Eco-Evolutionary Theory and Insect Outbreaks

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Abstract: Eco-evolutionary theory argues that population cycles in consumer-resource interactions are partly driven by natural selection, such that changes in densities and changes in trait values are mutually reinforcing. Evidence that the theory explains cycles in nature, however, is almost nonexistent. Experimental tests of model assumptions are logistically impractical for most organisms, while for others, evidence that population cycles occur in nature is lacking. For insect baculoviruses in contrast, tests of model assumptions are straightforward, and there is strong evidence that baculoviruses help drive population cycles in many insects, including the gypsy moth that we study here. We therefore used field experiments with the gypsy moth baculovirus to test two key assumptions of eco-evolutionary models of host-pathogen population cycles: that reduced host infection risk is heritable and that it is costly. Our experiments confirm both assumptions, and inserting parameters estimated from our data into eco-evolutionary insect-outbreak models gives cycles closely resembling gypsy moth outbreak cycles in North America, whereas standard models predict unrealistic stable equilibria. Our work shows that eco-evolutionary models are useful for explaining outbreaks of forest insect defoliators, while widespread observations of intense selection on defoliators in nature and of heritable and costly resistance in defoliators in the lab together suggest that eco-evolutionary dynamics may play a general role in defoliate outbreaks.

Keywords: heritability, trade-offs, host-pathogen, complex dynamics, eco-evolutionary.

Introduction

Eco-evolutionary theory has shown that natural selection can help drive cycles in predator-prey and other consumer-resource interactions, such that changes in trait values drive changes in population densities and vice versa (Abrams 2000). Recent work has focused in particular on the case for which selection by the consumer drives selection on the resource (Ellner 2013). In this case, increases in consumer attack rates lead to both reductions in resource densities and selection-driven increases in resource resistance, while decreases in attack rates lead to both increases in resource densities and selection-driven reductions in resistance because of a fitness trade-off between resistance and fecundity. In eco-evolutionary dynamics, changes in population densities and changes in trait values are thus mutually reinforcing.

Eco-evolutionary cycles occur in predator-prey models (Abrams and Matsuda 1997; Doebeli 1997; Ellner et al. 2011; Schreiber et al. 2011), host-parasitoid models (Sasaki and Godfray 1999), and host-pathogen models (Dieckmann 2002; Elderd et al. 2008), suggesting that eco-evolutionary cycles should be widespread in nature. Moreover, laboratory microcosms have provided conclusive evidence of eco-evolutionary predator-prey cycles in real consumer-resource interactions (Fussmann et al. 2000; Yoshida et al. 2003). Field tests of the theory, however, are almost nonexistent (Abrams 2000), which is important because conditions in nature are often very different from conditions in the lab. It is thus unclear whether eco-evolutionary consumer-resource cycles occur in nature.

We therefore tested eco-evolutionary theory using field data for the gypsy moth (Lymantria dispar) and its baculovirus pathogen. Insect-baculovirus interactions provide useful systems for testing models of host-pathogen interactions because they can be used in field experiments designed to estimate overall infection risk (Elderd 2013), which in eco-evolutionary models is equivalent to host resistance (Dieckmann 2002). Previous studies of the heritability and costs of resistance—whether in insects (Watanabe 1987; Boots and Begon 1993; Cory and Myers 2009) or in other hosts (Altizer et al. 2003)—have in contrast relied mostly on laboratory experiments in which all hosts are forced to be exposed to the pathogen, so that the experiments measure infection risk given exposure rather than overall infection risk. Even if exposure risk is allowed to vary, host behavior in the lab-
oratory may be artificially constrained in a way that substantially alters overall risk (Eakin et al. 2015). In insect-baculovirus interactions, however, it is possible to carry out field experiments that allow for natural variation in host behavior, leading to estimates of overall infection risk that match those estimated from epizootics in nature (Dwyer et al. 1997). In the first step in our research, we therefore used field experiments to test the assumptions of eco-evolutionary models that resistance is heritable and costly.

Because our experiments supported the model assumptions, in the second step in our research, we tested the model prediction that natural selection helps drive population cycles. In a few previous studies, the heritability of overall infection risk has at least been measured in the laboratory or the greenhouse (Henter and Via 1995; Herzog et al. 2007; Zbinden et al. 2008; Auld et al. 2013, 2014), but these experiments have used hosts for which there is no evidence of population cycles in nature. For the gypsy moth and other defoliating insects, however, the economic damage imposed by outbreaks has driven the collection of extensive data sets documenting population cycles (Liebhold and Kamata 2000; Johnson et al. 2005). Experimental manipulation of such cycles is impractical, because defoliation outbreaks cycles occur over timescales of decades and spatial scales of thousands of square kilometers (Liebhold and Kamata 2000), but the data nevertheless allow us to indirectly test the predictions of our models. We thus tested whether our data and our models are consistent with gypsy moth cycles in nature by comparing the predictions of models parameterized from our experimental data to observational data on gypsy moth population cycles.

Previous efforts to explain gypsy moth population cycles have met with limited success. Classical insect-pathogen models require variability in host infection risk to prevent pathogen extinction, but realistically high variability causes the models to produce a stable equilibrium instead of cycles (Dwyer et al. 2000). Extending classical models to include effects of induced plant defenses on disease transmission produces models that again show realistic cycles, but these cycles require particular spatial configurations of tree species (Elder et al. 2013). Host-pathogen/induced-defense models therefore cannot explain observations of outbreaks in some forest types (Haynes et al. 2009b).

