

# **Spatial omics feature representation** using graph Fourier transform



COLLEGE OF MEDICINE

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Introduction			Graph signal transform	
Background:	Challenge			Step 1: K-nearest neighbor (KNN) Graph construction
<ul> <li>Spatial omics (e.g., spatial transcriptome, proteome, ep are transforming our understanding of cell or tissue biolog</li> </ul>		mplexity of construction spatial omics platforms.	due to	(i) Define an undirected graph and adjacency matrix.
<ul> <li>Cell-centric analysis enables us to investigate the organ</li> </ul>	zation of spatial domain, • Interpret	ability of repres	sentation	G = (V, E)
relations of the cell-neighborhood, cell-cell communicatio		0		where $V = \{v_1, v_2,, v_n\}$ is the node set referring to n
<ul> <li>Gene-centric analysis enables the discovery of spatially as spatial variable genes (SVG).</li> </ul>		ty issue due to the p (e.g., Stereo-seq and COD	ixel-level	spots; <i>E</i> is the edge set defined by KNN.
<ul> <li>However, a quantitative and qualitative representatio</li> </ul>	n method of organized • Non-triv	al aggregation meth	nod of	(ii) An adjacent binary matrix $A = (a_{ij})$ with rows and
spatial pattern presented by diverse spatial omics feature	es is still a gap for further embedd	ng graph topological struc	ture and	columns as n spots is defined as:
gene-centric analysis		)	$(1 \circ C F)$	

gene-centric analysis.

graph signal (e.g., gene expression).

Solution: A hypothesis-free graph Fourier transform framework, Spatial Graph Fourier Transform (SpaGFT), for spatial omics data feature representation.



Figure. 1 The SpaGFT conceptual schema. A spatially organized molecule is a smooth signal and can be represented as the linear combination of k low-frequency Fourier mode (FMs), where a low-frequency FM contributes to a slow and smooth graph signal variation. Fourier coefficient (FC) can measure FMs contribution.

 $e_{ii} \in E$  $a_{ij} =$ else.

(iii) A diagonal matrix  $D = diag(d_1, d_2, ..., d_n)$ , where  $d_i = \sum_{j=1}^n a_{ij}$  represents the degree of  $v_i$ 

#### **Step 2: Fourier mode calculation**

(i) Using matrices A and D, a Laplacian matrix L can be obtained by

$$L = D - A$$

(ii) The Laplacian matrix *L* can be decomposed using spectral decomposition

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L = U\Lambda U^{\mathrm{T}}
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$$\Lambda = diag(\lambda_1, \lambda_2, \dots, \lambda_n),$$
$$U = (\mu_1, \mu_2, \dots, \mu_n),$$

where the diagonal elements of  $\Lambda$  are the eigenvalues of *L* with  $\lambda_1 \leq \lambda_2 \leq \cdots \leq \lambda_n$ , where  $\lambda_1$  is always equal to 0 regardless of graph topology.

#### **Step 3: Graph Fourier transform**

The graph signal of a gene g is defined as  $f_g =$  $(f_q^1, f_q^2, \dots, f_q^n) \in \mathbb{R}^n$ , which is a *n*-dimensional vector and represents the gene expression values across nspots. The graph signal  $f_{q}$  is transformed into a Fourier coefficient  $\widehat{f}_g$  by

## **Results-SVG identification performance**



Figure. 2 a. The SVG prediction evaluation was compared to five benchmarking tools. The running time (log transformation) seconds) of each tool is represented as red lines. **b.** After parameter selection (three high-quality datasets), the SVG prediction performance of SpaGFT on additional 28 independent datasets was compared to those of the five benchmark tools. Conclusion: **SpaGFT identifies SVG more accurately and faster.** 

**Results – graph signal representation and process** 

 $\hat{\boldsymbol{f}}_{g} = \boldsymbol{U}^{T} \boldsymbol{f}_{g}, \, \hat{\boldsymbol{f}}_{g} = (\hat{f}_{g}^{1}, \hat{f}_{g}^{2}, \dots, \hat{f}_{g}^{n})$ 

 $\hat{f}_{g}^{k}$  is the projection of  $f_{g}$  on FM  $\mu_{k}$ , representing the contribution of FM  $\mu_k$  to graph signal  $f_g$ , k is the index of  $f_g$  (e.g., k = 1, 2, ..., n). This Fourier transform harmonizes gene expression and its spatial distribution to represent gene g in the frequency domain.

### Discussion



- Transformed signals (FCs) compressed graph topology and graph signal (e.g., gene expression).
- Low-frequency FCs represent features' spatial smooth pattern, leading to a new method for SVG identification.
- A low-pass filter enhances signal and removes noise.
- FCs can be used for other downstream tasks (e.g., SVG clustering to identify functional niches).

Link and acknowledgement

Paper QR



SpaGFT GitHub QR



Figure. 3 a. SVGs identified by SpaGFT were distinguishably separated from non-SVGs on the FM-based UMAP with a clear boundary, whereas SVGs were irregularly distributed on the PC-based gene UMAP. b. SpaGFT can enhance and remove noise and outperformed other gene enhancement tools. c. SpaGFT enhanced signal and removed the noisy background for spatial omics platforms. Conclusion: (1) FC is a transformed simple but informative topological features for representing complex structures with irregular topologies. (2) The FCs of low-frequency FMs will be enhanced and those of highfrequency FMs will be diminished.

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