

WORKSHEET 10/3/22
MATH 2331, FALL 2022

You may take for granted that the reduced row-echelon form of the matrix $\begin{bmatrix} 1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 9 \end{bmatrix}$ is the matrix $\begin{bmatrix} 1 & 0 & -1 \\ 0 & 1 & 2 \\ 0 & 0 & 0 \end{bmatrix}$.

- (1) Are the vectors $\vec{v}_1 = (1, 2, 3)$, $\vec{v}_2 = (4, 5, 6)$, and $\vec{v}_3 = (7, 8, 9)$ linearly independent?
- (2) How large could a collection of linearly independent vectors in \mathbb{R}^m be?
- (3) Do the vectors $\vec{v}_1 = (1, 2, 3)$, $\vec{v}_2 = (4, 5, 6)$, and $\vec{v}_3 = (7, 8, 9)$ span \mathbb{R}^3 ?
- (4) How small could a set of vectors spanning \mathbb{R}^m be?
- (5) Suppose that \vec{w}_1 , \vec{w}_2 , and \vec{w}_3 are linearly independent vectors. How many ways could there be to write another vector \vec{w} as a linear combination of these vectors?