Adding heritable variation in resistance to classical insect outbreak models in contrast leads to realistic cycles for realistic variability in host infection risk, irrespective of forest type (Elder et al. 2008). Moreover, baculovirus mortality is often high during gypsy moth outbreaks (Woods and Elkinton 1987), implying that selection pressure is high, while resistance in the lab is heritable and costly (Pâez et al. 2015). Eco-evolutionary models may therefore provide a better explanation for gypsy moth outbreak cycles than existing models.

Previous eco-evolutionary insect outbreak models nevertheless made the unrealistic but mathematically convenient assumption that heritability is perfect (Elder et al. 2008), whereas in nature heritability is almost certainly <1. Moreover, reduced heritability is strongly stabilizing in predator-prey models (Schreiber et al. 2011), so if the heritability of resistance to the baculovirus is too low, cycles may not occur in the models. Whether eco-evolutionary insect-outbreak models can explain gypsy moth outbreak cycles is therefore an open question.

Testing whether our experimental estimates of the heritability and cost of infection risk are consistent with gypsy moth population cycles therefore required that we extend previous eco-evolutionary insect outbreak models to allow for imperfect heritability. Because the predictions of the parameterized models match the data, we conclude that eco-evolutionary consumer-resource cycles occur in nature, not just in microcosms. Because the gypsy moth is a major pest of hardwood forests in North America (Elkinton and Liebhold 1990), and because the virus plays a role in gypsy moth control (Podgwaite et al. 1993), our models may be practically useful for guiding gypsy moth management, as we discuss.

Methods

Baculovirus Biology and Eco-Evolutionary Models of Insect Outbreaks

In defoliating insects like the gypsy moth, baculovirus transmission occurs when larvae accidentally consume foliage contaminated with infectious occlusion bodies, microscopic particles with a 10–20-nm radius that are released in large numbers (10^6–10^9) from the cadavers of infected conspecifics (Cory and Hoover 2006). In an occlusion body, DNA-containing virions are enclosed in a polyhedral-shaped protein matrix, which dissolves in the alkaline conditions of the insect midgut, freeing the virions so that they can infect the insect’s tissues (Funk et al. 1997). Consumption of a large enough dose leads to death, after which viral enzymes break down the larval cuticle, releasing occlusion bodies into the environment to complete the cycle of transmission (Elderd 2013). In high-density insect populations, multiple rounds of transmission cause severe mortality, terminating outbreaks (Moreau and Lucarotti 2007). The virus then overwinters by contaminating the egg masses produced by surviving insects, and hatching larvae become infected as they chew their way out of contaminated eggs the following spring (Murray and Elkinton 1989).

Because gypsy moths have only one generation per year, and because only larvae can become infected, there can be only one epizootic per year (Fuller et al. 2012). To model gypsy moth outbreaks, we therefore first constructed a
continuous-time epizootic submodel, which we embedded inside a discrete generation model of long-term population dynamics and evolutionary change (Elderd et al. 2008). The epizootic submodel thus uses the initial densities of hosts and pathogen particles and the initial average infection risk (as calculated by the long-term model) to calculate the fraction of hosts that become infected. The fraction infected is in turn used in the long-term model to update the number of hosts and pathogen particles and the average host infection risk. Although the model is constructed to describe gypsy moth–baculovirus interactions, it is general enough to describe many host–pathogen interactions for which hosts have discrete generations.

The epizootic submodel is a susceptible-exposed-infected-recovered (SEIR) model (Keeling and Rohani 2008), modified to allow for host variation in infection risk (Dwyer et al. 1997, 2002; Fuller et al. 2012):

\[
\frac{dS}{dt} = -\nu SP \left[ \frac{S(t)}{S(0)} \right] ^{V}, \tag{1}
\]

\[
\frac{dE_i}{dt} = \nu SP \left[ \frac{S(t)}{S(0)} \right] ^{V} - m\delta E_i, \tag{2}
\]

\[
\frac{dE_j}{dt} = m\delta E_{j-1} - m\delta E_j, \quad j = 2, \ldots, m, \tag{3}
\]

\[
\frac{dP}{dt} = m\delta E_m - \mu P. \tag{4}
\]

Here \(S\) and \(P\) are the densities of healthy hosts and pathogen-infected cadavers, respectively, so that \(I\) for infected host in the standard SEIR model is replaced by \(P\) for pathogen. Like most host–pathogen models, this model is fundamentally similar to Lotka–Volterra predator-prey models (Anderson and May 1992), except that host reproduction is instead described by the long-term model, as we will explain.

At field temperatures, gypsy moth larvae die an average of 16 days after consuming an infectious dose (Fleming-Davies et al. 2015), and so we allowed for a delay between infection and death. To do this, we included multiple classes of exposed but not yet infectious hosts \(E_j\), which produces a delay between infection and death that follows a gamma distribution. To explain why multiple exposed classes produce a gamma-distributed delay, we observe that if all hosts were in class \(j\), then the dynamics of class \(j\) would follow exponential decay \(dE_j/\ dt = -m\delta E_j\), implying that the time spent in class \(j\) is exponentially distributed with mean \(1/m\delta\). The time between infection and death is then the sum of \(m\) such exponentially distributed kill times, and a standard result from probability theory states that the sum of \(m\) exponential random variables follows a gamma distribution, in this case, with mean \(1/\delta\) and coefficient of variation (CV) \(1/m^{1/2}\) (Keeling and Rohani 2008).

