Learning from Inflation Experiences*

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Abstract

How do individuals form expectations about future inflation? We propose that individuals overweight inflation experienced during their lifetimes. This approach modifies existing adaptive learning models to allow for age-dependent updating of expectations in response to inflation surprises. Young individuals update their expectations more strongly than older individuals since recent experiences account for a greater share of their accumulated lifetime history. We find support for these predictions using 57 years of microdata on inflation expectations from the Reuters/Michigan Survey of Consumers. Differences in experiences strongly predict differences in expectations, including the substantial disagreement between young and old individuals in periods of highly volatile inflation, such as the 1970s. It also explains household borrowing and lending behavior, including the choice of mortgages.

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1 Introduction

How do individuals form expectations about future inflation? The answer to this question is of central importance for both monetary policy and individual financial decisions. Policy makers would like to better understand the formation of inflation expectations to improve their inflation forecasts and resulting policy choices (Bernanke (2007)). Individuals’ perception of inflation persistence is likely to influence actual persistence (Roberts (1997), Orphanides and Williams (2005a), Milani (2007)). Inflation expectations influence the real interest rates perceived by individuals, which in turn affects financial decisions (e.g., in the housing market), real expenditure decisions, and macroeconomic outcomes (Woodford (2003)).

Despite a large volume of research, there is still little convergence on the best approach to model the dynamics of individuals’ inflation expectations (see Mankiw, Reis, and Wolfers (2003); Blanchflower and Kelly (2008)). In particular, the empirical heterogeneity in expectations remains hard to reconcile with existing models. Consider the time series of inflation expectations from the Reuters/Michigan Survey of Consumers in Figure 1.\footnote{We will discuss the data and the figure in detail in Section 3.1.} The figure plots the expectations of young (age below 40), middle-aged (age 40 to 60), and older individuals (age above 60) as deviations from the cross-sectional mean in each period. It reveals that the dispersion in beliefs can be large, reaching almost 3 percentage points (pp) during the high-inflation years of the 1970s and early 1980s. We also see repeated reversals in relative beliefs, with the young expecting higher inflation than the old following those years of high inflation, but having lower expectations in the late 1960s, mid-1990s, and late 2000s. These patterns are unexplained in existing models.

In this paper, we argue that personal experiences play an important role in shaping expectations. Individuals put more weight on realizations experienced during their lifetimes than on other available historical data. In the words of the Chairman of the Federal Reserve Paul Volcker during the high inflation of the late 1970s: “An entire generation of young adults has grown up since the mid-1960’s knowing only inflation, indeed an inflation that
Figure 1: Four-quarter moving averages of mean one-year inflation expectations of young individuals (below 40), mid-aged individuals (between 40 and 60), and old individuals (above 60), shown as deviations from the cross-sectional mean expectation. Percentage forecasts are available from the survey in periods shaded in light grey; they are imputed from categorical responses in the periods shaded in dark grey; and they are unavailable in unshaded periods.

has seemed to accelerate inexorably. In the circumstances, it is hardly surprising that many citizens have begun to wonder whether it is realistic to anticipate a return to general price stability, and have begun to change their behavior accordingly.”

We formalize this idea by building on existing adaptive learning algorithms in the macroeconomics literature in which agents estimate forecasting rules from historical data.\(^2\) We modify these algorithms to allow for learning from experience, by which we mean the possibility that agents are influenced more strongly by inflation realizations observed during their life-

\(^2\) See Volcker 1979, p. 888; quoted in Orphanides and Williams (2005b).

\(^3\) See Marcet and Sargent (1989); also Bray (1982), Sargent (1993), and Evans and Honkapohja (2001). In these models, agents use adaptive-learning algorithms as “rules of thumb” because of cognitive and computational constraints.
times than by other historical data. Specifically, we assume that individuals use experienced inflation rates to recursively estimate an AR(1) model of inflation. The key difference to standard adaptive learning models is that we allow the gain, i.e., the strength of updating in response to surprise inflation, to depend on age. Young individuals react more strongly to an inflation surprise than older individuals who already have a longer data series accumulated in their lifetime histories. As a result, different generations disagree about the outlook for inflation. Moreover, learning dynamics are perpetual. Beliefs keep fluctuating and do not converge in the long-run, as attention to distant historical data diminishes when old generations disappear and new generations emerge.

We estimate our model using 57 years of microdata on inflation expectations from the Reuters/Michigan Survey of Consumers (MSC). To identify the model parameters, we exploit the fact that learning from experience generates cross-sectional differences in expectations that vary over time depending on the evolution of each cohort’s inflation experiences. This identification from cross-sectional variation eliminates omitted macroeconomic variables or other unobserved common effects that could otherwise bias the estimation results. Furthermore, by focusing on cross-sectional differences, we can isolate the incremental explanatory power of individuals’ lifetime experiences over and above any common time-specific factors that individuals may pay attention to, such as, for example, published forecasts of professional forecasters. This is a key distinction from standard adaptive learning models that are typically fit to aggregate time-series of (mean or median) expectations.

Our estimation results show that past experiences have an economically important effect on inflation expectations. Individuals of different ages disagree significantly in their expectations of future inflation, and this heterogeneity is well explained by differences in their lifetime experiences of inflation persistence and the mean rate of inflation. The heterogeneity is particularly pronounced following periods of highly volatile inflation.

We also link the effect of experiences on beliefs to households’ financial decisions in the Survey of Consumer Finances. Disagreement about future inflation implies disagreement
about real interest rates. Consistent with this effect, households with higher experience-induced inflation expectations tilt their exposure towards liabilities (but not assets) with nominally fixed rates.\(^4\) The effects are economically large. For instance, a one percentage point difference in the learning-from-experience forecast of one-year inflation affects the mortgage balance by as much as a one-standard-deviation change in log income. Our findings complement the evidence in Piazzesi and Schneider (2012) that disagreement about future inflation between younger and older households in the late 1970s, as measured in the survey data, helps understand household borrowing and lending, portfolio choices, and prices of real assets. Our findings identify the source of this disagreement between generations, namely differences in their experiences.

Finally, we link learning from experience to aggregate expectations. We show that the cross-sectional averages of the experience-based forecasts closely match the time-series of the average survey expectations at each point in time. Furthermore, the average learning-from-experience forecast can be approximated quite closely by constant-gain learning with a gain parameter that is almost identical to the estimates that Orphanides and Williams (2005a) and Milani (2007) obtained by fitting adaptive learning models to aggregate data.\(^5\) The similarity is remarkable because our estimation of the learning-rule parameters does not utilize any information about the level of the average expectations or any aggregate data; it only uses information about cross-sectional differences between cohorts.

Learning from experience further provides a natural micro-foundation for constant-gain learning. While standard implementations of constant-gain learning motivate the down-weighting of past data with structural shifts and parameter drift, learning from experience offers an alternative reason: Memory of macroeconomic history is lost as new generations emerge whose subjective beliefs are shaped by relatively recent experiences. Our approach builds on the psychology evidence on the role of personal experiences and availability bias.

