

PROBLEM FALL-04-Q.1.1:

Simplify the following complex-valued expressions. In each case reduce the answers to the **simple** numerical form requested. Let

$$U = \sqrt{3} - j; \quad V = \frac{1}{2}e^{j\frac{3\pi}{4}}.$$

(a) Express $X = U + j^3V$ in rectangular form.

(b) Express $Y = U^*V$ in polar form.

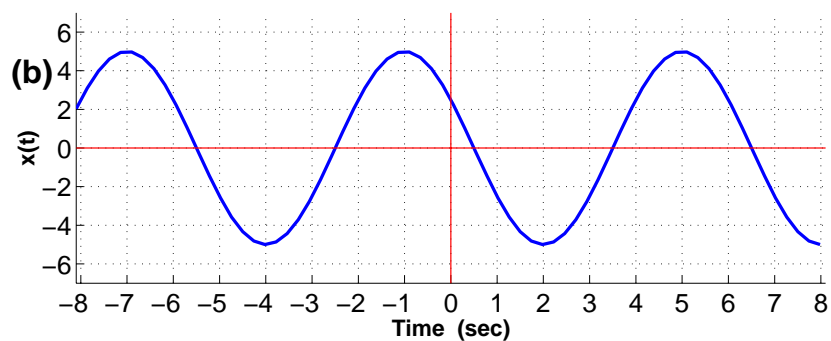
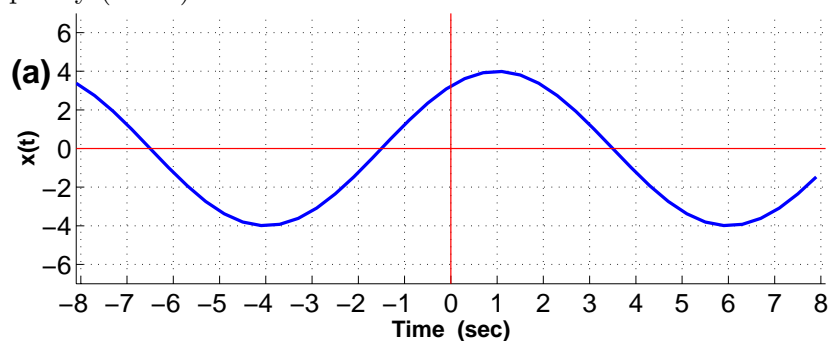
(c) Express $Z = V + V^*$ in rectangular form.

(d) Determine $\Re \left\{ \frac{U}{|V^*|} \right\}$.

(e) Express $\Re \left\{ \frac{1}{\sqrt{V}} e^{j5t} \right\}$ in the standard “cosine” form.

PROBLEM FALL-04-Q.1.2:

Two sinusoidal signals are plotted below. For each signal, determine the amplitude, phase (in radians) and frequency (in Hz).



(a) Determine the amplitude, A_a , frequency in Hz., f_a , and phase, ϕ_a , of the upper sinusoid.

(b) Determine the amplitude, A_b , frequency in Hz., f_b , and phase, ϕ_b , of the lower sinusoid.

(c) What is the fundamental frequency (in Hz.) of the sum of these two sinusoids?

PROBLEM FALL-04-Q.1.3:

The following MATLAB code defines several signals that are then multiplied and summed:

```
tt = -10:0.001:10;  
xxe = 2*cos(60*pi*tt);  
xx1 = 3*cos( pi*(tt - 2/3) );  
xx2 = 4*cos( pi*tt - 7*pi/6 );  
xx = xxe.*(xx1 + xx2);
```

- (a) If the signal $x_1(t)$ corresponds to the MATLAB vector **xx1**, determine the complex amplitude of $x_1(t)$.

- (b) If the signal $x(t)$ corresponds to the MATLAB vector **xx**, then it is possible to express $x(t)$ in the form

$$x(t) = A \cos(\omega_1 t) \cos(\omega_2 t + \phi)$$

Determine the numerical values of A , ω_1 , ω_2 and ϕ . *Hint:* Use phasor addition.

$$A = \underline{\hspace{2cm}}$$

$$\omega_1 = \underline{\hspace{2cm}}$$

$$\omega_2 = \underline{\hspace{2cm}}$$

$$\phi = \underline{\hspace{2cm}}$$

PROBLEM FALL-04-Q.1.4:

Let

$$x_1(t) = 3 \cos\left(5\pi t + \frac{\pi}{3}\right); \quad x_2(t) = \Im\left\{\frac{1}{2}e^{j5\pi t}\right\}$$

(a) Plot the spectrum of $x_1(t)$. Be sure to label all of the frequencies and complex amplitudes.

(b) Plot the spectrum of $x_2(t)$. Be sure to label all of the frequencies and complex amplitudes.

(c) Plot the spectrum of $y(t) = x_1(t)x_2(t)$. Be sure to label all of the frequencies and complex amplitudes.

(d) Now let $z(t) = x_1(t) \cos(5\pi t + \phi)$. Determine **all** possible values of ϕ for which the DC value of $z(t)$ will be zero.