Variation in infection risk modulates transmission through the term \(\bar{\nu}(S(t)/S(0))^V\), such that the initial mean transmission rate is \(\bar{\nu}\) and the squared CV of transmission rates is \(V\) (Dwyer et al. 2000). Because \(S(t) < S(0)\) for all \(t\), higher variation \(V\) thus reduces overall transmission. To explain why this is so, we note that an increase in \(V\) without a change in \(\bar{\nu}\) implies that there have been increases in the resistance of some individuals—and reductions in the resistance of others—in such a way that the mean does not change but overall variation increases. In this hypothetical situation, it is possible to show that the increases in resistance that have occurred in some individuals have bigger effects on the infection rate than do the decreases in resistance that have occurred in others (Anderson and May 1992).

The SEIR equations (1)–(4) are then used to calculate the fraction of hosts infected by the virus \(i(N_n, Z_n, \bar{\nu}_n) \equiv S(T)/S(0)\), where \(T = 8\) weeks is the length of the epizootic (Fuller et al. 2012). The fraction infected is in turn used in the long-term model to calculate the number of offspring produced by the surviving hosts, the number of infectious cadavers that survive the winter, and the change in infection risk that results from natural selection (for the derivation, see app. A). Because gypsy moths often experience high mortality from generalist predators and parasitoids (Gould et al. 1990; Elkinton et al. 1996), we also include a term that describes the fraction of hosts that survive predation (Dwyer et al. 2004):

\[
N_{n+1} = re^{cr}N_n \left[ 1 - \frac{2\omega N_n}{\omega^2 + N^2_n} \right] \left\{ 1 + s\bar{\nu}_n[1 - i(N_n, Z_n, \bar{\nu}_n)]^{V} \right\}, \tag{5}
\]

\[
Z_{n+1} = \phi N_n i(N_{n}, Z_{n}, \bar{\nu}_{n}) + \gamma Z_{n}, \tag{6}
\]

\[
\bar{\nu}_{n+1} = \bar{\nu}_n \left[ 1 - i(N_n, Z_n, \bar{\nu}_n) \right]^{V} \left\{ 1 + s\bar{\nu}_n(bV + 1)[1 - i(N_n, Z_n, \bar{\nu}_n)]^{V} \right\}, \tag{7}
\]

Host density \(N_{n+1}\) is the product of baseline fecundity \(r\), a stochasticity term \(c^r\), host density in the preceding generation \(N_n\) and the fraction surviving the epizootic \(1 - i(N_n, Z_n, \bar{\nu}_n)\). The stochasticity parameter \(c^r\) is a normal random variate with mean 0 and standard deviation \(\sigma\), representing the stochastic effects of weather (Williams et al. 1990). Generalist predation is represented by the term \(1 - 2\omega N_n/\omega^2 + N^2_n\), which describes host survival as determined by a type III functional response (Dwyer et al. 2004). To allow for the cost of resistance, we assume that fecundity at low host and pathogen densities increases linearly with increased infection risk \(\bar{\nu}_n\), according to \(1 + s\bar{\nu}_n[1 - i(N_n, Z_n, \bar{\nu}_n)]\). Changes in host density are thus partly driven by balancing...
selection, such that higher average infection risk \( \bar{\pi} \) leads to increased mortality but also to increased fecundity. The fecundity cost of resistance is reduced, however, when the infection rate \( i(N_n, Z_n, \bar{\pi}_n) \) is high, which is more likely when average infection risk is high or when host and pathogen densities are high. Increases in average infection risk or in host and pathogen densities thus reduce the fecundity cost but also increase host mortality.

Pathogen density \( Z_{n+1} \) is equal to the density of infectious cadavers produced in the preceding generation’s epizooic, \( N_n i(N_n, Z_n, \bar{\pi}_n) \), times the effective overwintering rate \( \phi \). We refer to \( \phi \) as the effective overwintering rate because it allows for both pathogen survival and the higher susceptibility of neonate larvae (Dwyer et al. 2000). Because neonates are orders of magnitude more susceptible than later-stage larvae, previous work has shown that \( \phi > 1 \) (Fuller et al. 2012; Fleming-Davies and Dwyer 2015). Longer-term pathogen survival is represented by the cadaver density \( Z_n \) times the long-term pathogen survival rate \( \gamma \) (Fuller et al. 2012).

Infection risk \( \bar{\pi}_{n+1} \) is equal to the preceding generation’s infection risk \( \bar{\pi}_n \), times the fraction infected \( i(N_n, Z_n, \bar{\pi}_n) \), so that higher virus mortality selects for reduced risk. The cost of resistance in contrast selects for higher risk, because fecundity at low densities increases linearly with increases in previous-generation risk, \( 1 + sv_n(bV + 1)[1 - i(N_n, Z_n, \bar{\pi}_n)]^{1/2} \), an effect that is again reduced by high infection rates. The symbol \( b \) represents the heritability of risk, so that \( bV \) is the fraction of overall variation in risk that is due to additive genetic factors, and high values of \( b \) strengthen the effects of selection. Changes in infection risk are thus determined by balancing selection, as in the case of host density, except that in contrast to host density, the change in infection risk does not depend on the baseline fecundity \( r \).

Population cycles in this model then occur because of the consumer-resource interaction between the host and the pathogen and because of natural selection on infection risk and fecundity (fig. 1). Low virus mortality drives increases in the density of high-fecundity, high-infection-risk genotypes, leading to increases in the density of the virus and increases in the average infection risk, which in turn cause virus epizootics that decimate the host population. Host density is then low for multiple host generations not just because of the pathogen and the generalist predators but also because the survivors of virus epizootics are more resistant to the pathogen and therefore have low fecundity. Eventually, however, reductions in the density of the virus and increases in the fecundity of the insect drive increases in the density of the host, leading to a new outbreak. Natural selection therefore combines with ecological factors to drive outbreaks. Qualitatively similar behavior occurs in models in which there is no generalist predator or in which the pathogen is replaced by a parasitoid (see app. B, available online).

