure or extract the source size (easy to overestimate)
- No reliable studies of Brightness vs. Field, Temperature or monochromation

Sample Tilt in ADF-STEM

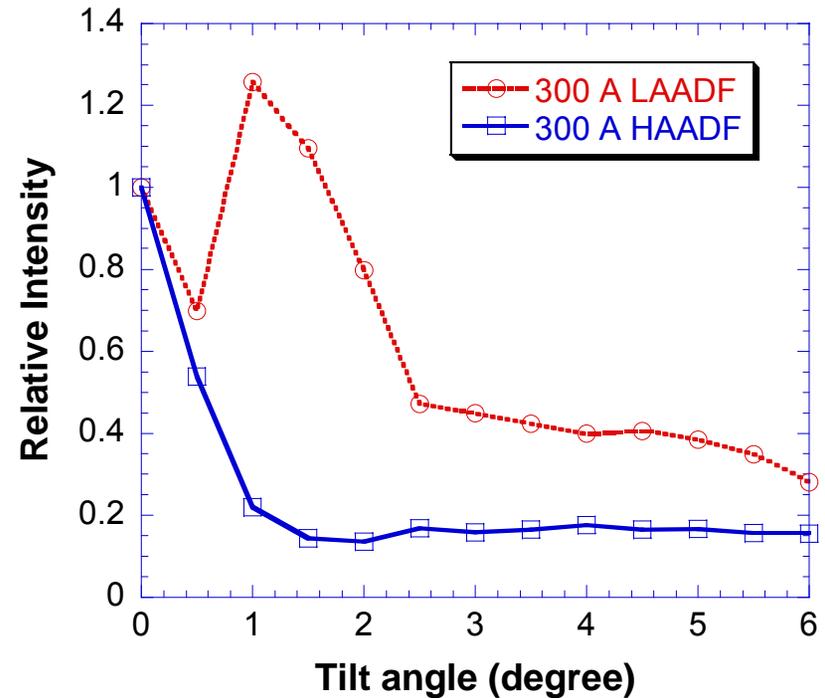


(200kV, 10 mrad)

200Å of [001] SrTiO₃



300Å of [011] Si



Up to ~ 5 mrad of mistilt is OK before fringe contrast is reduced