\(^4\) Relatedly, Inoue, Kilian, and Kiraz (2009) relate inflation to consumption decisions. Their emphasis is different, though. They utilize consumption behavior to calculate implicit inflation expectations.

\(^5\) Eusepi and Preston (2011) use a smaller gain to calibrate a stochastic growth model in which agents learn about wages and the return on capital.
(Tversky and Kahneman (1973)) rather than on the stochastic properties of macroeconomic variables to explain why data in the distant past is ignored.

The learning-from-experience mechanism also sheds light on one source of the dispersion in inflation expectations that is documented in Cukierman and Wachtel (1979) and Mankiw, Reis, and Wolfers (2003). This is an alternative to sticky information (Mankiw and Reis (2002)), heterogeneity based on gender and demographics (Bryan and Venkatu (2001)), or dispersion as a proxy for uncertainty (Zarnowitz and Lambros (1987), Bomberger (1996), Rich and Tracy (2010), and Bachmann, Elstener, and Sims (2013)). In our model, dispersion arises naturally due to differences in experiences.

Overall, our paper demonstrates that learning from experience plays a significant role in the formation of expectations. Our analysis builds on earlier work by Vissing-Jorgensen (2003) that points to age-related dispersion in individuals’ stock return and inflation expectations. Our findings also tie in closely with the evidence in Malmendier and Nagel (2011) that past stock- and bond-market return experiences predict portfolio choices of households. While these portfolio choice effects could arise from experience-induced changes in beliefs about asset returns or changes in risk preferences, the expectations data that we use in this paper here allow us to isolate the beliefs channel. Interestingly, our estimates of the weighting of past inflation experiences match very closely the estimates of the weighting of past asset-return experiences in Malmendier and Nagel (2011), even though the inflation expectations data is from a completely different data set. Further evidence for experience effects in financial decisions exists for mutual fund managers during the stock market boom and bust of the late 1990s (Greenwood and Nagel (2009)), for CEOs who grew up in the Great Depression (Malmendier and Tate (2005) and Malmendier, Tate, and Yan (2011)), and for investors participating in initial public offerings (Kaustia and Knüpfer (2008) and Chiang, Hirshleifer, Qian, and Sherman (2011)). Also related is the work by Fuster, Laibson, and Mendel (2010) and Fuster, Hebert, and Laibson (2011), who propose a model of “natural expectations” and demonstrate its ability to match hump-shaped dynamics in various economic time series.
The rest of the paper is organized as follows. Section 2 introduces our learning-from-experience framework and the estimation approach. Section 3 presents the data and the core results on learning from inflation experiences. Section 4 shows that learning-from-experience also helps understand household decisions about bond investing and mortgage borrowing. In Section 5, we look at the aggregate implications of our results. Section 6 concludes.

2 Learning from experience

Consider two individuals, one born at time $s$, and the other at time $s+j$. At time $t > s+j$, how do they form expectations of next period’s inflation, $\pi_{t+1}$? The essence of learning from experience is that they place different weights on recent and distant historical data, reflecting the different inflation histories of their lives so far. The younger individual, born at $s+j$, has experienced a shorter data set and is therefore more strongly influenced by recent data. As a result, the two individuals may produce different forecasts at the same point in time.

We model the perceived law of motion that individuals are trying to estimate as an AR(1) process, as, for example, in Orphanides and Williams (2005b):

$$\pi_{t+1} = \alpha + \phi \pi_t + \eta_{t+1}. \quad (1)$$

Individuals estimate $b \equiv (\alpha, \phi)'$ recursively from past data following

$$b_{t,s} = b_{t-1,s} + \gamma_{t,s} R_{t,s}^{-1} x_{t-1}(\pi_t - b'_{t-1,s} x_{t-1}), \quad (2)$$

$$R_{t,s} = R_{t-1,s} + \gamma_{t,s} (x_{t-1}' x_{t-1} \pi_t') - R_{t-1,s}, \quad (3)$$

where $x_t \equiv (1, \pi_t)'$. The recursion is started at some point in the distant past.\(^6\) The sequence of gains $\gamma_{t,s}$ determines the degree of updating cohort $s$ applies when faced with an inflation surprise at time $t$. For $\gamma_{t,s} = 1/t$, the algorithm represents a recursive formulation of an

\(^6\) We will see below that our empirical estimate of the parameter that determines $\gamma_{t,s}$ implies that past data is downweighted sufficiently fast so that initial conditions do not exert any relevant influence.
ordinary least squares estimation that uses all available data until time $t$ with equal weights (see Evans and Honkapohja (2001)). For constant $\gamma_{t,s}$, it represents a constant-gain learning algorithm with exponentially decaying weights. Our key modification of this standard adaptive learning framework is that we let the gain $\gamma$ depend on the age $t - s$ of the members of cohort $s$. Specifically, we consider the following decreasing-gain specification,

$$
\gamma_{t,s} = \begin{cases} 
\frac{\theta}{t-s} & \text{if } t-s \geq \theta \\
1 & \text{if } t-s < \theta,
\end{cases}
$$

where $\theta > 0$ is a constant parameter that determines the shape of the implied function of weights on past inflation experiences. We let the recursion start with $\gamma_{t,s} = 1$ for $t-s < \theta$, which implies that data before birth is ignored.\footnote{As will become clear, our econometric specification does allow individuals to use all available historical data when forming expectations, but isolates the incremental effect of data realized during individuals’ lifetimes. Also note that our results are robust to variations in the starting point for experience accumulation; see Online Appendix D.} This specification is the same as in Marcet and Sargent (1989) with one modification: the gain here is decreasing in age, not in time. The parameterization $\frac{\theta}{t-s}$ allows experiences earlier and later in life to have a different influence. For example, the memory of past episodes of high inflation might fade away over time as an individual ages. Alternatively, high inflation experienced at young age, and perhaps conveyed through the worries of parents, might leave a particularly strong and lasting impression.

Figure 2 illustrates the role of $\theta$. The top graph presents the sequences of gains $\gamma$ as a function of age (in quarters) for different values of $\theta$. For any $\theta$, gains decrease with age. This is sensible in the context of learning from experience: Young individuals, who have experienced only a small set of historical data, have a higher gain than older individuals, for whom a single inflation surprise has a weaker marginal influence on expectations. The graph also illustrates that higher $\theta$ implies that gains are higher and, hence, less weight is given to the more distant past. The latter implication is further illustrated in the bottom graph, which shows the implied weights on past inflation for a 50-year old individual. Our gain
Figure 2: Examples of gain sequences (top) and associated implied weighting of past data (bottom) for an individual who is 50 years (200 quarters) old. The top panel shows the sequence of gains as a function of age. The bottom panel shows the weighting of past data implied by the gain sequence in the top panel, with the weights for most recent data to the left and weights for early-life experiences to the right.
The parametrization is flexible in accommodating monotonically increasing, decreasing, and flat weights. For $\theta = 1$, all observations since birth are equal-weighted. For $\theta < 1$, observations early in life receive more weight, and for $\theta > 1$ less weight, than more recent observations. With $\theta = 3$, for example, very little weight is put on observations in the first 50 quarters since birth. The parametrization also allows for weight sequences that are virtually identical to those in Malmendier and Nagel (2011) (see Online Appendix A). Hence, we can compare the weights estimated from inflation expectations with those estimated from portfolio allocations.