Field Experiments to Estimate the Heritability and Cost of Reduced Infection Risk

Our experiments were designed to test the two key assumptions of our eco-evolutionary model: that infection risk is heritable and that there is a fecundity cost of reduced risk. Previous work produced preliminary evidence that infection risk is heritable without estimating heritability and without showing that there is a cost of reduced risk (Elderd et al. 2008). In testing whether infection risk is heritable and costly, we therefore also aimed to estimate the heritability parameter \( b \) and the cost parameters \( r \) and \( s \) to determine whether the values of these parameters fall in the right range to produce realistic model outbreaks. To estimate \( b \), we carried out a field transmission experiment using half-sibling families, which we created by taking advantage of the ability of male gypsy moths to mate with two to three different females, given 24 h of rest between matings (Páez et al. 2015). To estimate \( r \) and \( s \), we carried out a field transmission experiment using full-sibling families, which we produced by mating individual males to individual females.

We carried out our experiments in the field because overall infection risk depends on feeding behavior, which cannot be easily allowed for in laboratory experiments (Dwyer et al. 2005). Feeding behavior affects overall risk by determining exposure risk (Eakin et al. 2015), but overall risk is also affected by risk given exposure, which is instead determined by the insect’s immune system (Páez et al. 2015). Moreover, in the lab, both feeding behavior and immune system functioning show heritable variation that affects exposure risk and infection risk given exposure, respectively (Parker et al. 2011; Páez et al. 2015). By measuring overall infection risk, we thus allowed for heritable variation in both feeding behavior and immune system functioning. In previous work, inserting estimates of infection risk from this type of experiment into the SEIR equations (1)–(4) produced infection rates close to those seen in nature (Dwyer et al. 1997, 2008). In testing whether infection risk is heritable without estimating heritability and with-
Figure 1: Single realization of the model equations (5)–(7). Top panel shows changes in host $N_h$ (filled circles, black lines) and pathogen $Z_p$ (open circles, gray lines) densities, while bottom panel shows changes in average infection risk $i$ (filled circles, black lines) and in the fraction infected $i$ (open circles, gray lines). Here we use the median parameters calculated from our experimental data: heritability $b = 0.129$, baseline fecundity $r = 0.21$, cost-scaling parameter $s = 1.21$, and total variation $V = 2.97$. The death rate of exposed hosts $\delta = 1/16$ per day and the number of classes $m = 27$ are from Fleming-Davies et al. (2015). The generalist predation parameters $a = 0.96$ and $w = 0.14$ are from Dwyer et al. (2004). The pathogen overwintering parameter $\phi = 7.4$ and the long-term survival parameter $\gamma = 0.3$ are from Fuller et al. (2012). Long-term survival $\gamma$ is on the high end of reasonable values, but variation in $\gamma$ has only modest effects (app. B, available online).
\[ p_{ji} = e^{\log(\nu^*) + S_i + M_i + D_i}. \]  
Here \( \nu^* \) is the baseline infection risk. A basic result from quantitative genetic theory (Falconer and Mackay 1996) then states that heritability can be expressed in terms of the sire variance \( \sigma_s^2 \), the maternal variance \( \sigma_m^2 \), and the day variance \( \sigma_d^2 \):

\[ b = 4 \times \frac{\sigma_s^2}{(\sigma_s^2 + \sigma_m^2 + \sigma_d^2)}. \]

Estimating \( \sigma_s^2, \sigma_m^2, \) and \( \sigma_d^2 \) then required that we relate infection risk \( p_{ji} \) to a measurable quantity. To do this, we used \( p_{ji} \) in the SEIR equations (1)–(4) to calculate the fraction infected, as measured in our experiments. In practice, we first simplified the SEIR equations, because in our experiments, the mesh bags block enough sunlight that decay is 0 (Fuller et al. 2012) and the exposure period is short enough (7 days) that no new virus deaths occur. These two factors ensure that the density of virus does not change during the experiments, so that we can set \( dp/dt = 0 \) in equations (1)–(4), which in turn allows us to derive an expression for the fraction infected \( i \) in terms of \( p_{ji} \) (Dwyer et al. 2000):

\[ i = 1 - \left[ 1 + p_{ji} VP(0)T \right]^{-1/V}. \]

Here \( P(0) \) is the density of virus-infected cadavers and \( T \) is the length of time for which the experiment runs. Because in our experiments we varied the density of virus-infected cadavers, we were able to fit \( p_{ji} \) and \( V \) to our data, which made it possible to estimate the effects of sire, dam, and day on infection risk. To do this, we used a hierarchical Bayesian fitting routine (see app. B), such that the sire, maternal, and day effects were drawn from normal distributions with mean 0 and respective variances \( \sigma_s^2, \sigma_m^2, \) and \( \sigma_d^2 \). Once we had estimates of \( \sigma_s^2, \sigma_m^2, \) and \( \sigma_d^2 \), we inserted them into equation (9) to estimate the heritability \( b \) of infection risk. We also tested more directly whether there was meaningful heritable variation by using Akaike information criterion (AIC) analysis to choose between models that included sire, dam, and day effects in different combinations.

