ECE-2025 Spring-03

LECTURE #1
Sinusoids
6-Jan-03

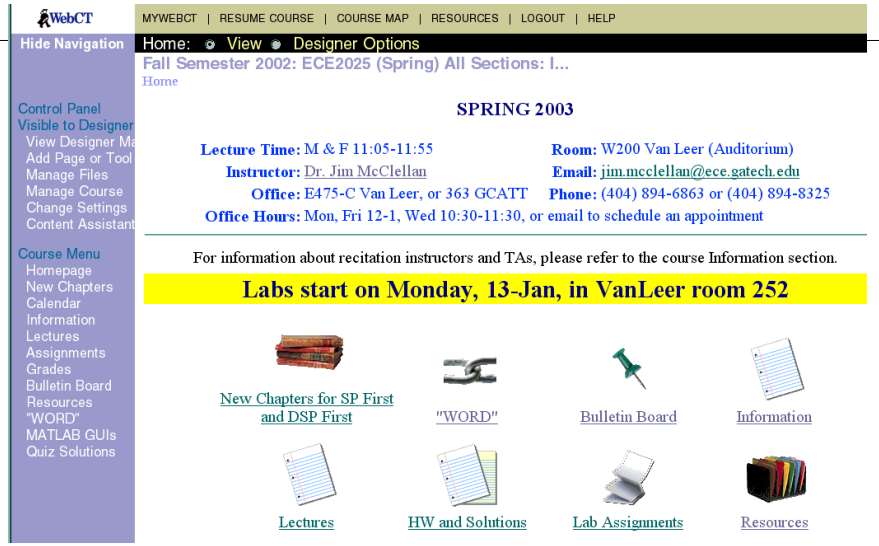
INFORMATION

- LABS
  - Room 252 in VanLeer Building
  - MATLAB based computer projects
  - MATLAB Help: next week in the evenings
- RECITATIONS
  - EMPHASIS on Problem Solving
- GRADING ?

REMINDERS

- Web-CT Login:
  - **gtxxxx** username & PRISM password
- ECE Computer Account
  - All ECE Students have an account
  - **www.ece-help.gatech.edu/faq/index.html**
- On-Line questions in WebCT
  - Review questions

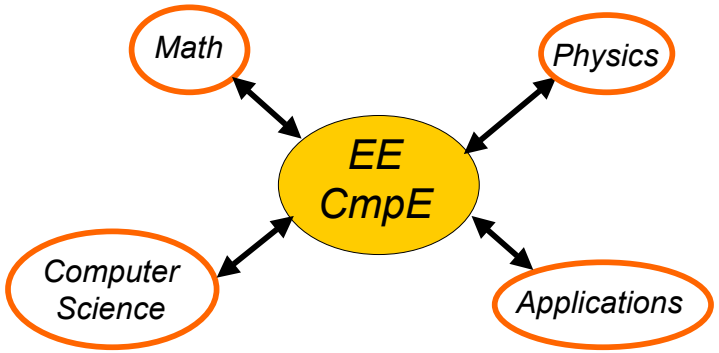
webct.gatech.edu



READING ASSIGNMENTS

- This Lecture:
  - Chapter 2, pp. 9-17
- Appendix A: Complex Numbers
- Appendix B: MATLAB
- Chapter 1: Introduction

CONVERGING FIELDS



COURSE OBJECTIVE

- Students will be able to:
- Understand **mathematical** descriptions of signal processing **algorithms** and express those algorithms as computer **implementations** (MATLAB)
- What are your objectives?

WHY USE DSP ?