The different weights that young and old individuals place on past observations give rise to cross-sectional heterogeneity in expectations. Given the perceived law of motion in equation (1), these between-cohort differences can arise from two sources: from differences in the perceived mean, $\mu = \alpha(1 - \phi)^{-1}$, and from differences in the perceived persistence, $\phi$, of deviations of recent inflation from the perceived mean.

In addition to past inflation experiences, we allow other information to affect expectations. Let $\pi_{t+1|t,s}$ be the forecast of period $t+1$ inflation made by cohort $s$ at time $t$. The experience-based component of individuals’ one-step-ahead forecast is obtained from (2) as $\tau_{t+1|t,s} = b_{t,s}'x_t$.\footnote{We capture the influence of information other than experienced inflation by assuming $\pi_{t+1|t,s} = \beta \tau_{t+1|t,s} + (1 - \beta) f_t$. (5)} We capture the influence of information other than experienced inflation by assuming

$$\pi_{t+1|t,s} = \beta \tau_{t+1|t,s} + (1 - \beta) f_t.$$ (5)

That is, the subjective expectation is a weighted average of the learning-from-experience component $\tau_{t+1|t,s}$ and an unobserved common component $f_t$ that is available to all individuals at time $t$. Examples are the opinion of professional forecasters, the representation of their opinions in the news media (e.g., as in Carroll (2003)), or even a component that is based on all available historical data. In either case, the coefficient $\beta$ captures the incremental contribution of life-time experiences $\tau_{t+1|t,s}$ to $\pi_{t+1|t,s}$ over and above these common components.

\footnote{In our estimation, we apply the AR(1) process in equation (1) to quarterly inflation data, while the survey data provides individuals’ forecasts of inflation over a one-year (i.e., four-quarter) horizon. Correspondingly, we employ multi-period learning-from-experience forecasts that we obtain by iterating, at time $t$, on the perceived law of motion in (1) using the time-$t$ estimates $b_{t,s}$. To economize on notation, we do not explicitly highlight the multi-period nature of the forecasts here.}
Thus, we do not assume that individuals only use data realized during their life-times, but isolate empirically the incremental effect of life-time experiences on expectations formation.

Empirically, we first estimate the following modification of equation (5):

\[ \tilde{\pi}_{t+1|t,s} = \beta \tau_{t+1|t,s} + \delta' D_t + \varepsilon_{t,s}, \]  

(6)

where \( \tilde{\pi}_{t+1|t,s} \) denotes measured inflation expectations from survey data. A vector of time dummies \( D_t \) absorbs the unobserved \( f_t \). We also add the disturbance \( \varepsilon_{t,s} \), which we assume to be uncorrelated with \( \tau_{t+1|t,s} \), but which is allowed to be correlated over time within cohorts and between cohorts within the same time period. It captures, for example, measurement error in the survey data and idiosyncratic factors influencing expectations beyond those explicitly considered here. We use this specification to jointly estimate \( \theta \) and \( \beta \) with non-linear least squares. (Recall that \( \tau_{t+1|t,s} \) is a non-linear function of \( \theta \).)

The presence of time dummies in equation (6) implies that we identify \( \beta \) and \( \theta \), and hence the learning-from-experience effect, from cross-sectional differences between the subjective inflation expectations of individuals of different ages, and from the evolution of those cross-sectional differences over time. The cross-sectional identification allows us to rule out confounds that can affect the estimation of adaptive learning rules from aggregate (mean or median) time-series data. With aggregate data, it is difficult to establish whether a time-series relationship between inflation expectations and lagged inflation truly reflects adaptive learning or some other formation mechanism (e.g., rational expectations) that happens to generate expectations with similar time-series properties. In contrast, the learning-from-experience model makes a clear prediction about the cross-section: Expectations should be heterogeneous by age, and for young people they should be more closely related to recent data than for older people. Moreover, we can estimate the gain parameter \( \theta \) that determines the strength of updating from this cross-sectional heterogeneity. This provides a new source of identification.
3 Inflation experiences and inflation expectations

We estimate the learning-from-experience effects by fitting the estimating equation (6) and the underlying AR(1) model to the MSC data on inflation expectations.

3.1 Data

We measure inflation experiences using long-term historical data on the consumer price index (CPI). In order to capture inflation experiences during the lifetimes of even the oldest respondents, we need inflation data stretching back 74 years before the start of the MSC survey data in 1953. We obtain the time series of inflation data since 1872 (until the end of 2009) from Robert Shiller’s website (see Shiller (2005)) and calculate annualized quarterly log inflation rates. Figure 3 shows annual inflation rates from this series.

The inflation expectations microdata is from the MSC, conducted by the Survey Research Center at the University of Michigan since 1953, initially three times per year, then quarterly.
We obtain the 1953-1977 surveys from the Inter-University Consortium for Political and Social Research (ICPSR) at the University of Michigan. From 1959 to 1971, the questions of the winter-quarter Survey of Consumer Attitudes were administered as part of the Survey of Consumer Finances (SCF), also available at the ICPSR. The data from 1978 to 2009 is available from the University of Michigan Survey Research Center. Online Appendix B provides more details.

In most periods, the survey asks both about the expected direction of future price changes (“up,” “same,” or “down”), and about the expected percentage of price changes. Since our analysis aims to make quantitative predictions, we focus on percentage expectations. For quarters in which the survey asks only the categorical question about the expected direction (20 out of 429 surveys), we impute percentage responses from the distribution of the categorical responses. (The imputation procedure is described in Online Appendix C.) Figure 1 in the introduction highlights the periods in which we have percentage expectations data in light grey, and the quarters in which the survey asks only the categorical questions in dark grey.

Since learning from experience predicts that inflation expectations differ by past experiences, we aggregate the data at the cohort level, i.e., by birth year. If multiple monthly surveys are administered within a quarter, we average the monthly means within the quarter to make the survey compatible with our quarterly inflation data. We restrict the sample to household heads aged 25 to 74 to ensure reasonable cohort sizes.

Figure 1 provides some sense of the variation in the data. It plots the average inflation expectations of young (below age 40), middle-aged (40 to 60), and older individuals (ages above 60), expressed as deviations from the cross-sectional mean expectation each period. To better illustrate lower-frequency variation, we plot the data as four-quarter moving averages. The figure shows that the dispersion across age groups reaches almost 3 pp during the high-inflation years of the 1970s and early 1980s. The fact that then-young individuals expected

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9 The cohort aggregation also alleviates concerns about digit preferencing and extreme outlier forecasts.
higher inflation is consistent with learning from experience: Their experience was dominated by high and persistent inflation, while the experience of older individuals also included the modest and less persistent inflation rates of earlier decades.