Inferences about transmission parameters are stronger in experiments that include a range of virus densities (Elderd et al. 2008), and so we used densities of 0, 25, 50, and 75 virus-infected cadavers per 40-leaf branch. Each branch was fed on by roughly 20 uninfected larvae, a density that falls within the range of gypsy moth densities observed at the start of baculovirus epizootics (Woods and Elkinton 1987). After larvae had fed freely on virus-contaminated foliage in the field, we reared them in individual diet cups in the lab until death or pupation. Infected larvae are usually easily recognizable because the virus has caused them to disintegrate, but in cases of uncertainty, we examined smears from dead larvae under a light microscope for the presence of occlusion bodies, which are easily visible at \( \times 400 \) (Woods and Elkinton 1987). Because we used an area in which gypsy moth densities were very low, and because all eggs were surface sterilized in dilute formalin (Dwyer and Elkinton 1995), infection rates on uninfected control foliage were low (heritability experiment: 12/209 = 5.7%; cost experiment: 6/371 = 1.6%), and so we do not consider controls further.

In our fitting routine, we assumed that the data are binomially distributed, which is equivalent to assuming that infection risk is independent across larvae within a branch, but in practice there may be correlations in infection risk between larvae that cause the observed variance to be higher than the binomial variance (McCullagh and Nelder 1989; see app. B; note that this is a nonissue for our analyses of the cost of resistance data, which instead rely on bootstrapping to quantify uncertainty). A standard way to test for such extrabinomial variation is to calculate the variance inflation factor, the ratio of the observed variance to what the corresponding binomial variance would be, given the sample size (Burnham and Anderson 2002). Variance inflation factors >4 suggest that there is substantial model inadequacy, but smaller values can instead be used to adjust the likelihood score, leading to a quasi-likelihood AIC (QAIC). In our experiments, we kept extrabinomial variation reasonably low by ensuring that all uninfected larvae had reached the fourth instar within 48 h of the beginning of the experiment (Elderd et al. 2008; see app. B), leading to a variance inflation factor of 2.27. We then divided the likelihood score of each model by 2.27 before calculating AIC values, thus using QAIC scores to choose the best model (Burnham and Anderson 2002).

In principle, sire, dam, and day effects could explain all the variation in infection risk so that we could allow \( V \rightarrow 0 \) in equation (10) (Dwyer et al. 2005), but there are also effects of small-scale spatial variation in virus density that do not depend on factors that vary between host families (Eakin et al. 2015). Because of this variation, allowing \( V \rightarrow 0 \) in equation (10) produced a model that gave a much worse fit to the data, and we therefore instead assumed \( V > 0 \).

To estimate the cost of reduced infection risk, we fit a version of the fraction-infected equation (10) to the data for each full-sibling group, and we regressed average female pupal weight in each group on the average infection risk in that group (Elderd et al. 2008). Because pupal weight is a good predictor of egg number (Páez et al. 2015; \( r^2 = 0.57 \)), a positive relationship between pupal weight and infection risk indicates that there is a fecundity cost of reduced risk. Because we measured fecundity in terms of pupal weight, however, estimating the cost parameters \( r \) and \( s \) required that we convert from pupal weight to egg number. We did this in two steps: first, by using data from Páez et al. (2015) to convert from pupal weight to egg mass weight, and second, by using data from Dwyer and Elkinton (1995) to convert from egg mass weight to egg number. An additional consideration, however, is that the model requires an estimate of net fecundity,
because early instars often die from starvation as they disperse from egg masses laid on bark to foliage at branch tips. To allow for such losses, we used data from Hunter and Elkinton (2000), who measured early instar survival in experimental gypsy moth populations. We then bootstrapped to estimate the net uncertainty arising from the three conversions (app. B).

Results

In the heritability experiment, infection rates and infection risk varied strongly across half-sibling families (fig. 2A, 2B), with 13% of the variation in risk explained by additive genetic variation ($b = 0.13$). QAIC scores were vastly better (lower) for models with sire effects (table 1), while the model with sire and dam effects was the only model with a substantial QAIC weight, indicating that dam effects were also strong but that day effects were weak. Because the models include random effects, it is almost impossible to assess goodness of fit through visual inspection of plots of the model predictions and the data versus virus densities, as is usually done with this kind of experiment (Elderd 2013), but in appendix B, we use a plot of observed versus predicted infection rates to demonstrate that the best model is quite accurate. For heritability $b$, the 95% highest posterior density (HPD) interval (the Bayesian equivalent of a 95% confidence interval) was broad but excluded values below $5 \times 10^{-4}$ (HPD = 0.0005, 0.51). Infection risk in the gypsy moth therefore has low but nonzero heritability, confirming the first key assumption of our eco-evolutionary model.

In the cost experiment, there was a noisy but positive relationship between female pupal weight and infection risk (fig. 2C), and the slope of the regression line was significantly $>0$, confirming that there is a cost of reduced risk (median intercept = 0.73, upper and lower 95th percentiles = 0.70, 0.80; median slope = 0.45, upper and lower 95th percentiles = 0.09, 0.56; for a description of how we bootstrapped the regression parameters to account for error in both infection risk and pupal weight, see app. B). In this regression, we included only survivors of virus exposure, which may have led to an underestimate of the cost, because of selection for low-risk/low-fecundity individuals within full-sibling groups. We therefore carried out a second regression (see app. B) in which we also included unexposed larvae from the lab, but the resulting regression line had identical slopes for exposed and unexposed individuals (intercepts in contrast were different, probably because lab-reared insects have artificially high growth (Páez et al. 2015); thus, in estimating costs, we used weights for field-reared insects. Irrespective of the analysis, our data show that female gypsy moths experience a fecundity cost of reduced infection risk, confirming the second key assumption of our eco-evolutionary model.