- Mathematical **abstractions** lead to generalization and discovery of new processing techniques
- Computer implementations are **flexible**
- Applications provide a **physical** context

LECTURE OBJECTIVES

- Write general formula for a "sinusoidal" waveform, or signal
- From the formula, plot the sinusoid versus time
- What's a **signal**?
  - It's a **function** of time, x(t)
  - in the mathematical sense

TUNING FORK EXAMPLE

- CD-ROM demo
- "A" is at 440 Hertz (Hz)
- Waveform is a SINUSOIDAL SIGNAL
- Computer plot looks like a sine wave
- Here is a mathematical formula:

$$A\cos(2\pi(440)t+\varphi)$$

SPEECH EXAMPLE

- More complicated signal (BAT.MAT)
- Waveform ***x(t)*** is NOT a Sinusoid
- Theory will tell us
  - ***x(t)*** is approximately a sum of sinusoids
  - FOURIER ANALYSIS
    - Break ***x(t)*** into its sinusoidal components
  - Called the FREQUENCY SPECTRUM

DIGITIZE the WAVEFORM

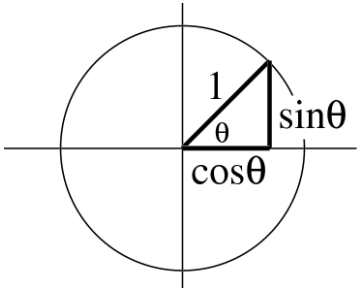
- ***x[n]*** is a SAMPLED SINUSOID
  - A list of numbers stored in memory
- Sample at 11,025 samples per second
  - Called the SAMPLING RATE of the A/D
  - Time between samples is
    - 1/11025 = 90.7 microsec
- Output via D/A hardware (at F_{samp})

STORING DIGITAL SOUND

- ***x[n]*** is a SAMPLED SINUSOID
  - A list of numbers stored in memory
- CD rate is 44,100 samples per second
- 16-bit samples
- Stereo uses 2 channels
- Number of bytes for 1 minute is
  - 2 X (16/8) X 60 X 44100 = 10.584 Mbytes

TRIG FUNCTIONS

- Circular Functions



- Common Values
  - sin($k\pi$) = 0
  - cos(0) = 1
  - cos($2k\pi$) = 1 and cos(($2k+1$)π) = -1
  - cos(($k+0.5$)π) = 0

SINES and COSINES

- Always use the COSINE FORM

$$A\cos(2\pi(440)t+\varphi)$$

- Sine is a special case:

$$\sin(\omega t)=\cos(\omega t-\frac{\pi}{2})$$

SINUSOIDAL SIGNAL

$$A\cos(\omega t+\varphi)$$

- **FREQUENCY** ω
  - Radians/sec
  - Hertz (cycles/sec)

$$\omega=(2\pi)f$$

- **PERIOD** (in sec)

$$T=\frac{1}{f}=\frac{2\pi}{\omega}$$

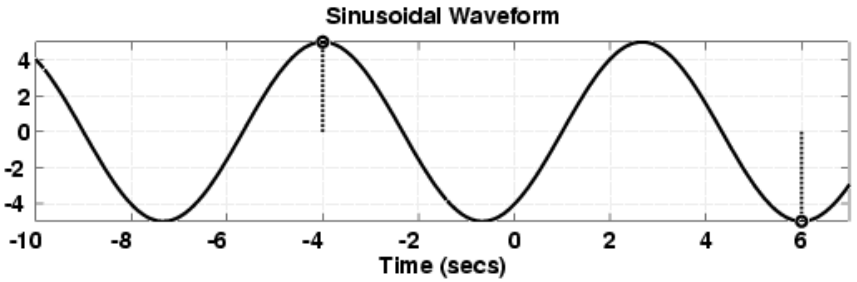
- **AMPLITUDE** A
  - Magnitude
- **PHASE** φ

EXAMPLE of SINUSOID

- Given the Formula

$$5\cos(0.3\pi t + 1.2\pi)$$

- Make a plot



PLOT COSINE SIGNAL

$$5\cos(0.3\pi t + 1.2\pi)$$

- Formula defines A, ω, and ϕ

$$A = 5$$
$$\omega = 0.3\pi$$
$$\varphi = 1.2\pi$$

PLOTTING COSINE SIGNAL from the FORMULA

$$5\cos(0.3\pi t + 1.2\pi)$$

- Determine **period**:

$$T = 2\pi / \omega = 2\pi / 0.3\pi = 20/3$$

- Determine a **peak** location by solving

$$(\omega t + \varphi) = 0$$

- **Zero** crossing is T/4 before or after
- Positive & Negative peaks spaced by T/2