### 3.2 Baseline results

We now fit the estimating equation (6) and the underlying AR(1) model using nonlinear least squares on the cohort-level aggregate data. We relate the inflation forecasts in the MSC to learning-from-experience forecasts. We assume that the data available to individuals who are surveyed (at various points) during quarter $t$ are quarterly inflation rates until the end of quarter $t - 1$. Since the survey elicits expectations about the inflation rate over the course of the next year, but the (annualized) inflation rates that serve as input to the learning-from-experience algorithm are measured at quarterly frequency, we require multi-period forecasts from the learning-from-experience model. We obtain these multi-period forecasts by iterating on the perceived AR(1) law of motion from equation (1) at each cohort’s quarter-$t$ estimates of the AR(1) parameters $\alpha$ and $\phi$ (which are based on inflation data up to the end of quarter $t - 1$). Hence, the one-year forecast is the average of the AR(1) forecasts of quarter $t + 1$ to quarter $t + 4$ annualized inflation rates. To account for possible serial correlation of residuals within cohorts and correlation between cohorts within the same time period, we report standard errors that are robust to two-way clustering by cohort and calendar quarter.

Table 1 presents the estimation results. In the full sample (column (i)), we estimate a gain parameter $\theta$ of 3.044 (s.e. 0.233). Comparing this estimate of $\theta$ with the illustration in Figure 2 one can see that the estimate implies weights that are declining a bit faster than linearly.

The estimation results also reveal a strong relationship between the learning-from-experience forecast and measured inflation expectations. We estimate the sensitivity parameter $\beta$ to be 0.672 (s.e. 0.076), implying that, when two individuals differ in their learning-from-experience forecast by 1 pp, their one-year inflation expectations differ by 0.672 pp on average. To check whether the imputation of percentage responses from categorical responses affects our results,
we re-run the estimation excluding the imputed data. As shown in column (ii), the estimates remain very similar, with $\theta = 3.144$ (s.e. 0.257) and $\beta = 0.675$ (s.e. 0.079).

We have also re-estimated the coefficients accounting for age-specific differences in consumption baskets. These estimations address the concern that inflation differentials between age-specific consumption baskets could be an omitted variable that happens to be correlated with the differences in age-specific learning-from-experience forecasts that we construct. In other words, individuals might form inflation expectations based on (recent) inflation rates they observe in their age-specific consumption baskets. We re-run the regressions in Table 1 controlling for differences in inflation between consumption baskets of the elderly and overall CPI using the experimental CPI for the elderly series (CPI-E) provided by the Bureau of Labor Statistics. As reported in Online Appendix E, our results are unaffected. We also report a similar analysis with a gasoline price series to check whether age-specific sensitivity to gasoline price inflation drives the results. We find that this extension does not add explanatory power either, nor does it significantly affect our learning-rule parameter estimates. Hence, the cross-sectional differences that we attribute to learning-from-experience effects are not explained by differences in age-specific inflation rates.

The presence of the time dummies in these regressions is important. It rules out that the estimates pick up time-specific effects unrelated to learning from experience. If individual expectations were unaffected by heterogeneity in inflation experiences—for example, if all individuals learned from the same historical data applying the same forecasting rules—then $\beta$ would be zero. The effect of historical inflation rates, including “experienced” inflation rates, on current forecasts would be picked up by the time dummies. The fact that $\beta$ is significantly different from zero is direct evidence that differences in experienced-inflation histories are correlated with differences in expectations. The significant $\beta$-estimate also implies that recent observations exert a stronger influence on expectations of the young since the set of historical inflation rates experienced by the young that enters into the construction of the learning-from-experience forecast comprises only relatively few observations.
Table 1: Learning-from-experience model: Estimates from cohort data

Each cohort born at time $s$ is assumed to recursively estimate an AR(1) model of inflation, with the decreasing gain $\gamma_{t,s} = \theta/(t-s)$ and using quarterly annualized inflation rate data up to the end of quarter $t-1$. The table reports the results of non-linear least-squares regressions of one-year survey inflation expectations in quarter $t$ (cohort means) on these learning-from-experience forecasts. Standard errors reported in parentheses are two-way clustered by time (quarter) and cohort. The sample period runs from 1953 to 2009 (with gaps).

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<td>$f_t = \bar{\tau}_{t+1</td>
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Consider again the strong divergence in expectations between younger and older cohorts during the late 1970s and early 1980s displayed in Figure 1. The higher expectations of younger individuals are consistent with their experience being dominated by the high-inflation years of the 1970s, while older individuals also experienced the low-inflation years of the 1950s and 1960s. The discrepancy faded away only slowly by the 1990s, after many years of moderate inflation. Our model explains this difference as the result of younger individuals perceiving inflation to be (i) higher on average and (ii) more persistent when inflation rates were high until the early 1980s, but less persistent when inflation rates dropped subsequently. Our estimates of the gain parameter further imply that when individuals weight their accumulated life-time experiences, recent data receives higher weight than experiences earlier in
life, though experiences from 20 to 30 years ago still have some measurable long-run effects.

Figure 4 illustrates the extent to which learning-from-experience effects explain cross-sectional differences in inflation expectations. The figure shows both the raw survey data and the fitted values based on the estimates in column (i) of Table 1. For the purpose of these plots, we average inflation expectations and the fitted values within the same categories of the young (age < 40), middle-aged (40 to 60) and old (> 60) that we used in Figure 1, expressed as deviations from the cross-sectional mean expectation in each period (since our baseline estimation with time dummies focuses on cross-sectional differences.) To better illustrate lower-frequency variation, we plot the data as four-quarter moving averages. Fitted values are drawn as lines, raw inflation expectations are shown as diamonds (young), x’s (middle-aged), and filled circles (old). The plot shows that the learning-from-experience model does a good job of explaining the age-related heterogeneity in inflation expectations. In particular, it accounts to a large extent for the sizeable difference in expectations between young and old in the late 1970s and early 1980s, including the double-spike. It also captures all of the low-frequency reversals in the expectations gap between older and younger individuals.

Figure 5 illustrates the stronger response of younger individuals to recent data. We plot the time series of the persistence and mean parameters for each age group over the course of our sample period, using the $\theta$ estimate from Table 1, column (i). For the purpose of the plot, we average these perceived parameters again within the three age groups. The figure reveals that the perceived mean increased up to 1980 and then declined. The path of the perceived persistence is flatter but also increases initially and then declines dramatically after 2000. In both graphs, the assessments of younger individuals are much more volatile than those of older individuals. Our estimates also imply that at the end of the sample period, young individuals’ perceived inflation persistence is close to zero. That is, the expectations of young individuals at the end of the sample period are well-anchored, in the sense that they would be relatively insensitive to a short period of higher-than-expected inflation. As Mishkin (2007) and Bernanke (2007) argue, better anchoring of inflation expectations plays an important

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Figure 4: Comparison of four-quarter moving averages of actual and fitted one-year inflation expectations for individuals below age of 40, between 40 and 60, and above 60, shown as deviations from the cross-sectional mean expectation. The fitted values corresponds to column (i) in Table 1.

role in explaining why the dynamics of inflation have changed in recent decades. Figure 5 illustrates that learning-from-experience effects help understand the source of this improved anchoring. According to our estimates, older individuals’ perceived inflation persistence, however, is still substantially above zero.

