

Hint (2.31)

Difference equation is

$$y[n] + \frac{1}{15}y[n-1] - \frac{2}{5}y[n-2] = x[n]$$

- For the homogeneous solution, find the roots,  $p_1$  and  $p_2$  of the homogeneous equation

$$p^2 + \frac{1}{15}p - \frac{2}{5} = 0$$

- Responses of this system have a general form

$$h[n] = A(p_1)^n + B(p_2)^n$$

- ~~For~~ If the system is causal,

$$h_{\text{causal}}[n] = [A(p_1)^n + B(p_2)^n] u[n]$$

↑ step function  
non-zero for  $n \geq 0$

- If the system is anti-causal

$$h_{\text{A-causal}}[n] = [A(p_1)^n + B(p_2)^n] u[-n-1]$$



- For homogeneous solutions,

all  $x[n] = 0$ ,  $A, B$  just constant

(verify that the sequence satisfies the homogeneous equation)

- For  $h_{\text{causal}}[n]$ , use the fact that  $x[n] = \delta[n]$  to generate equations from which the values of  $A$  &  $B$  can be determined. E.g. at  $n=0$ ,  $h[0] = x[0] = A+B$

- For  $h_{\text{anticausal}}[n]$ , similarly, generate equations to determine  $A$  and  $B$ . E.g. at  $n=0$ ,  $h[0] + \frac{1}{15}h[-1] - \frac{2}{5}h[-2] = 1$ , ← express this in  $A$  and  $B$ .