Because infection risk is heritable and costly, balancing selection must inevitably play a role in determining infection risk in the gypsy moth. It does not follow, however, that selection alters gypsy moth outbreak cycles, because realistic cycles in our model do not occur for all parameter values. To test whether our experimental parameters give realistic cycles, we therefore simulated the model using the experimental parameters to determine whether the parameterized model can reproduce data on gypsy moth outbreak cycles.

Because cyclic population dynamics are at least moderately sensitive to initial densities, which are almost always unknown, Kendall et al. (1999) argued that a useful way to compare model cycles to data is by comparing periods and amplitudes, which in the long run are insensitive to initial conditions. Accordingly, when we inserted the median parameter values calculated from our experiments into our model, the average cycle period was 7.4 years, and the average amplitude was 2.1 orders of magnitude (fig. 1), which compares well with observed periods of 5–9 years (Johnson et al. 2005) and observed amplitudes of 2–4 orders of magnitude (Skaller 1985; Williams et al. 1990; Jones et al. 1998). Moreover, variation in the parameter estimates has only modest effects on model periods and amplitudes (fig. 3). Finally, the model predicts that average infection risk (fig. 1) will fall in synchrony with falling population densities, a prediction that was confirmed by previous experiments that measured infection risk before and after a population crash (Elderd et al. 2008). Observational and experimental data thus support the model predictions, suggesting that natural selection plays an important role in gypsy moth outbreaks.

We also used our models to address the general issue of how heritability affects population stability. In continuous-time eco-evolutionary predator-prey models, stability is more likely when heritability is low (Schreiber et al. 2011), but in our model, stability is more likely when heritability is intermediate (fig. 3). In both types of models, high heritability causes such a rapid response to selection that risk undergoes large-amplitude fluctuations, driving large-amplitude fluctuations in densities. In our model, however, low heritability causes a slow response to selection that exacerbates the delayed density dependence that drives cycles, and so low heritability is mildly destabilizing instead of stabilizing. This destabilizing effect of low heritability also occurs in a model in which the pathogen is replaced by a parasitoid (see app. B), but the effect almost disappears in a model in which the epizootic continues until it has burned out as a result of low densities of susceptible hosts (Dwyer et al. 2000; see app. B).

The lack of a destabilizing effect in the burnout model is likely due to the less severe effects of delayed density dependence in that model. That is, when the epizootic proceeds to burnout, the pathogen responds more rapidly to density, reducing the delay between increases in host density and
Figure 2: A. Relationship between fraction infected and density of virus-infected cadavers in our heritability experiment. Gray lines show the data for each half-sibling family, while black circles show the average and 1 SE of the mean (table 1). Median values for $\bar{p}$ and $V$ are 0.80 (highest posterior density [HPD] interval = 0.43, 1.37) and 2.97 (HPD = 1.55, 4.59), respectively, which are close to values from previous experiments (Elderd et al. 2008). B, Variation in average infection risk $\bar{p}$ across half-sibling families, again suggesting that infection risk is heritable. C, Fecundity cost of resistance, as demonstrated by a positive relationship between infection risk and female pupal mass, a proxy for fecundity (Páez et al. 2015). Data underlying this figure are deposited in the Dryad Digital Repository: http://dx.doi.org/10.5061/dryad.8mv03 (Páez et al. 2017).
increases in pathogen density, in turn reducing the period and amplitude of outbreak cycles. Discrete generations nevertheless also appear to play a role, in that stability in the burnout model is at least slightly lower at low heritability. We therefore conclude that the effects of heritability on stability are modulated by the severity of the delayed density dependence, which in turn depends on the occurrence of discrete generations.

A second general point is that our model does not appear to have either the half-cycle lags (Yoshida et al. 2003) nor the cryptic population cycles (Yoshida et al. 2007) that have been observed in microcosm models. We have not been able to prove this result, but for almost all the parameter values in figure 3, the average lag was two generations or less (99.6% of 96,981 parameter sets that did not cause host or pathogen extinction), strongly suggesting that longer lags do not occur. Meanwhile, in outbreak data on several different insects, baculovirus infection rates likewise peaked shortly after host densities (Moreau and Lucarotti 2007), confirming the model prediction.

A full understanding of why our model behaves differently from microcosm models is beyond the scope of our work. We note, however, that half-cycle lags in microcosm models are more likely when costs are low, whereas in our model, reducing the cost-scaling parameter \( s \) had no effect on the lag (for \( s = 0.2 \), the lower bound on the HPD: 94.8% of 87,515 parameter sets had lags of two generations or less; for \( s = 0.2 \): 91.3% of 13,387 parameter sets; note that reducing \( s \) tends to increase the probability of host and/or pathogen extinction; see app. B). The key difference between our model and microcosm models therefore again appears to be that our model assumes discrete host generations, whereas microcosm models assume continuous reproduction (Hiltunen et al. 2014).

**Discussion**

In comparing the cycles in our models to cycles in North American gypsy moth populations, it is important to point out that Allstadt et al. (2013) showed that gypsy moth populations in New England cycled from 1943 to 1965 and from 1978 to 1996, with periods of noncyclic dynamics at other times (data points after 2009 were too few to permit testing, but a 2016 outbreak in New England suggests that cycling may have returned; G. Dwyer, personal observation). This lack of cycling is not necessarily inconsistent with our models, however, because Allstadt et al. showed that the dynamics seen in the New England data can be explained by a version of the Dwyer et al. (2004) model that includes stochastic fluctuations in generalist-predator density. Given that our model is basically the Dwyer et al. model plus natural selection, it seems likely that adding stochastic fluctuations in generalist-predator density to our model would allow it to reproduce the New England data, with the proviso that such a test is beyond the scope of our work.