To refine our understanding of the formation of inflation expectations, it would be useful to further analyze the exact transmission channel of experience effects. For example, how do experience effects depend on the cognitive ability to perceive price changes? How do they depend on the prices of items personally consumed versus the CPI? Does the strength of experience effects vary depending on macroeconomic conditions, e.g., inflation during boom times versus recessions?
Figure 5: Learning-from-experience AR(1) model estimates (with $\theta = 3.044$) of autocorrelation (top) and mean inflation (bottom) for individuals below age of 40, between 40 and 60, and above 60.
Our data is not rich enough to fully address these questions. At best, we can explore suggestive subsample variation. One such variation is in the starting point for personal experiences, which could be already before birth (in case of parental transmission) or after birth (when individuals start paying attention to price increases). As shown in Online Appendix Table OA.1, our findings are not sensitive to this variation. If we assume that inflation experiences start to accumulate 10 years before birth, the estimated gain parameter $\theta$ is higher, which implies a greater degree of downweighting of early experiences. As a result, the weights on pre-birth experiences are very small, and the specification effectively gets back to the implied weights of the baseline estimation. Conversely, if we assume that inflation experiences start to accumulate 10 years after birth, the estimated $\theta$ is lower, which puts more weight on early experiences and gets back to the implied weights in the baseline estimation. Evidently, our specification has sufficient flexibility to adapt to different starting points for experience accumulation without resulting in much difference in the fit of the model.

We have also explored whether inflation during booms and recessions leave systematically different imprints on individuals’ beliefs. In unreported results, we have divided our sample period into post-war boom, stagflation (1969Q4-1982Q4), Great Moderation (1983-2006), and Great Recession, fixing $\theta$ at the estimate of 3.044 from our main specification in Table 1(i). We do not detect systematic differences between boom- and recession-period inflation experiences. The stagflation period does generate a somewhat higher $\beta$-estimate ($\beta = 0.769$); but we also find a relatively high sensitivity parameter during the post-war boom, $\beta = 0.688$.

3.3 Exploring the common factor

Our main estimating equation in (6) includes time dummies in order to identify the learning-from-experience effect with a test of the null hypothesis $\beta = 0$. The specification also allows us to estimate $\theta$ purely from cross-sectional differences, removing potentially confounding unobserved common factors in expectations. We now ask whether learning-from-experience forecasts can explain not only cross-sectional differences but also the level of expectations.
We also explore the nature of the common factor $f_t$ in the underlying structural model (5), which is absorbed by the time dummies in our estimating equation (6). For both steps, we re-estimate equation (6) without the time dummies and intercept, but instead with observable proxies for $f_t$.

First, we consider the possibility that $f_t$ captures individuals’ tendency to rely, to some extent, on the opinions of professional forecasters that get disseminated in the media. We specify $f_t$ as the sum of the Survey of Professional Forecasters (SPF) forecast in quarter $t - 1$ and a noise term $\eta_t$ that is uncorrelated with the SPF forecast and the learning-from-experience forecast. Equation (5) becomes

$$
\pi_{t+1|t,s} = \beta \tau_{t+1|t,s} + (1 - \beta) SPF_{t-1} + (1 - \beta) \eta_t.
$$

Since this estimating equation does not include time dummies, it utilizes information about the levels of inflation expectations, not only cross-sectional differences. The estimation results are shown in column (iii) of Table 1. In the estimation, we remove the imputed data from the sample, as the imputation was only designed to capture cross-sectional differences, not levels. The number of observations is further slightly lower than in column (ii) because SPF forecasts are not available in a few quarters early in the sample. As before, we work with one-year forecasts in the survey data, so we use the corresponding four-quarter, iterated version of the learning-from-experience forecast.

As column (iii) shows, replacing the time dummies with the SPF has little effect on the estimate of $\beta$ compared with column (ii). With 3.976 (s.e. 0.612), the estimate of $\theta$ is higher, but the implied weighting of past inflation experiences remains quite similar to the weighting implied by the estimates in columns (i) and (ii). The standard error of $\beta$ also remains similar while the standard error of $\theta$ doubles. The noisier $\theta$ estimate reflects that the removal of the time dummies leaves the noise term $\eta_t$ in (7) in the regression residual. This effect of the noise term can also be seen in the increase in RMSE compared with columns (i) and (ii).\footnote{We focus on the RMSE since this regression is run without intercept, and hence the adjusted $R^2$ is not a}
Nevertheless, the fact that the $\beta$-estimate in columns (iii) is virtually identical to those in columns (i) and (ii) indicates that SPF forecast captures much of the common component of $f_t$ that could be correlated with the learning-from-experience forecast.

Another possibility is that the common component $f_t$ in individuals’ beliefs is the result of a social learning process in which individuals with different experienced inflation histories share their opinions, and, as a result, their beliefs have a tendency to converge to the average belief, as in DeGroot (1974). To explore this possibility, we represent $f_t$ as the mean learning-from-experience forecast across all age groups, which we denote as $\bar{\tau}_{t+1|t}$, and a noise term:

$$\pi_{t+1|t,s} = \beta \tau_{t+1|t,s} + (1 - \beta) \bar{\tau}_{t+1|t} + (1 - \beta) \eta_t. \quad (8)$$

Column (iv) reports the results. The estimates are almost identical to those in column (iii). Evidently, the average learning-from-experience forecast is very close to the SPF forecast and it, too, does a good job in absorbing the component of $f_t$ that could be correlated with the learning-from-experience forecast. As in column (iii), though, $\theta$ is estimated with substantially higher standard errors than in the specifications with time dummies.

In a last estimation, shown in column (v), we explore the fit of regression model (8) after fixing $\theta$ at its more precise estimate from column (i), $\theta = 3.044$, which was more cleanly identified due to the inclusion of time dummies. This specification allows us, on the one hand, to track both the cross-sectional and the time-series variation in inflation expectations induced by learning from experience, and, on the other hand, to eliminate the potential confounds affecting the (noisier) estimates of $\theta$ in columns (iii) and (iv). We find that the estimate of $\beta$ is almost unchanged, and there is little deterioration in fit. The RMSE is only slightly higher than in column (iv). We will use this specification below in Section 5 when we explore time-variation in inflation expectations and the aggregate implications of learning from experience.

useful measure of fit.
4 Inflation experiences and financial decisions

So far our results show that differences in inflation experiences generate differences in beliefs about future inflation. To what extent do these differences in beliefs affect the economic decisions of households? Since differences in inflation expectations generate disagreement about real rates of return on assets and liabilities with nominally fixed rates, households with higher experience-based inflation expectations should be more inclined to borrow and less inclined to invest at nominally fixed rates than households with lower experience-based inflation expectations. We test this prediction by estimating the regression equation

\[ y_{t,s} = \beta_1 \tau_{t+1|t,s} + \beta_2 X_{t,s} + \beta_3 A_{t-s} + \beta_4 D_t + \xi_{t,s}, \]  

(9)

where \( y_{t,s} \) is a measure of either fixed-rate liabilities or fixed-rate assets held at time \( t \) by people born in year \( s \), and \( \tau_{t+1|t,s} \) denotes the learning-from-experience forecast of inflation, constructed with the \( \theta \) estimate from Table 1, column (i). \( X_{t,s} \) is a vector of cohort characteristics, \( A_{t-s} \) a vector of age dummies, and \( D_t \) a vector of time dummies. We also add the disturbance \( \xi_{t,s} \), which we allow to be correlated between cohorts within the same time period.

