

# Traitor Traceable Signature Scheme

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*Abstract* — The new signature scheme, *traitor traceable signature scheme* is presented, which allows the signer to convince any arbiter of the recipient's infringement, if the recipient distributes illegally the signature which he got. We use the techniques of a proof of knowledge of discrete logarithm[1][2], identification of double spender in an off-line electronic cash[3][4], and a signcryption scheme[5]. Our scheme consists of 3-move and it is more compact and efficient compared with the previous scheme[6], due to eliminate the cumbersome cut-and-choose like techniques. Moreover, our accusation protocol does not require the private-key of the recipient of signature, i.e., signer can convince any arbiter of the recipient's infringement without help of original recipient.

## I. INTRODUCTION

In a conventional digital signature scheme, after issuing the digital document with his signature, the signer cannot convince anyone who has leaked his signed document, since he can reproduce it arbitrarily. Recently, [6] proposed that the technique of tracing traitor[7][8] could be applied to the message with signature in order to prevent illegal proliferation of it. This approach is effective in case that both the message and signature are valuable for anyone.

However, this method[6] is not efficient in communication and computation, due to involve the cumbersome cut-and-choose like technique. Moreover, [6] has the following two problems, 1) an accusation protocol requires the private-key of the recipient of signature. Therefore, if the recipient is not available, the arbiter cannot make decision of accusation, 2) after accusation protocol, the signer can know the complete signature which is known only by recipient before accusation. This means that [6] is not robust against signer making wrong accusations.

## II. TRAITOR TRACEABLE SIGNATURE

In this paper, we propose the new signature scheme, *traitor traceable signature*, which solves several problems of [6]: 1) if the recipient distributes illegally the signature which he got, our scheme allows the signer to convince any arbiter of the recipient's infringement, 2) We use the technique of a proof of knowledge of discrete logarithm, identification of double spender in an off-line electronic cash, and a signcryption scheme, which are well estimated to be (provably) secure, 3) our scheme consists of 3-move and it is more compact and efficient compared with the previous scheme[6], due to eliminate

<sup>1</sup>This work was performed in part of Research for the Future Program (RFTF) supported by Japan Society for the Promotion of Science (JSPS) under contract no. JSPS-RFTF 96P00604.

the cumbersome cut-and-choose like techniques, 4) our accusation protocol does not require the private-key of the recipient of signature (the signer can convince any arbiter of the recipient's infringement without help of original recipient), 5) the signature can be generated to the recipient only once per each execution of this protocol in order to prevent the signer from making wrong accusations.

Table 1: Traitor Traceable Signature Scheme

Alice		Bob
$x \in_R \mathbb{Z}_q$		
$X \leftarrow g^x$		
$init_A(x) \leftarrow (X, sig_A(X))$	$\xrightarrow{init_A(x)}$	
		$verify\ init_A(x)$ $i, j, r_1, r_2, u_1 \in_R \mathbb{Z}_q$ $I \leftarrow g^i$ $J \leftarrow g^j$ $R_1 \leftarrow g^{r_1}$ $R_2 \leftarrow g^{r_2}$ $\sigma_1 \leftarrow r_1 - iH(R_1) \bmod q$ $\sigma_2 \leftarrow r_2 - jH(R_2) \bmod q$ $v_1 \leftarrow i - ju_1 \bmod q$ $u_2 \leftarrow H(I, J, R_1, R_2,$ $\sigma_1, \sigma_2, u_1, v_1)$ $v_2 \leftarrow i - ju_2 \bmod q$ $V \leftarrow g^{v_2}$ $W(i, x) = (I, J, R_1,$ $R_2, \sigma_1, \sigma_2,$ $u_1, v_1, u_2, V)$
	$\xrightarrow{req_B(i, x)}$	$req_B(i, x)$ $\leftarrow (W(i, x),$ $sig_B(W(i, x)))$
$verify\ req_B(i, x)$ by $R_1 \stackrel{?}{=} g^{\sigma_1} I^{H(R_1)}$ $R_2 \stackrel{?}{=} g^{\sigma_2} J^{H(R_2)}$ $I \stackrel{?}{=} g^{v_1} J^{u_1}$ $I \stackrel{?}{=} V J^{u_2}$		
$generate(c, r, s)$ by $V^x \rightarrow k_1, k_2$ $r = KH_{k_2}(m)$ $s = x/(r + x_a) \bmod q$ $c = E_{k_1}(m)$	$\xrightarrow{(c, r, s)}$	obtain $(c, r, s, v_2)$

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