Another important feature of Allstadt et al.’s work, however, is that they forced their version of the nonevolutionary Dwyer et al. model to show at least intermittent cycles, by using values of host variation \( V \) that are now known to

![Figure 3](image-url)
be unrealistically low (Elderd et al. 2008). As we have described, realistic values of $V$ eliminate cycles altogether in nonevolutionary insect-outbreak models, leading instead to a stable, point equilibrium. Given that Allstadt et al.’s approach has been followed in several other articles (Haynes et al. 2009a; Bjørnstad et al. 2010; Walter et al. 2015), a consideration of eco-evolutionary dynamics may have broad implications for our understanding of gypsy moth dynamics.

In focusing on the effects of natural selection, we nevertheless neglected other mechanisms known to affect gypsy moth outbreak cycles in North America. First, since 1989, the fungal pathogen *Entomophaga maimaiga* has often caused high mortality in North American gypsy moth populations when rainfall is high (Hajek 1999; Liebhold et al. 2013; Hajek et al. 2015). Indeed, the advent of *E. maimaiga* may provide an alternative explanation for the lack of outbreaks in New England since 1996 (Allstadt et al. 2013).

Second, we assumed that baculovirus transmission is unaffected by host-plant foliage quality, but defoliation-induced increases in hydrolyzable tannins in oaks (*Quercus* spp.) can greatly reduce variation in infection risk. Because of this effect, host-pathogen/induced-defense models can help explain variability in outbreak periods across forest types (Elderd et al. 2013). Although the models do not allow for outbreaks in forest types with low frequencies of oaks, where outbreaks have in fact been observed (Haynes et al. 2009b), and although the models are sensitive to the degree of clumping of oaks within the forest (Elderd et al. 2013), which has not been measured, it nevertheless seems likely that induced defenses also affect gypsy moth outbreaks.

Third, our models assume that the pathogen population is monomorphic, but the gypsy moth virus is at least moderately polymorphic and is also subject to trade-offs between fitness components (Fleming-Davies et al. 2015). Indeed, natural selection on the pathogen is perhaps the most important missing mechanism in our model, because it is most likely to lead to changes in dynamics (Dieckmann 2002), but allowing for pathogen evolution would require extensive experiments to estimate how host trade-offs vary with pathogen strain and how pathogen trade-offs vary with host family (Hudson et al. 2016). Simple coevolutionary host-parasitoid models have nevertheless shown that coevolutionary dynamics can also help drive insect outbreak cycles while also helping to maintain variation in the host (Sasaki and Godfray 1999), which in our models is assumed constant.

Allowing for these complications is an important next step in our work, but the evidence that we have provided for the effects of natural selection suggests that selection has at least some effect on outbreaks, confirming eco-evolutionary theory in a broader sense. Nevertheless, in the absence of outbreak-scale experiments, our work cannot provide conclusive proof of eco-evolutionary cycles, a problem that afflicts most studies of complex population dynamics (Turchin 2003). For eco-evolutionary models in particular, simultaneous collection of phenotypic and density data could provide additional evidence, but for now the combination of experimental and observational data that we have used here may provide the best support for eco-evolutionary theory.

The insect ecology literature suggests that eco-evolutionary dynamics may also play a role in population cycles of other forest defoliating insects (Anderson and May 1981; Myers 1988, 1993). First, laboratory observations of heritable variation and costs of resistance are common in insect-host-pathogen (Watanabe 1987; Boots and Begon 1993; Cory and Myers 2009) and host-parasitoid (Kraaijeveld et al. 2002) interactions. Although lab experiments are limited to measurements of risk given exposure, as we described, the results of our gypsy moth field experiments qualitatively match the results of gypsy moth lab experiments (Páez et al. 2015). The large number of previous lab studies showing heritable variation in insect-host-pathogen and host-parasitoid interactions therefore suggests that the effects of natural selection are widespread. Meanwhile, mortality due to baculoviruses and parasitoids is high in most cycling forest defoliators (Nealis 1991; Turchin 2003; Moreau and Lucarotti 2007), suggesting that selection pressure is often high enough to affect outbreak cycles. More broadly, because seasonality plays a role in many other host-pathogen interactions (Altizer et al. 2006), the effects of seasonal breeding in our models may be of general applicability, while the lack of half-cycle lags in our models means that a lack of such lags in general does not rule out eco-evolutionary cycles.

Baculoviruses are used as environmentally benign insecticides (Hunter-Fujita et al. 1998), which in the gypsy moth consists of the Gypchek spray product (Podgwaite et al. 1992). As is often the case with baculoviruses used in pest control, Gypchek plays only a modest role in gypsy moth control, because production costs are lower for the insecticide Btk, a naturally occurring bacterial toxin. Btk targets effectively all Lepidoptera, however, and so concerns over its environmental costs have led to increasing public demand for Gypchek (Boulton and Otvos 2004; Narciso 2014; Nolan 2015). Baculovirus spray products like Gypchek may therefore be used repeatedly in the future, and the resulting increases in infection rates may substantially alter insect outbreak cycles.

Reilly and Elderd (2014) tested this hypothesis by modifying the Dwyer et al. (2004) model to allow for repeated spraying, which showed that spraying dampens population cycles, effectively eliminating outbreaks. Our eco-evolutionary models, however, show that realistic outbreaks occur in nature for a broader range of parameters than in the Dwyer et al. model, and it may therefore be the case that resistance evolution will prevent the cycle-dampening effects of repeated baculovirus sprays, with the proviso that the evolution of increased resistance will likely raise average host densities. Extending our
models to allow for repeated baculovirus sprays may thus provide a better understanding of baculovirus use in pest control, and carrying out such an extension is therefore another next step. Our models thus support the growing consensus that eco-evolutionary theory has direct relevance for applied ecology (Menalled et al. 2016; Rozins and Day 2016).