To estimate the effect of learning from inflation experiences on financial decisions, we turn to a different data source, the Survey of Consumer Finances (SCF), which provides detailed information on households’ financial situation. We rely on the data set constructed by Malmendier and Nagel (2011), which comprises both the modern triennial SCF from 1983-2007 and older versions of the SCF from 1960-1977. For comparability with our baseline estimation in Table 1, we aggregate the microdata again at the cohort-level. In each survey wave, we construct per-capita numbers of debt and bond holdings (in September 2007 dollars), as well as income and net worth, for all birth-year cohorts. We then run the estimation on

\(^{11}\)Cohort-level aggregation is common in the household finance literature. It also serves to minimize the influence of outliers and erroneous zeros when analyzing ratios such as \( \log(\text{debt/income}) \), or regressing \( \log(\text{debt}) \) on \( \log(\text{income}) \). For completeness, and as a robustness check, we show household-level regressions in Online Appendix H, Tables OA.4 and OA.5, with similar or even stronger results.
Table 2: Survey of Consumer Finances: Summary statistics of cohort aggregates

The SCF sample includes 19 surveys during the period from 1960 to 2007, and 18 of those have information on holdings of long-term bonds. The data on borrowing and bond holdings is aggregated to per-capita numbers at the cohort level.

<table>
<thead>
<tr>
<th>Log fixed-rate mortgages (i)</th>
<th>Log long-term bonds (ii)</th>
<th>Log new fixed-rate mortgages (iii)</th>
<th>Log new variable-rate mortgages (iv)</th>
<th>Log income (v)</th>
<th>Log net worth (vi)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mean</td>
<td>9.76</td>
<td>8.61</td>
<td>6.71</td>
<td>3.39</td>
<td>10.91</td>
</tr>
<tr>
<td>Std.dev.</td>
<td>1.29</td>
<td>1.85</td>
<td>3.45</td>
<td>3.72</td>
<td>0.41</td>
</tr>
<tr>
<td>p10</td>
<td>8.43</td>
<td>6.26</td>
<td>0.00</td>
<td>0.00</td>
<td>10.42</td>
</tr>
<tr>
<td>Median</td>
<td>10.05</td>
<td>8.73</td>
<td>8.21</td>
<td>0.00</td>
<td>10.93</td>
</tr>
<tr>
<td>p90</td>
<td>10.92</td>
<td>10.87</td>
<td>9.50</td>
<td>8.30</td>
<td>11.42</td>
</tr>
<tr>
<td>Sample</td>
<td>Full</td>
<td>Full</td>
<td>≥ 1983</td>
<td>≥ 1983</td>
<td>Full</td>
</tr>
</tbody>
</table>

Table 2 provides summary statistics for the key variables in our analysis. Households’ main fixed-rate liability is mortgage debt, shown in column (i). Prior to 1983, the SCF often provides mortgage information only for households’ primary residence, not for other real estate owned by the household. To construct a measure that is consistent over time, we focus on fixed-rate mortgage balances secured by the primary residence. On the asset side, we measure households’ holdings of long-term bonds, shown in column (ii). This variable includes holdings through mutual funds and defined contribution (DC) accounts.

We also tabulate separately the summary statistics for mortgages that are newly taken out or refinanced in the year a household is surveyed. (The survey is carried out from June to September.) We split these (re-)financing volumes into “new fixed-rate” and “new variable-rate” mortgages, as shown in columns (iii) and (iv). We use these alternative outcome variables when focusing on the flow rather than the level of liabilities. The information about fixed or variable rates is available only starting in 1983; however, variable-rate mortgages
were largely non-existent in the U.S. prior to the 1980s (see Green and Wachter (2005)).

Finally, columns (v) and (vii) show family income and net worth, which we use as control variables. In the years before 1983, the coverage of household assets in the \textit{SCF} is not as comprehensive as from 1983 onwards. For the sake of comparability over time, our measure of net worth uses only categories of assets and liabilities that are available in all survey waves: financial assets, defined as stocks, bonds, and cash, including mutual funds and DC accounts, plus equity in the households’ primary residence.

Table 3 presents the estimation results. In each column we regress the log of the respective cohort-level per-capita nominal position on the learning-from-experience inflation forecast, constructed using the estimate of $\theta = 3.044$ from Table 1.(i). We control for the logs of per-capita income and net worth. All regressions include dummies for the survey year and for age.

Column (i) shows that households’ fixed-rate mortgage positions are positively related to the learning-from-experience inflation forecast. The point estimate of the coefficient is more than four standard errors above zero. As predicted, households whose experiences lead them to expect higher inflation and, hence, lower real interest rates take on more fixed-rate liabilities. The magnitude of the effect is large: a one percentage point difference in the learning-from-experience forecast corresponds to a 0.35 change in the log of the fixed-rate mortgage balance, which is between a third and a quarter of a standard deviation of the dependent variable (see Table 2). This magnitude is comparable to the variation associated with a one-standard-deviation change in log income.

In column (ii), we estimate the effect of inflation experiences on households’ nominal bond positions. Here, the sign of the coefficient is negative, indicating that households with higher learning-from-experience forecasts of inflation invest less in long-term bonds. The coefficient estimate is on the same order of magnitude as the coefficient in column (i), but not statistically significant. Taken together, the results in column (i) and (ii) show that households with higher learning-from-experience inflation forecasts tilt their exposure to fixed-rate liabilities rather
Table 3: Inflation experiences and household nominal positions

The SCF sample includes 19 surveys during the period from 1960 to 2007, and 18 of those have information on holdings of long-term bonds. The data is aggregated to per-capita numbers at the cohort level. Each cohort is assumed to recursively estimate an AR(1) model of inflation, with $\theta = 3.044$, as in Table 1.(i). We use the resulting learning-from-experience forecast of inflation to explain log fixed-rate mortgage borrowing and log long-term bond holdings in OLS regressions. Log mortgage borrowing in columns (v) and (vi) comprises only loans taken out or refinanced in the year in which the survey was carried out. Standard errors reported in parentheses are clustered by time period.

