

GEORGIA INSTITUTE OF TECHNOLOGY  
School of Electrical and Computer Engineering

EE3230  
Homework Assignment No. 9

**Date Assigned:** March 4, 1998

**Date Due:** March 13, 1998

---

**Reading Assignment:** In Oppenheim and Willsky, study pp. 816-836.

---

**Homework Assignment:** Turn in for grading only Problems 9.4\*, 9.5\*, and 9.6\*.

---

**NOTICE:** The final exam is Thursday, March 19, at 2:50 -5:40 pm. It will cover the entire course. You may use one 8.5 by 11 inch sheet (both sides) of notes and a calculator.

---

**Problem 9.1:**

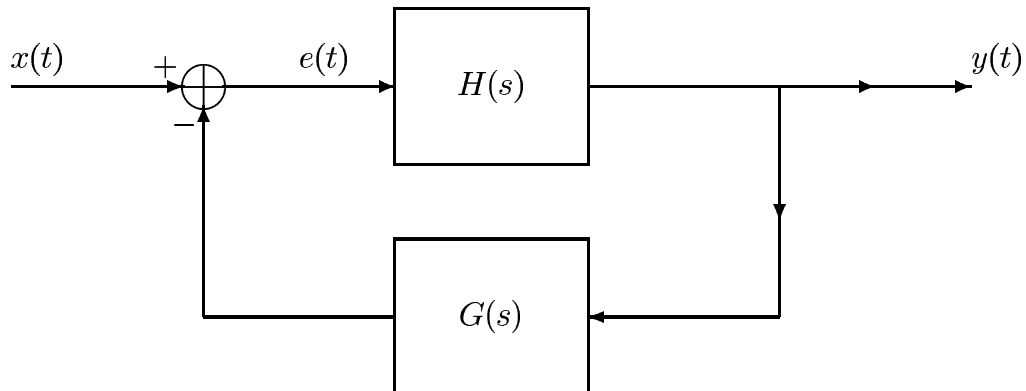
Work Problem 11.22 parts (a) and (c) in Oppenheim and Willsky.

*Answers:* (a)  $q(t) = te^{-2t}u(t)$   
(c)  $q(t) = 0.5 \sum_{k=0}^{\infty} (-0.5)^k \delta(t - k/3)$

**Problem 9.2:**

Work Problem 11.2 in Oppenheim and Willsky.

*Answer:*  $Q(s) = \frac{H_1(s)H_2(s)}{1 + H_1(s)H_2(s)G_2 + H_1(s)G_1(s)}$

**Problem 9.3:**

In the above system,  $G(s) = K$  and

$$H(s) = \frac{s - 1}{s(s + 1)}$$

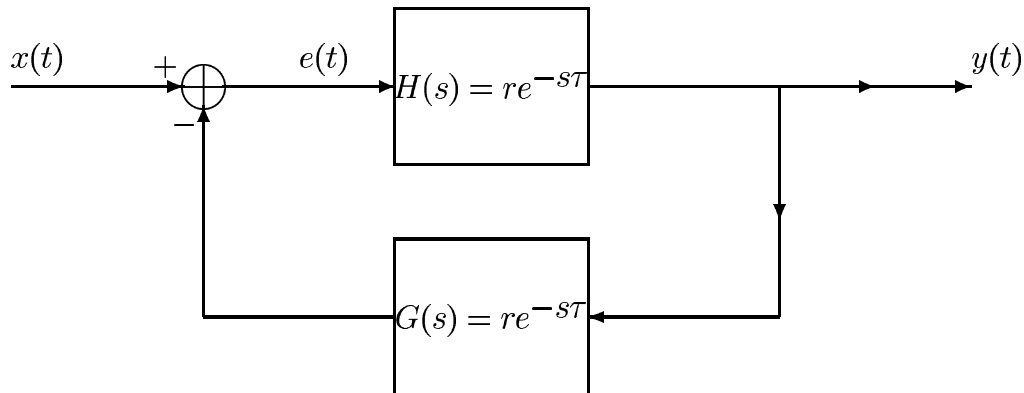
- (a) Find the value of  $K$  such that the system function  $Q(s)$  of the overall system has all its poles on the  $j\omega$  axis.
- (b) Find the impulse response of the system for the value of  $K$  found in part (a).  
*Answer:*  $q(t) = [\cos(t) - \sin(t)]u(t)$ .

**Problem 9.4\*:**

Work Problem 9.25 parts (a), (b), (c), and (d) in Oppenheim and Willsky.

**Problem 9.5\*:**

Work Problem 11.49 in Oppenheim and Willsky.

**Problem 9.6\*:**

The above diagram is a model for reflections that occur on a transmission line when it is improperly terminated. Both the upper (forward) path and the feedback path have a gain of  $r$  and a delay of  $\tau$  sec. The gain constant is such that  $|r| < 1$ .

- (a) Show that the above diagram represents the equations

$$e(t) = x(t) - ry(t - \tau) \qquad y(t) = re(t - \tau)$$

- (b) Find the system function  $Q(s)$  of the overall system.
- (c) Determine the poles and zeros of  $Q(s)$ . *Hint: The poles of  $Q(s)$  are the values of  $s$  such that  $G(s)H(s) = -1$ . Is the system stable for the values of  $r$  specified? For what values of  $r$  will the system be unstable?*
- (d) Find the impulse response of the overall system. *Hint: You may find the following result useful:*

$$\frac{1}{1 - \alpha} = \sum_{k=0}^{\infty} \alpha^k \quad \text{if } |\alpha| < 1$$

- (e) Use the impulse response to determine an expression for  $y(t)$  in terms of an infinite sum of delayed and scaled copies (echos) of  $x(t)$ .
- (f) Determine the system function  $H_i(s)$  and impulse response  $h_i(t)$  of an echo removal system which, when cascaded with the above system (i.e., the echo removal system has  $y(t)$  as input), will remove the echos producing an output  $w(t) = x(t - \tau)$ .