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APPENDIX A

Derivation of the Eco-Evolutionary Host-Pathogen Model

Elderd et al. (2013) present a version of the Dwyer et al. (2004) model that also includes heritable changes in average infection risk and a trade-off between infection risk and fecundity. Their model, however, assumes that the phenotypic and genotypic distributions of infection risk are identical, as though heritability $b = 1$. Here we instead assume that $b < 1$, which significantly complicates the derivation of the model.

The initial steps in the Elderd et al. derivation are nevertheless useful. First, the pathogen equation (6) is unchanged from the original non-evolutionary insect-pathogen model of Dwyer et al. (2000), and therefore we do not consider it here. Second, by temporarily neglecting predation, we can integrate over the phenotypic distribution to derive an equation for the host population:

$$N_{n+1} = \int (r + rs) f_\nu(\nu) S(T) d\nu. \quad (A1)$$

Here $f_\nu(\nu)$ is the distribution of infection risk phenotypes $\nu$ and $S(T)$ is the host density, where both are calculated after an epizootic that lasts $T$ days. Host density is then calculated by allowing for disease-driven mortality (which determines the host density after the epizootic) and by including a fecundity cost of reproduction, as determined by the cost parameters $r$ and $s$. Meanwhile, Elderd et al. assumed that $T \to \infty$, and they used the alternative parameterization $r + \lambda \nu$ to describe the cost function, but the effects of these differences are minor compared with the complications that arise from assuming that $b < 1$.

We further follow the Elderd et al. derivation in assuming that the epizootic reduces the mean of the distribution of phenotypes but does not change the shape of the distribution, so that the squared coefficient of variation ($CV$) $V$ is constant. Given this constant-shape assumption, it is possible to show that the postepizootic mean is $\bar{\nu}_n [S(T)/S(0)]^b$, where $\bar{\nu}_n$ is the pre-epizootic mean (Dwyer et al. 2000). This assumption is also fundamental to the derivation of the susceptible-exposed-infected-recovered (SEIR) epizootic model (eqq. [1]–[4]), which is an approximation of a model that describes the entire distribution of phenotypes. The SEIR equations provide a highly accurate approximation of the full model if phenotypes follow a gamma distribution, but they are only moderately inaccurate for distributions with longer tails, such as a log-normal distribution. More importantly, for our purposes, the approximation means that both the SEIR model and the multigeneration model derived here can be simulated with only modest computational costs.

Continuing to follow the Elderd et al. derivation, we observe that the postepizootic host density is

$$S(T) = N_a [1 - i(N_a, Z, \bar{\nu}_n)], \quad (A2)$$

where $i(N_a, Z, \bar{\nu}_n)$ is calculated using equations (1)–(4). Including predation and stochasticity then gives equation (5), which is effectively the same as the host-density equation in the Elderd et al. model.

As we described, however, a crucial difference from the Elderd et al. model is that we allow the genotypic and phenotypic distributions to have different shape parameters $V$, which is necessary to allow for imperfect heritability. This assumption becomes important when we calculate how the average phenotype $\bar{\nu}_c$ changes as a result of mating, because in calculating the change in the phenotype, we average the fecundity costs over the genotypic distribution, whereas in the host density equation (1), we average over the phenotypic distribution. Specifically, we assume that the squared CV of the genotypic distribution is $bV$, where $V$ is the squared CV of the phenotypic distribution and $b$ is the heritability. Although other assumptions may also produce a reasonably simple model, this assumption has several advantages: (1) it ensures that genotypic variation is lower than phenotypic variation, as expected from quantitative genetic theory (Falconer and Mackay 1996); (2) it is consistent with previous approaches to adding quantitative genetic variation to predator-prey models (Abrams and Matsuda 1997); and (3) it produces a model that makes intuitive sense, as we now show.

To integrate over the genotypic distribution, we proceed as follows:

$$\bar{\nu}_{n+1} = \frac{\int \nu (r + rs) f_\nu(\nu) S(T) d\nu}{\int (r + rs) f_\nu(\nu) S(T) d\nu}. \quad (A3)$$
Here $f_c(n)$ is the postepizootic distribution of genotypes $n$, and $S(T)$ is again the host density after an epidemic that lasts $T$ days. To solve the integral, we again use the observation that the mean of the phenotypic distribution after the epizootic is $\bar{p}_n[S(T)/S(0)]^1$. Also, we use the assumption that the genotypic distribution has the same mean as the phenotypic distribution but that it has a squared CV equal to $bV$, with the proviso that for the genotypic distribution, the mean depends on the squared genotypic CV, not the phenotypic CV as in the host-density equation (1). We then have equation (7), which we repeat here for convenience:

$$\bar{p}_{n+1} = \bar{p}_n[1 - i(N_n, Z_n, \bar{p}_n)]^{bV} \left(1 + s\bar{p}_n(bV + 1)[1 - i(N_n, Z_n, \bar{p}_n)]^{bV}\right).$$

(A4)

This model makes intuitive sense, in that setting $b = 1$ again produces the Elderd et al. model, while setting $b = 0$ gives the classical model with no natural selection, as in Dwyer et al. (2000) and Dwyer et al. (2004).

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Gypsy moth larva eating an oak leaf. Photo credit: Alison Hunter.