<table>
<thead>
<tr>
<th></th>
<th>Fixed-rate mortgages (i)</th>
<th>Long-term bonds (ii)</th>
<th>Fixed-rate mortgages (iii)</th>
<th>Long-term bonds (iv)</th>
<th>New fixed-rate mortgages (v)</th>
<th>New variable-rate mortgages (vi)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Learn.-from-exp. forecast</td>
<td>35.27 (8.39)</td>
<td>-20.56 (13.74)</td>
<td>26.77 (4.47)</td>
<td>-9.07 (6.92)</td>
<td>132.71 (25.08)</td>
<td>-42.82 (55.57)</td>
</tr>
<tr>
<td>Log income</td>
<td>0.92 (0.16)</td>
<td>0.45 (0.25)</td>
<td>0.60 (0.13)</td>
<td>0.02 (0.13)</td>
<td>1.23 (1.9)</td>
<td>2.60 (1.29)</td>
</tr>
<tr>
<td>Log net worth</td>
<td>-0.10 (0.15)</td>
<td>1.09 (0.13)</td>
<td>0.18 (0.06)</td>
<td>1.18 (0.10)</td>
<td>-0.56 (0.69)</td>
<td>-1.79 (0.94)</td>
</tr>
<tr>
<td>Time dummies</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Age dummies</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Sample</td>
<td>Full</td>
<td>Full</td>
<td>$\geq 1983$</td>
<td>$\geq 1983$</td>
<td>$\geq 1983$</td>
<td>$\geq 1983$</td>
</tr>
<tr>
<td>Adj. $R^2$</td>
<td>0.617</td>
<td>0.852</td>
<td>0.856</td>
<td>0.915</td>
<td>0.485</td>
<td>0.243</td>
</tr>
<tr>
<td>#Obs.</td>
<td>950</td>
<td>900</td>
<td>450</td>
<td>450</td>
<td>450</td>
<td>450</td>
</tr>
</tbody>
</table>

than assets. As shown in columns (iii) and (iv), we obtain similar results when restricting the sample period to 1983-2007, when the SCF data is of higher quality.

In columns (v) and (vi), we refine the analysis in two ways. First, we focus on mortgages that have recently been taken out or refinanced, rather than the total mortgage positions of households. The flow variable addresses concerns about the “stickiness” of mortgage positions: They include loans taken out many years ago. Once a household has taken out a mortgage and bought a house, the mortgage balance cannot easily be adjusted. While a household can take out a second mortgage, buy a bigger house, or (since the 1980s) refinance
with a variable-rate mortgage, there are frictions and indivisibilities that are likely to generate substantial stickiness. In contrast, for the volume of newly taken out or refinanced mortgages, this stickiness plays less of a role. Using the more recent data on re-financing, we are also able to distinguish between fixed-rate and variable-rate mortgages. According to our hypothesis, households with higher learning-from-experience forecasts of inflation should be more likely to take out a fixed-rate mortgage, and less likely to take out a variable-rate mortgage.

The results in column (v) and (vi) are consistent with this prediction. We find that households with high learning-from-experience forecasts of inflation are significantly more likely to take out new fixed-rate mortgages and to re-finance at fixed rates. A one percentage point difference in the learning-from-experience forecast corresponds roughly to a 1.33 change in the log of the fixed-rate mortgage balance, which is more than a third of a standard deviation of the dependent variable according to Table 2. We also find that experience-based inflation expectations are negatively related to the volume of new variable-rate mortgages, but the estimated coefficient in column (vi) is not statistically significant, and the point estimate is small—a one percentage point difference in the learning-from-experience forecast corresponds only to about a ninth of the standard deviation of the dependent variable.

Overall, the findings in this section confirm that learning from inflation experiences affects not only the expectations of individuals but also their asset allocation to long-term bonds and their mortgage financing decisions. The latter is, for many households, among the most important financial decisions they make.

5 Aggregate implications

Our analysis so far has focused on using heterogeneity in inflation experiences to explain heterogeneity in expectations and financial decisions. We now test whether learning from experience also helps explain aggregate dynamics in inflation expectations. We show that experience-based forecasts aggregate to average forecasts that closely resemble those from constant-gain algorithms in the existing literature, which have been shown to explain macroe-
economic time series data. We argue that learning from experience provides a micro-underpinning for adaptive-learning models, but offers conceptual and econometric advantages in the identification of the structural parameters that pin down the learning rule.

5.1 Approximating constant-gain learning

We start from the model in (8), which allows for social learning. Averaging across all cohorts $s$ in each period $t$, and denoting cross-sectional averages with an upper bar, we get

$$\bar{\pi}_{t+1|t} = \bar{\tau}_{t+1|t} + (1 - \beta) \eta_t. \quad (10)$$

Thus, apart from the noise term $\eta_t$, the mean expectation is pinned down by the mean learning-from-experience forecast across all age groups, $\bar{\tau}_{t+1|t}$. This mean learning-from-experience forecast behaves approximately as if it was generated from a constant-gain learning algorithm: While individuals update their expectations with decreasing gain, i.e., older individuals react less to a given inflation surprise than younger individuals, the average gain each period is constant (as long as the weight on each age group is constant over time.) The average learning-from-experience forecast is an approximation, rather than an exact match, of a constant-gain learning forecast because the means of the surprise terms in (2) and (3) are not exactly identical to the surprises arising in a constant-gain learning algorithm.

Figure 6 illustrates how well the approximation with a constant gain works. The figure compares the weights on past inflation implied by learning-from-experience with $\theta = 3.044$ (from Table 1, column (i)) and averaged across all age groups (solid line) with the weights implied by constant-gain learning (dashed line). We use the constant gain for which the constant-gain algorithm minimizes the squared deviations from the average learning-from-experience weights. The result is a constant gain of $\gamma = 0.0180$.

The figure shows that the weighting of past data is very similar. It is noteworthy that the deviation-minimizing constant gain $\gamma = 0.0180$ is virtually the same as the gain required to match aggregate expectations and macro time-series data. For example, Milani (2007) reports
Figure 6: Comparison of implied mean weights on past inflation observations under learning-from-experience and constant-gain learning. The learning-from-experience weights for each lag are calculated for each age at the point estimate $\theta = 3.044$ from Table 1, column (i), and then averaged across all ages from 25 to 74 (equally weighted). The weights implied by constant-gain learning are calculated with gain $\gamma = 0.0180$, which minimizes squared deviations from the learning-from-experience weights shown in the figure.

that an estimate of $\gamma = 0.0183$ provides the best fit of a DSGE model with constant-gain learning to macroeconomic variables. Orphanides and Williams (2005a) choose a gain of 0.02 to match the time series of inflation forecasts from the SPF. Our estimate of $\gamma$ is, instead, chosen to match the weights implied by the $\theta$ that we estimated purely from cross-sectional heterogeneity. We did not employ aggregate expectations data and we did not try to fit future realized inflation rates. Hence, our estimates of $\theta$ from between-cohort heterogeneity provide “out-of-sample” support for values of the gain parameter around $\gamma = 0.0180$ that are necessary, according to the prior literature, to fit time-series data. We conclude that the aggregate implications of learning from experience for the formation of expectations are very
similar to those of constant-gain learning algorithms, which have been used successfully to 
explain macroeconomic dynamics (e.g., Sargent (1999), Orphanides and Williams (2005a), 
Milani (2007)), but with the added benefit of empirical consistency with between-cohort 
heterogeneity.

