

9.4 B)

$$w(t) = \frac{dx(t)}{dt} + 3x(t)$$

$$h(t)_{\text{overall}} = \delta(t)$$

$$h(t)_{\text{overall}} = \left[\frac{d\delta(t)}{dt} + 3\delta(t) \right] * h_2(t) = \delta(t)$$

$$\Rightarrow \frac{d\delta(t)}{dt} * h_2(t) + 3\delta(t) * h_2(t) = \delta(t)$$

now use these rules $\left\{ \begin{array}{l} \delta(t-\alpha) * x(t) = x(t-\alpha) \\ \frac{d\delta(t)}{dt} * x(t) = \frac{dx(t)}{dt} \end{array} \right.$

$$\frac{dh_2(t)}{dt} + 3h_2(t) = \delta(t)$$

USE INTEGRATING FACTOR (diff. eq.)

$$e^{3t} \frac{dh_2(t)}{dt} + 3e^{3t} h_2(t) = \delta(t) e^{3t} = \delta(t) e^{3t}$$

\int USE $\delta(t-\alpha) x(t) = \delta(t-\alpha) x(\alpha)$

$$[e^{3t} h_2(t)]' = \delta(t)$$

$$e^{3t} h_2(t) = \int \delta(t) dt = u(t)$$

$$\Rightarrow h_2(t) = e^{-3t} u(t)$$

Note: the problem statement implies that the form for $h_2(t)$ is $Ae^{-at} u(t)$