5.2 Explaining aggregate expectations

We now test directly how well the learning-from-experience model matches aggregate survey 
expectations. Figure 7 shows both the time path of averages from the raw survey data 
(circles) and average experience-based forecasts (solid line), as before based on \( \theta = 3.044 \). 
Since our imputation of percentage responses only targeted cross-sectional differences, but 
not the average level of percentage expectations, we omit all periods in which we only have 
categorical inflation expectations data.

It is apparent from the figure that the average learning-from-experience forecasts closely 
track average expectations. The good match is by no means mechanical. As discussed above, 
our estimation of \( \theta \) uses only cross-sectional differences in expectations, but no information 
about the level of the average expectation. The time path for average expectations generated 
by the \( \theta \) that best fits cross-sectional differences could easily have failed to match average 
expectations. As the figure shows, though, the two time paths match well.

Figure 7 also shows the time path of constant-gain-learning forecasts, using \( \gamma = 0.0180 \) 
from Figure 6. Not surprisingly, given that \( \gamma \) was chosen to minimize the distance in the 
implied weights, the forecasts are almost indistinguishable. This illustrates further that, at 
the aggregate level, the learning-from-experience expectations formation mechanism can be 
approximated well with constant-gain learning.

Finally, we compare the average learning-from-experience forecast to a sticky-information 
forecast. Sticky information, as in Mankiw and Reis (2002) and Carroll (2003), induces stick-
iness in expectations, and it is possible that our estimation of the learning-from-experience 
rule is picking up some of this stickiness in expectations. We calculate sticky-information
inflation expectations as in Carroll’s model as a geometric distributed lag of current and past quarterly SPF forecasts of one-year inflation rates. Note that the sticky-information model can only be estimated from 1977Q4 on, when the SPF data with all the required lags is available (129 observations, compared to 173 observations for full sample.) We set the weight parameter $\lambda = 0.25$ as in Mankiw and Reis (2002) (and similar to $\lambda = 0.27$ estimated in Carroll (2003)). The resulting sticky-information forecast is shown as the short-dashed line in Figure 7. The graph illustrates that the learning-from-experience model helps to predict actual forecast data better than the sticky-information model. For example, learning-from-experience forecasts track actual forecasts more closely during the peak around 1980 and also during the 2000s, though both models fail to match a few highly positive expectations.

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\(^{12}\) We use the one-year inflation forecasts that the SPF constructs from median CPI inflation forecasts for each of the four quarters ahead. Before 1981Q3, when the CPI inflation forecast series is not available, we use the GDP deflator inflation forecast series.
Table 4: Explaining mean inflation expectations

OLS regressions with quarterly data from 1973Q1 to 2009Q4 (with gaps). The dependent variable is the forecast of one-year inflation made during quarter $t$, averaged across all cohorts. Newey-West standard errors (with five lags) are shown in parentheses.

<table>
<thead>
<tr>
<th></th>
<th>(i)</th>
<th>(ii)</th>
<th>(iii)</th>
<th>(iv)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Learning-from-experience</td>
<td>0.887</td>
<td>0.695</td>
<td></td>
<td></td>
</tr>
<tr>
<td>forecast</td>
<td>(0.120)</td>
<td>(0.132)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Constant-gain-learning</td>
<td>0.931</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>forecast</td>
<td>(0.137)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Sticky-information forecast</td>
<td></td>
<td>0.878</td>
<td>0.390</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>(0.199)</td>
<td>(0.150)</td>
<td></td>
</tr>
<tr>
<td>Intercept</td>
<td>0.009</td>
<td>0.008</td>
<td>0.011</td>
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</tr>
<tr>
<td></td>
<td>(0.005)</td>
<td>(0.005)</td>
<td>(0.006)</td>
<td>(0.005)</td>
</tr>
<tr>
<td>Adj. $R^2$</td>
<td>0.564</td>
<td>0.555</td>
<td>0.602</td>
<td>0.715</td>
</tr>
<tr>
<td>#Obs.</td>
<td>173</td>
<td>173</td>
<td>129</td>
<td>129</td>
</tr>
</tbody>
</table>

towards the end of the last decade.

We evaluate the statistical significance of this graphical impression in Table 4. We regress average survey expectations on the average forecast predicted for the same quarter under the various models. For the learning-from-experience model (column (i)), the estimated coefficient is 0.887, less than one standard error away from the model prediction of 1. With 56.4% the adjusted $R^2$ is high. This confirms the visual impression that experience-based forecasts closely track the actual average survey expectations. The constant-gain forecast in column (ii) produces almost identical results, not surprisingly given its similarity with $\bar{\tau}_{t+1|t}$ when using $\gamma = 0.0180$. The sticky-information coefficient in column (iii) is only a bit lower and noisier, and the adjusted $R^2$ is slightly higher. Note, though, that the learning-from-experience model, re-estimated over the shorter sub-sample from column (iii), yields an even higher adjusted $R^2$, 67.2%, and a learning-from-experience coefficient of 1.039 (s.e. 0.114) that is even closer to 1. Most importantly, if we include both the sticky-information and the experience-based forecast (column (iv)), the coefficient on the experience-based fore-
cast becomes only slightly smaller, but remains large (also relative to the sticky-information coefficient) and significant. Hence, the experience-based forecast does not just pick up the sticky-information effect of Mankiw and Reis (2002) and Carroll (2003).

6 Conclusion

Our analysis shows that inflation expectations depend on the inflation experiences that people accumulate during their lives. Differences in experienced mean inflation and inflation persistence generate (time-varying) differences in inflation expectations between cohorts. The experience of younger individuals is dominated by recent observations, while older individuals draw on a more extended historical data set in forming their expectations.

Learning from experience can explain, for example, why young individuals forecasted much higher inflation than older individuals following the high-inflation years of the late 1970s and early 1980s: Both the mean inflation rate and inflation persistence were particularly high in the short data set experienced by young individuals at the time. For recent years, instead, towards the end of our sample, our estimates imply a perceived persistence of inflation shocks close to zero, particularly for young individuals. This suggests that unexpected movements in inflation are currently unlikely to move inflation expectations much.

To further refine the understanding of expectations formation and the impact on financial decisions, it will be important to shed more light on the exact transmission channel for experience effects. For example, does the salience of an experience depend on individuals’ personal investment choices or financial constraints? Does it vary by macroeconomic conditions? These are important questions for future research.

More work is also needed to ascertain whether the learning-from-experience model applies more generally to other types of macroeconomic expectations. In this regard it is interesting to note that the weights individuals put on past inflation experiences, according to our estimates, are very similar to the weights individuals put on past stock-market return experiences when they choose asset allocations in their investment portfolios, according to
the estimates in Malmendier and Nagel (2011).\textsuperscript{13} This is remarkable since the weights we estimated here are based on a different data set, and since we analyze beliefs rather than investment choices. Taken together, these findings are suggestive that individuals process different types of macroeconomic experiences in similar ways when they form expectations.

\textsuperscript{13} The weighting function in Malmendier and Nagel (2011) is controlled by a parameter $\lambda$ which relates to $\theta$ in this paper as $\theta \approx \lambda + 1$ (see Online Appendix A), and is estimated in the range from 1.1 to 1.9.
References


